

C_{2h}^6
 $C12/c1$

No. 15

 $C2/c$

 UNIQUE AXIS b , CELL CHOICE 1

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(\frac{1}{2},\frac{1}{2},0)$; (2); (3)

General position

 Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

8	f	1	(1) x, y, z	(2) $\bar{x}, y, \bar{z} + \frac{1}{2}$	(3) $\bar{x}, \bar{y}, \bar{z}$	(4) $x, \bar{y}, z + \frac{1}{2}$			

I Maximal translationengleiche subgroups

[2] $C1c1$ (9)	(1; 4)+	
[2] $C121$ (5)	(1; 2)+	0, 0, 1/4
[2] $C\bar{1}$ (2, $P\bar{1}$)	(1; 3)+	$1/2(\mathbf{a} - \mathbf{b}), 1/2(\mathbf{a} + \mathbf{b}), \mathbf{c}$

II Maximal klassengleiche subgroups

• Loss of centring translations

[2] $P12_1/n1$ (14, $P12_1/c1$)	1; 3; (2; 4) + $(\frac{1}{2}, \frac{1}{2}, 0)$	c, b, $-\mathbf{a} - \mathbf{c}$
[2] $P12_1/c1$ (14)	1; 4; (2; 3) + $(\frac{1}{2}, \frac{1}{2}, 0)$	1/4, 1/4, 0
[2] $P12/c1$ (13)	1; 2; 3; 4	
[2] $P12/n1$ (13, $P12/c1$)	1; 2; (3; 4) + $(\frac{1}{2}, \frac{1}{2}, 0)$	c, b, $-\mathbf{a} - \mathbf{c}$ 1/4, 1/4, 0

• Enlarged unit cell

[3] $\mathbf{b}' = 3\mathbf{b}$											
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$C12/c1$ (15)	⟨2; 3⟩	a, 3b, c									
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[3] $\mathbf{c}' = 3\mathbf{c}$											
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$C12/c1$ (15)	⟨3; 2 + (0, 0, 1)⟩	a - 2c, b, 3c									
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$C12/c1$ (15)	⟨3; 2 + (0, 0, 1)⟩	a - 4c, b, 3c									
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[3] $\mathbf{a}' = 3\mathbf{a}$											
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$C12/c1$ (15)	⟨2; 3⟩	3a, b, c									
$C12/c1$ (15)	⟨(2; 3) + (2, 0, 0)⟩	1, 0, 0									
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• Series of maximal isomorphic subgroups

[p] $\mathbf{b}' = p\mathbf{b}$		
$C12/c1$ (15)	⟨2; 3 + (0, 2u, 0)⟩ prime $p > 2$; $0 \leq u < p$ p conjugate subgroups	a, pb, c 0, u, 0
[p] $\mathbf{a}' = \mathbf{a} - 2q\mathbf{c}, \mathbf{c}' = p\mathbf{c}$		
$C12/c1$ (15)	⟨2 + (0, 0, $\frac{p}{2} - \frac{1}{2} + 2u$); 3 + (0, 0, 2u)⟩ prime $p > 2$; $0 \leq q < p$; $0 \leq u < p$ p conjugate subgroups for each pair of q and p	a - 2qc, b, pc 0, 0, u
[p] $\mathbf{a}' = p\mathbf{a}$		
$C12/c1$ (15)	⟨(2; 3) + (2u, 0, 0)⟩ prime $p > 2$; $0 \leq u < p$ p conjugate subgroups	pa, b, c u, 0, 0

I Minimal translationengleiche supergroups

[2] *Cmcm* (63); [2] *Cmce* (64); [2] *Cccm* (66); [2] *Ccce* (68); [2] *Fddd* (70); [2] *Ibam* (72); [2] *Ibca* (73); [2] *Imma* (74); [2] *I4₁/a* (88);
 [3] *P $\bar{3}$ 12/c* (163, *P $\bar{3}$ 1c*); [3] *P $\bar{3}$ 2/c1* (165, *P $\bar{3}$ c1*); [3] *R $\bar{3}$ 2/c* (167, *R $\bar{3}$ c*)

II Minimal non-isomorphic klassengleiche supergroups

- Additional centring translations

[2] *F12/m1* (12, *C12/m1*)

- Decreased unit cell

[2] $\mathbf{c}' = \frac{1}{2}\mathbf{c}$ *C12/m1* (12); [2] $\mathbf{a}' = \frac{1}{2}\mathbf{a}$, $\mathbf{b}' = \frac{1}{2}\mathbf{b}$ *P12/c1* (13)

I Minimal translationengleiche supergroups

[2] *Cmcm* (63); [2] *Cmce* (64); [2] *Cccm* (66); [2] *Ccce* (68); [2] *Fddd* (70); [2] *Ibam* (72); [2] *Ibca* (73); [2] *Imma* (74); [2] *I4₁/a* (88);
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II Minimal non-isomorphic klassengleiche supergroups

- Additional centring translations

[2] *F112/m* (12, *A112/m*)

- Decreased unit cell

[2] $\mathbf{a}' = \frac{1}{2}\mathbf{a}$ *A112/m* (12); [2] $\mathbf{b}' = \frac{1}{2}\mathbf{b}$, $\mathbf{c}' = \frac{1}{2}\mathbf{c}$ *P112/a* (13)

