

$P4/m$

No. 83

 $P4/m$
 C_{4h}^1
Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5)

General position

 Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

| | | | | | | |
|---|----------|---|---------------------------------|---------------------------|---------------------------|---------------------------|
| 8 | <i>l</i> | 1 | (1) x, y, z | (2) \bar{x}, \bar{y}, z | (3) \bar{y}, x, z | (4) y, \bar{x}, z |
| | | | (5) $\bar{x}, \bar{y}, \bar{z}$ | (6) x, y, \bar{z} | (7) y, \bar{x}, \bar{z} | (8) \bar{y}, x, \bar{z} |

I Maximal translationengleiche subgroups

| | |
|----------------------------|------------|
| [2] $P\bar{4}$ (81) | 1; 2; 7; 8 |
| [2] $P4$ (75) | 1; 2; 3; 4 |
| [2] $P2/m$ (10, $P112/m$) | 1; 2; 5; 6 |

II Maximal klassengleiche subgroups

• Enlarged unit cell

| | | | |
|---|---|---|---------------|
| [2] $\mathbf{c}' = 2\mathbf{c}$ | | | |
| $P4_2/m$ (84) | $\langle 2; 5; 3 + (0,0,1) \rangle$ | $\mathbf{a}, \mathbf{b}, 2\mathbf{c}$ | |
| $P4_2/m$ (84) | $\langle 2; (3; 5) + (0,0,1) \rangle$ | $\mathbf{a}, \mathbf{b}, 2\mathbf{c}$ | 0, 0, 1/2 |
| $P4/m$ (83) | $\langle 2; 3; 5 \rangle$ | $\mathbf{a}, \mathbf{b}, 2\mathbf{c}$ | |
| $P4/m$ (83) | $\langle 2; 3; 5 + (0,0,1) \rangle$ | $\mathbf{a}, \mathbf{b}, 2\mathbf{c}$ | 0, 0, 1/2 |
| [2] $\mathbf{a}' = 2\mathbf{a}, \mathbf{b}' = 2\mathbf{b}$ | | | |
| $C4/e$ (85, $P4/n$) | $\langle 2; 3; 5 + (1,0,0) \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, \mathbf{c}$ | 1/2, 0, 0 |
| $C4/e$ (85, $P4/n$) | $\langle 2 + (1,1,0); 3 + (1,0,0); 5 + (0,1,0) \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, \mathbf{c}$ | 0, 1/2, 0 |
| $C4/m$ (83, $P4/m$) | $\langle 2; 3; 5 \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, \mathbf{c}$ | |
| $C4/m$ (83, $P4/m$) | $\langle (2; 5) + (1,1,0); 3 + (1,0,0) \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, \mathbf{c}$ | 1/2, 1/2, 0 |
| [2] $\mathbf{a}' = 2\mathbf{a}, \mathbf{b}' = 2\mathbf{b}, \mathbf{c}' = 2\mathbf{c}$ | | | |
| $F4/m$ (87, $I4/m$) | $\langle 2; 3; 5 \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, 2\mathbf{c}$ | |
| $F4/m$ (87, $I4/m$) | $\langle 2; 3; 5 + (0,0,1) \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, 2\mathbf{c}$ | 0, 0, 1/2 |
| $F4/m$ (87, $I4/m$) | $\langle (2; 5) + (1,1,0); 3 + (1,0,0) \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, 2\mathbf{c}$ | 1/2, 1/2, 0 |
| $F4/m$ (87, $I4/m$) | $\langle 2 + (1,1,0); 3 + (1,0,0); 5 + (1,1,1) \rangle$ | $\mathbf{a} - \mathbf{b}, \mathbf{a} + \mathbf{b}, 2\mathbf{c}$ | 1/2, 1/2, 1/2 |
| [3] $\mathbf{c}' = 3\mathbf{c}$ | | | |
| $P4/m$ (83) | $\langle 2; 3; 5 \rangle$ | $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$ | |
| $P4/m$ (83) | $\langle 2; 3; 5 + (0,0,2) \rangle$ | $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$ | 0, 0, 1 |
| $P4/m$ (83) | $\langle 2; 3; 5 + (0,0,4) \rangle$ | $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$ | 0, 0, 2 |

• Series of maximal isomorphic subgroups

| | | | |
|--|--|--|-----------|
| [p] $\mathbf{c}' = p\mathbf{c}$ | | | |
| $P4/m$ (83) | $\langle 2; 3; 5 + (0,0,2u) \rangle$ $p > 2; 0 \leq u < p$ p conjugate subgroups for the prime p | $\mathbf{a}, \mathbf{b}, p\mathbf{c}$ | 0, 0, u |
| [p^2] $\mathbf{a}' = p\mathbf{a}, \mathbf{b}' = p\mathbf{b}$ | | | |
| $P4/m$ (83) | $\langle (2; 5) + (2u, 2v, 0); 3 + (u + v, -u + v, 0) \rangle$ $p > 2; 0 \leq u < p; 0 \leq v < p$ p^2 conjugate subgroups for prime $p \equiv 3 \pmod{4}$ | $p\mathbf{a}, p\mathbf{b}, \mathbf{c}$ | $u, v, 0$ |
| [$p = q^2 + r^2$] $\mathbf{a}' = q\mathbf{a} - r\mathbf{b}, \mathbf{b}' = r\mathbf{a} + q\mathbf{b}$ | | | |
| $P4/m$ (83) | $\langle (2; 5) + (2u, 0, 0); 3 + (u, -u, 0) \rangle$ $q > 0; r > 0; p > 4; 0 \leq u < p$ p conjugate subgroups for prime $p \equiv 1 \pmod{4}$ | $q\mathbf{a} - r\mathbf{b}, r\mathbf{a} + q\mathbf{b}, \mathbf{c}$ | $u, 0, 0$ |

I Minimal translationengleiche supergroups

 [2] $P4/mmm$ (123); [2] $P4/mcc$ (124); [2] $P4/mbm$ (127); [2] $P4/mnc$ (128)

II Minimal non-isomorphic klassengleiche supergroups

• Additional centring translations

 [2] $I4/m$ (87)

• Decreased unit cell

none