

$P4/nbm$

No. 125

 $P4/n2/b2/m$
 D_{4h}^3

 ORIGIN CHOICE 1, Origin at 422 at $4/n22/g$, at $-\frac{1}{4}, -\frac{1}{4}, 0$ from centre ($2/m$)

 Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5); (9)

General position

 Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

| | | | | | | |
|----|-----|---|---|--|--|--|
| 16 | n | 1 | (1) x, y, z | (2) \bar{x}, \bar{y}, z | (3) \bar{y}, x, z | (4) y, \bar{x}, z |
| | | | (5) \bar{x}, y, \bar{z} | (6) x, \bar{y}, \bar{z} | (7) y, x, \bar{z} | (8) $\bar{y}, \bar{x}, \bar{z}$ |
| | | | (9) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, \bar{z}$ | (10) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$ | (11) $y + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z}$ | (12) $\bar{y} + \frac{1}{2}, x + \frac{1}{2}, \bar{z}$ |
| | | | (13) $x + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$ | (14) $\bar{x} + \frac{1}{2}, y + \frac{1}{2}, z$ | (15) $\bar{y} + \frac{1}{2}, \bar{x} + \frac{1}{2}, z$ | (16) $y + \frac{1}{2}, x + \frac{1}{2}, z$ |

I Maximal translationengleiche subgroups

| | | | |
|------------------------------|----------------------------|----------------------------|-------------|
| [2] $P4b2$ (117) | 1; 2; 7; 8; 11; 12; 13; 14 | | 0, 1/2, 0 |
| [2] $P42m$ (111) | 1; 2; 5; 6; 11; 12; 15; 16 | | 0, 1/2, 0 |
| [2] $P4bm$ (100) | 1; 2; 3; 4; 13; 14; 15; 16 | | |
| [2] $P422$ (89) | 1; 2; 3; 4; 5; 6; 7; 8 | | |
| [2] $P4/n11$ (85, $P4/n$) | 1; 2; 3; 4; 9; 10; 11; 12 | | 0, 1/2, 0 |
| [2] $P2/n12/m$ (67, $Cmme$) | 1; 2; 7; 8; 9; 10; 15; 16 | $\mathbf{a - b, a + b, c}$ | 1/4, 3/4, 0 |
| [2] $P2/n2/b1$ (50, $Pban$) | 1; 2; 5; 6; 9; 10; 13; 14 | | |

II Maximal klassengleiche subgroups

• Enlarged unit cell

 [2] $\mathbf{c}' = 2\mathbf{c}$

| | | | |
|------------------|--|---------------------|-------------|
| $P4_2/nm$ (134) | $\langle 2; 9; (3; 5) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 1/2, 1/2 |
| $P4_2/nm$ (134) | $\langle 2; 5; (3; 9) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 1/2, 0 |
| $P4_2/nbc$ (133) | $\langle 2; 5; 9; 3 + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 1/2, 1/2 |
| $P4_2/nbc$ (133) | $\langle 2; (3; 5; 9) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 1/2, 0 |
| $P4/nnc$ (126) | $\langle 2; 3; 9; 5 + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 0, 1/2 |
| $P4/nnc$ (126) | $\langle 2; 3; 5; 9 + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | |
| $P4/nbm$ (125) | $\langle 2; 3; 5; 9 \rangle$ | $\mathbf{a, b, 2c}$ | |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 0, 1/2 |

 [3] $\mathbf{c}' = 3\mathbf{c}$

| | | | |
|----------------|--|---------------------|---------|
| $P4/nbm$ (125) | $\langle 2; 3; 5; 9 \rangle$ | $\mathbf{a, b, 3c}$ | |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 2) \rangle$ | $\mathbf{a, b, 3c}$ | 0, 0, 1 |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 4) \rangle$ | $\mathbf{a, b, 3c}$ | 0, 0, 2 |

• Series of maximal isomorphic subgroups

 [p] $\mathbf{c}' = p\mathbf{c}$

| | | | |
|----------------|---|---------------------|-----------|
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 2u) \rangle$ | $\mathbf{a, b, pc}$ | 0, 0, u |
| | $p > 2; 0 \leq u < p$ | | |
| | p conjugate subgroups for the prime p | | |

 [p²] $\mathbf{a}' = p\mathbf{a}, \mathbf{b}' = p\mathbf{b}$

| | | | |
|----------------|---|----------------------|-----------|
| $P4/nbm$ (125) | $\langle 2 + (2u, 2v, 0); 3 + (u + v, -u + v, 0); 5 + (2u, 0, 0);$ | $\mathbf{pa, pb, c}$ | $u, v, 0$ |
| | $9 + (\frac{p}{2} - \frac{1}{2} + 2u, \frac{p}{2} - \frac{1}{2} + 2v, 0) \rangle$ | | |
| | $p > 2; 0 \leq u < p; 0 \leq v < p$ | | |
| | p^2 conjugate subgroups for the prime p | | |

I Minimal translationengleiche supergroups

none

II Minimal non-isomorphic klassengleiche supergroups

• Additional centring translations

 [2] $C4/mmm$ (123, $P4/mmm$); [2] $I4/mcm$ (140)

• Decreased unit cell

none

ORIGIN CHOICE 2, Origin at centre ($2/m$) at $n(b, a)(2_1/g, 2/m)$, at $\frac{1}{4}, \frac{1}{4}, 0$ from 422

