

$I4/m$ 

No. 87

 $I4/m$  $C_{4h}^5$ Generators selected (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ;  $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$ ; (2); (3); (5)

## General position

Multiplicity, Wyckoff letter, Site symmetry	Coordinates
16 <i>i</i> 1	$(0,0,0)+ (\frac{1}{2},\frac{1}{2},\frac{1}{2})+$ (1) $x,y,z$ (2) $\bar{x},\bar{y},z$ (3) $\bar{y},x,z$ (4) $y,\bar{x},z$ (5) $\bar{x},\bar{y},\bar{z}$ (6) $x,y,\bar{z}$ (7) $y,\bar{x},\bar{z}$ (8) $\bar{y},x,\bar{z}$

I Maximal *translationengleiche* subgroups

[2] $I\bar{4}$ (82)	(1; 2; 7; 8)+	
[2] $I4$ (79)	(1; 2; 3; 4)+	
[2] $I2/m$ (12, $A112/m$ )	(1; 2; 5; 6)+	<b>b, -a - b, c</b>

II Maximal *klassengleiche* subgroups

## • Loss of centring translations

[2] $P4_2/n$ (86)	1; 2; 7; 8; (3; 4; 5; 6) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$	1/4, 1/4, 1/4
[2] $P4/n$ (85)	1; 2; 3; 4; (5; 6; 7; 8) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$	1/4, 1/4, 1/4
[2] $P4_2/m$ (84)	1; 2; 5; 6; (3; 4; 7; 8) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$	0, 1/2, 0
[2] $P4/m$ (83)	1; 2; 3; 4; 5; 6; 7; 8	

## • Enlarged unit cell

[3] $\mathbf{c}' = 3\mathbf{c}$			
$\left\{ \begin{array}{l} I4/m \text{ (87)} \\ I4/m \text{ (87)} \\ I4/m \text{ (87)} \end{array} \right.$	$\langle 2; 3; 5 \rangle$ $\langle 2; 3; 5 + (0,0,2) \rangle$ $\langle 2; 3; 5 + (0,0,4) \rangle$	<b>a, b, 3c</b> <b>a, b, 3c</b> <b>a, b, 3c</b>	0, 0, 1 0, 0, 2

## • Series of maximal isomorphic subgroups

[ $p$ ] $\mathbf{c}' = p\mathbf{c}$			
$I4/m$ (87)	$\langle 2; 3; 5 + (0,0,2u) \rangle$ prime $p > 2$ ; $0 \leq u < p$ $p$ conjugate subgroups	<b>a, b, <math>p\mathbf{c}</math></b>	0, 0, $u$
[ $p^2$ ] $\mathbf{a}' = p\mathbf{a}$ , $\mathbf{b}' = p\mathbf{b}$			
$I4/m$ (87)	$\langle (2; 5) + (2u, 2v, 0); 3 + (u + v, -u + v, 0) \rangle$ prime $p > 2$ ; $0 \leq u < p$ ; $0 \leq v < p$ $p^2$ conjugate subgroups for $p = 4n - 1$	<b><math>p\mathbf{a}</math>, <math>p\mathbf{b}</math>, <math>\mathbf{c}</math></b>	$u, v, 0$
[ $p = q^2 + r^2$ ] $\mathbf{a}' = q\mathbf{a} - r\mathbf{b}$ , $\mathbf{b}' = r\mathbf{a} + q\mathbf{b}$			
$I4/m$ (87)	$\langle (2; 5) + (2u, 0, 0); 3 + (u, -u, 0) \rangle$ prime $p > 4$ ; $q > 0$ ; $r > 0$ ; $0 \leq u < p$ $p$ conjugate subgroups for $p = 4n + 1$	<b><math>q\mathbf{a} - r\mathbf{b}</math>, <math>r\mathbf{a} + q\mathbf{b}</math>, <math>\mathbf{c}</math></b>	$u, 0, 0$

I Minimal *translationengleiche* supergroups[2]  $I4/mmm$  (139); [2]  $I4/mcm$  (140)II Minimal non-isomorphic *klassengleiche* supergroups

## • Additional centring translations

none

## • Decreased unit cell

[2]  $\mathbf{c}' = \frac{1}{2}\mathbf{c}$   $C4/m$  (83),  $P4/m$