

2.1. Guide to the subgroup tables and graphs

BY HANS WONDRATSCHEK AND MOIS I. AROYO

2.1.1. Contents and arrangement of the subgroup tables

In this chapter, the subgroup tables, the subgroup graphs and their general organization are discussed. In the following sections, the different types of data are explained in detail. For every plane group and every space group there is a separate table of maximal subgroups and minimal supergroups. These items are listed either individually, or as members of (infinite) series, or both. In addition, there are graphs of *translationengleiche* and *klassengleiche* subgroups which contain for each space group all kinds of subgroups, not just the maximal ones.

The presentation of the plane-group and space-group data in the tables of Chapters 2.2 and 2.3 follows the style of the tables of Parts 6 (plane groups) and 7 (space groups) in Vol. A of *International Tables for Crystallography* (2002), henceforth abbreviated as *IT A*. The data comprise:

- Headline
- Generators selected
- General position
- I Maximal *translationengleiche* subgroups
- II Maximal *klassengleiche* subgroups
- I Minimal *translationengleiche* supergroups
- II Minimal non-isomorphic *klassengleiche* supergroups.

For the majority of groups, the data can be listed completely on one page. Sometimes two pages are needed. If the data extend less than half a page over one full page and data for a neighbouring space-group table ‘overflow’ to a similar extent, then the two overflows are displayed on the same page. Such deviations from the standard sequence are indicated on the relevant pages by a remark *Continued on . . .*. The two overflows are separated by a rule and are designated by their headlines.

The sequence of the plane groups and space groups \mathcal{G} in this volume follows exactly that of the tables of Part 6 (plane groups) and Part 7 (space groups) in *IT A*. The format of the subgroup tables has also been chosen to resemble that of the tables of *IT A* as far as possible. Examples of graphs of subgroups can also be found in Section 10.1.4.3 of *IT A*, but only for subgroups of point groups. The graphs for the space groups are described in Section 2.1.7.

2.1.2. Structure of the subgroup tables

Some basic data in these tables have been repeated from the tables of *IT A* in order to allow the use of the subgroup tables independently of *IT A*. These data and the main features of the tables are described in this section. More detailed descriptions are given in the following sections.

2.1.2.1. Headline

The headline contains the specification of the space group for which the maximal subgroups are considered. The headline lists from the outside margin inwards:

- (1) The *short (international) Hermann–Mauguin symbol* for the plane group or space group. These symbols will be henceforth referred to as ‘HM symbols’. HM symbols are discussed in detail in Chapter 12.2 of *IT A* with a brief summary in Section 2.2.4 of *IT A*.

- (2) The plane-group or space-group number as introduced in *International Tables for X-ray Crystallography*, Vol. I (1952). These numbers run from 1 to 17 for the plane groups and from 1 to 230 for the space groups.
- (3) The *full (international) Hermann–Mauguin symbol* for the plane or space group, abbreviated ‘full HM symbol’. This describes the symmetry in up to three symmetry directions (*Blickrichtungen*) more completely, see Table 12.3.4.1 of *IT A*, which also allows comparison with earlier editions of *International Tables*.
- (4) The *Schoenflies symbol* for the space group (there are no Schoenflies symbols for the plane groups). The Schoenflies symbols are primarily point-group symbols; they are extended by superscripts for a unique designation of the space-group types, cf. *IT A*, Sections 12.1.2 and 12.2.2.

2.1.2.2. Data from *IT A*

2.1.2.2.1. Generators selected

As in *IT A*, for each plane group and space group \mathcal{G} a set of symmetry operations is listed under the heading ‘Generators selected’. From these group elements, \mathcal{G} can be generated conveniently. The generators in this volume are the same as those in *IT A*. They are explained in Section 2.2.10 of *IT A* and the choice of the generators is explained in Section 8.3.5 of *IT A*.

The generators are listed again in this present volume because many of the subgroups are characterized by their generators. These (often nonconventional) generators of the subgroups can thus be compared with the conventional ones without reference to *IT A*.

2.1.2.2.2. General position

Like the generators, the general position has also been copied from *IT A*, where an explanation can be found in Section 2.2.11. The general position in *IT A* is the first block under the heading ‘Positions’, characterized by its site symmetry of 1. The elements of the general position have the following meanings:

- (1) they are coset representatives of the space group \mathcal{G} . The other elements of a coset are obtained from its representative by combination with translations of \mathcal{G} ;
- (2) they form a kind of shorthand notation for the matrix description of the coset representatives of \mathcal{G} ;
- (3) they are the coordinates of those symmetry-equivalent points that are obtained by the application of the coset representatives on a point with the coordinates x, y, z ;
- (4) their numbers refer to the geometric description of the symmetry operations in the block ‘Symmetry operations’ of the space-group tables of *IT A*.

Many of the subgroups \mathcal{H} in these tables are characterized by the elements of their general position. These elements are specified by numbers which refer to the corresponding numbers in the general position of \mathcal{G} . Other subgroups are listed by the numbers of their generators, which again refer to the corresponding numbers in the general position of \mathcal{G} . Therefore, the listing of the general position of \mathcal{G} as well as the listing of the generators of \mathcal{G} is essential for