UNIQUE AXIS *c*, CELL CHOICE 1Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(0, \frac{1}{2}, \frac{1}{2})$; (2); (3)

General position

Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

(0,0,0)+ (0, $\frac{1}{2}$, $\frac{1}{2}$)+8 *f* 1(1) x, y, z (2) $\bar{x} + \frac{1}{2}, \bar{y}, z$ (3) $\bar{x}, \bar{y}, \bar{z}$ (4) $x + \frac{1}{2}, y, \bar{z}$ I Maximal *translationengleiche* subgroups

[2] A11a (9)	(1; 4)+		
[2] A112 (5)	(1; 2)+		1/4, 0, 0
[2] A $\bar{1}$ (2, P $\bar{1}$)	(1; 3)+	a, 1/2(b - c), 1/2(b + c)	

II Maximal *klassengleiche* subgroups

• Loss of centring translations

[2] P112 ₁ /n (14, P112 ₁ /a)	1; 3; (2; 4) + (0, $\frac{1}{2}$, $\frac{1}{2}$)	-a - b, a, c	
[2] P112 ₁ /a (14)	1; 4; (2; 3) + (0, $\frac{1}{2}$, $\frac{1}{2}$)		0, 1/4, 1/4
[2] P112/a (13)	1; 2; 3; 4		
[2] P112/n (13, P112/a)	1; 2; (3; 4) + (0, $\frac{1}{2}$, $\frac{1}{2}$)	-a - b, a, c	0, 1/4, 1/4

• Enlarged unit cell

[3] c' = 3c			
{ A112/a (15)	{ (2; 3)	a, b, 3c	
{ A112/a (15)	{ (2; 3 + (0, 0, 2))	a, b, 3c	0, 0, 1
{ A112/a (15)	{ (2; 3 + (0, 0, 4))	a, b, 3c	0, 0, 2
[3] a' = 3a			
{ A112/a (15)	{ (3; 2 + (1, 0, 0))	3a, b, c	
{ A112/a (15)	{ (2 + (3, 0, 0); 3 + (2, 0, 0))	3a, b, c	1, 0, 0
{ A112/a (15)	{ (2 + (5, 0, 0); 3 + (4, 0, 0))	3a, b, c	2, 0, 0
[3] a' = 3a, b' = -2a + b			
{ A112/a (15)	{ (3; 2 + (1, 0, 0))	3a, -2a + b, c	
{ A112/a (15)	{ (2 + (3, 0, 0); 3 + (2, 0, 0))	3a, -2a + b, c	1, 0, 0
{ A112/a (15)	{ (2 + (5, 0, 0); 3 + (4, 0, 0))	3a, -2a + b, c	2, 0, 0
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{ A112/a (15)	{ (3; 2 + (1, 0, 0))	3a, -4a + b, c	
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{ A112/a (15)	{ (2 + (5, 0, 0); 3 + (4, 0, 0))	3a, -4a + b, c	2, 0, 0
[3] b' = 3b			
{ A112/a (15)	{ (2; 3)	a, 3b, c	
{ A112/a (15)	{ ((2; 3) + (0, 2, 0))	a, 3b, c	0, 1, 0
{ A112/a (15)	{ ((2; 3) + (0, 4, 0))	a, 3b, c	0, 2, 0

• Series of maximal isomorphic subgroups

[<i>p</i>] c' = pc			
A112/a (15)	{ (2; 3 + (0, 0, 2 <i>u</i>))	a, b, pc	0, 0, <i>u</i>
	prime $p > 2$; $0 \leq u < p$		
	<i>p</i> conjugate subgroups		
[<i>p</i>] a' = pa, b' = -2qa + b			
A112/a (15)	{ (2 + ($\frac{p}{2} - \frac{1}{2} + 2u, 0, 0$); 3 + (2 <i>u</i> , 0, 0))	pa, -2qa + b, c	<i>u</i> , 0, 0
	prime $p > 2$; $0 \leq q < p$; $0 \leq u < p$		
	<i>p</i> conjugate subgroups for each pair of <i>q</i> and <i>p</i>		
[<i>p</i>] b' = pb			
A112/a (15)	{ ((2; 3) + (0, 2 <i>u</i> , 0))	a, pb, c	0, <i>u</i> , 0
	prime $p > 2$; $0 \leq u < p$		
	<i>p</i> conjugate subgroups		

(Continued on the facing page)

I Minimal translationengleiche supergroups

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II Minimal non-isomorphic klassengleiche supergroups

- Additional centring translations

[2] *F12/m1* (12, *C12/m1*)

- Decreased unit cell

[2] $\mathbf{c}' = \frac{1}{2}\mathbf{c}$ *C12/m1* (12); [2] $\mathbf{a}' = \frac{1}{2}\mathbf{a}$, $\mathbf{b}' = \frac{1}{2}\mathbf{b}$ *P12/c1* (13)

I Minimal translationengleiche supergroups

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II Minimal non-isomorphic klassengleiche supergroups

- Additional centring translations

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- Decreased unit cell

[2] $\mathbf{a}' = \frac{1}{2}\mathbf{a}$ *A112/m* (12); [2] $\mathbf{b}' = \frac{1}{2}\mathbf{b}$, $\mathbf{c}' = \frac{1}{2}\mathbf{c}$ *P112/a* (13)