

$I4_122$ 

No. 98

 $I4_122$ 
 $D_4^{10}$ 
**Generators selected** (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ;  $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$ ; (2); (3); (5)

**General position**

 Multiplicity,  
Wyckoff letter,  
Site symmetry

**Coordinates**
 $(0,0,0)+ (\frac{1}{2},\frac{1}{2},\frac{1}{2})+$ 

16	g	1	(1) $x,y,z$	(2) $\bar{x}+\frac{1}{2},\bar{y}+\frac{1}{2},z+\frac{1}{2}$	(3) $\bar{y},x+\frac{1}{2},z+\frac{1}{4}$	(4) $y+\frac{1}{2},\bar{x},z+\frac{3}{4}$
			(5) $\bar{x}+\frac{1}{2},y,\bar{z}+\frac{3}{4}$	(6) $x,\bar{y}+\frac{1}{2},\bar{z}+\frac{1}{4}$	(7) $y+\frac{1}{2},x+\frac{1}{2},\bar{z}+\frac{1}{2}$	(8) $\bar{y},\bar{x},\bar{z}$

**I Maximal translationengleiche subgroups**

[2] $I4_111$ (80, $I4_1$ )	(1; 2; 3; 4)+	
[2] $I2_121$ (24, $I2_12_12_1$ )	(1; 2; 5; 6)+	0, 1/4, 3/8
[2] $I2_112$ (22, $F222$ )	(1; 2; 7; 8)+	$\mathbf{a}-\mathbf{b}, \mathbf{a}+\mathbf{b}, \mathbf{c}$

**II Maximal klassengleiche subgroups**

## • Loss of centring translations

[2] $P4_32_12$ (96)	1; 2; 7; 8; (3; 4; 5; 6) + $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$	1/4, 3/4, 1/4
[2] $P4_322$ (95)	1; 2; 5; 6; (3; 4; 7; 8) + $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$	1/4, 1/4, 3/8
[2] $P4_12_12$ (92)	1; 2; 3; 4; (5; 6; 7; 8) + $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$	1/4, 1/4, 0
[2] $P4_122$ (91)	1; 2; 3; 4; 5; 6; 7; 8	3/4, 1/4, 3/8

## • Enlarged unit cell

[3] $\mathbf{c}' = 3\mathbf{c}$		
$\left\{ \begin{array}{l} I4_122 \text{ (98)} \\ I4_122 \text{ (98)} \\ I4_122 \text{ (98)} \end{array} \right.$	$\langle 2 + (1,0,1); 3 + (\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}); 5 + (1,0,2) \rangle$ $\langle 2 + (1,0,1); 3 + (\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}); 5 + (1,0,4) \rangle$ $\langle 2 + (1,0,1); 3 + (\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}); 5 + (1,0,6) \rangle$	$\mathbf{a}, \mathbf{b}, 3\mathbf{c}$ $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$ $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$
		1/2, 0, 1/4
		1/2, 0, 5/4
		1/2, 0, 9/4

## • Series of maximal isomorphic subgroups

[ $p$ ] $\mathbf{c}' = p\mathbf{c}$		
$I4_122$ (98)	$\langle 2 + (0,0,\frac{p}{2}-\frac{1}{2}); 3 + (0,0,\frac{p}{4}-\frac{1}{4}); 5 + (0,0,\frac{3p}{4}-\frac{3}{4}+2u) \rangle$ prime $p > 4$ ; $0 \leq u < p$ $p$ conjugate subgroups for $p = 4n + 1$	$\mathbf{a}, \mathbf{b}, p\mathbf{c}$
	$I4_122$ (98)	$\langle 2 + (1,0,\frac{p}{2}-\frac{1}{2}); 3 + (\frac{1}{2}, -\frac{1}{2}, \frac{p}{4}-\frac{1}{4}); 5 + (1,0,\frac{3p}{4}-\frac{1}{4}+2u) \rangle$ prime $p > 2$ ; $0 \leq u < p$ $p$ conjugate subgroups for $p = 4n - 1$
[ $p^2$ ] $\mathbf{a}' = p\mathbf{a}, \mathbf{b}' = p\mathbf{b}$		
$I4_122$ (98)	$\langle 2 + (\frac{p}{2}-\frac{1}{2}+2u, \frac{p}{2}-\frac{1}{2}+2v, 0); 3 + (u+v, \frac{p}{2}-\frac{1}{2}-u+v, 0); 5 + (\frac{p}{2}-\frac{1}{2}+2u, 0, 0) \rangle$ prime $p > 2$ ; $0 \leq u < p$ ; $0 \leq v < p$ $p^2$ conjugate subgroups	$p\mathbf{a}, p\mathbf{b}, \mathbf{c}$
		$u, v, 0$

**I Minimal translationengleiche supergroups**

 [2]  $I4_1/amd$  (141); [2]  $I4_1/acd$  (142); [3]  $F4_132$  (210); [3]  $I4_132$  (214)

**II Minimal non-isomorphic klassengleiche supergroups**

## • Additional centring translations

none

## • Decreased unit cell

 [2]  $\mathbf{c}' = \frac{1}{2}\mathbf{c}$   $C4_222$  (93),  $P4_222$