Generators selected (1); $t(1, 0, 0)$; $t(0, 1, 0)$; $t(0, 0, 1)$; (2); (3); (5); (9)

General position

Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

| | | | | | | |
|----|-----|---|---|---|--|---|
| 16 | n | 1 | (1) x, y, z | (2) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$ | (3) $\bar{y} + \frac{1}{2}, x, z$ | (4) $y, \bar{x} + \frac{1}{2}, z$ |
| | | | (5) $\bar{x} + \frac{1}{2}, y, \bar{z}$ | (6) $x, \bar{y} + \frac{1}{2}, \bar{z}$ | (7) y, x, \bar{z} | (8) $\bar{y} + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z}$ |
| | | | (9) $\bar{x}, \bar{y}, \bar{z}$ | (10) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$ | (11) $y + \frac{1}{2}, \bar{x}, \bar{z}$ | (12) $\bar{y}, x + \frac{1}{2}, \bar{z}$ |
| | | | (13) $x + \frac{1}{2}, \bar{y}, z$ | (14) $\bar{x}, y + \frac{1}{2}, z$ | (15) \bar{y}, \bar{x}, z | (16) $y + \frac{1}{2}, x + \frac{1}{2}, z$ |

I Maximal translationengleiche subgroups

| | | | |
|------------------------------|----------------------------|----------------------------|-------------|
| [2] $P\bar{4}b2$ (117) | 1; 2; 7; 8; 11; 12; 13; 14 | | 1/4, 3/4, 0 |
| [2] $P42m$ (111) | 1; 2; 5; 6; 11; 12; 15; 16 | | 1/4, 3/4, 0 |
| [2] $P4bm$ (100) | 1; 2; 3; 4; 13; 14; 15; 16 | | 1/4, 1/4, 0 |
| [2] $P422$ (89) | 1; 2; 3; 4; 5; 6; 7; 8 | | 1/4, 1/4, 0 |
| [2] $P4/n11$ (85, $P4/n$) | 1; 2; 3; 4; 9; 10; 11; 12 | | |
| [2] $P2/n12/m$ (67, $Cmme$) | 1; 2; 7; 8; 9; 10; 15; 16 | $\mathbf{a - b, a + b, c}$ | 0, 1/2, 0 |
| [2] $P2/n2/b1$ (50, $Pban$) | 1; 2; 5; 6; 9; 10; 13; 14 | | |

II Maximal klassengleiche subgroups

• **Enlarged unit cell**

| | | | |
|---------------------------------|--|---------------------|-----------|
| [2] $\mathbf{c}' = 2\mathbf{c}$ | | | |
| $P4_2/nnm$ (134) | $\langle 2; 9; (3; 5) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | |
| $P4_2/nm$ (134) | $\langle 2; 5; (3; 9) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 0, 1/2 |
| $P4_2/nbc$ (133) | $\langle 2; 5; 9; 3 + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | |
| $P4_2/nbc$ (133) | $\langle 2; (3; 5; 9) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 0, 1/2 |
| $P4/nmc$ (126) | $\langle 2; 3; 9; 5 + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | |
| $P4/nmc$ (126) | $\langle 2; 3; 5; 9 + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 0, 1/2 |
| $P4/nbm$ (125) | $\langle 2; 3; 5; 9 \rangle$ | $\mathbf{a, b, 2c}$ | |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 1) \rangle$ | $\mathbf{a, b, 2c}$ | 0, 0, 1/2 |
| [3] $\mathbf{c}' = 3\mathbf{c}$ | | | |
| $P4/nbm$ (125) | $\langle 2; 3; 5; 9 \rangle$ | $\mathbf{a, b, 3c}$ | |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 2) \rangle$ | $\mathbf{a, b, 3c}$ | 0, 0, 1 |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 4) \rangle$ | $\mathbf{a, b, 3c}$ | 0, 0, 2 |

• **Series of maximal isomorphic subgroups**

| | | | |
|--|--|----------------------|-----------|
| [p] $\mathbf{c}' = p\mathbf{c}$ | | | |
| $P4/nbm$ (125) | $\langle 2; 3; (5; 9) + (0, 0, 2u) \rangle$ $p > 2; 0 \leq u < p$ p conjugate subgroups for the prime p | $\mathbf{a, b, pc}$ | 0, 0, u |
| [p^2] $\mathbf{a}' = p\mathbf{a}, \mathbf{b}' = p\mathbf{b}$ | | | |
| $P4/nbm$ (125) | $\langle 2 + (\frac{p}{2} - \frac{1}{2} + 2u, \frac{p}{2} - \frac{1}{2} + 2v, 0);$ $3 + (\frac{p}{2} - \frac{1}{2} + u + v, -u + v, 0); 5 + (\frac{p}{2} - \frac{1}{2} + 2u, 0, 0);$ $9 + (2u, 2v, 0) \rangle$ $p > 2; 0 \leq u < p; 0 \leq v < p$ p^2 conjugate subgroups for the prime p | $\mathbf{pa, pb, c}$ | $u, v, 0$ |

I Minimal translationengleiche supergroups

none

II Minimal non-isomorphic klassengleiche supergroups

• **Additional centring translations**

[2] $C4/mmm$ (123, $P4/mmm$); [2] $I4/mcm$ (140)

• **Decreased unit cell**

none