



**Generators selected** (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ;  $t(0, \frac{1}{2}, \frac{1}{2})$ ;  $t(\frac{1}{2}, 0, \frac{1}{2})$ ; (2); (3); (5)

**Positions**

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions
	$(0,0,0)+$	$(0, \frac{1}{2}, \frac{1}{2})+$	$(\frac{1}{2}, 0, \frac{1}{2})+$	$(\frac{1}{2}, \frac{1}{2}, 0)+$	
32 <i>p</i> 1	(1) $x, y, z$ (5) $\bar{x}, \bar{y}, \bar{z}$	(2) $\bar{x}, \bar{y}, z$ (6) $x, y, \bar{z}$	(3) $\bar{x}, y, \bar{z}$ (7) $x, \bar{y}, z$	(4) $x, \bar{y}, \bar{z}$ (8) $\bar{x}, y, z$	General: $hkl : h+k, h+l, k+l = 2n$ $0kl : k, l = 2n$ $h0l : h, l = 2n$ $hk0 : h, k = 2n$ $h00 : h = 2n$ $0k0 : k = 2n$ $00l : l = 2n$  Special: as above, plus no extra conditions
16 <i>o</i> . . <i>m</i>	$x, y, 0$	$\bar{x}, \bar{y}, 0$	$\bar{x}, y, 0$	$x, \bar{y}, 0$	no extra conditions
16 <i>n</i> . <i>m</i> .	$x, 0, z$	$\bar{x}, 0, z$	$\bar{x}, 0, \bar{z}$	$x, 0, \bar{z}$	no extra conditions
16 <i>m</i> <i>m</i> . .	$0, y, z$	$0, \bar{y}, z$	$0, y, \bar{z}$	$0, \bar{y}, \bar{z}$	no extra conditions
16 <i>l</i> 2 . .	$x, \frac{1}{4}, \frac{1}{4}$	$\bar{x}, \frac{3}{4}, \frac{1}{4}$	$\bar{x}, \frac{3}{4}, \frac{3}{4}$	$x, \frac{1}{4}, \frac{3}{4}$	$hkl : h = 2n$
16 <i>k</i> . 2 .	$\frac{1}{4}, y, \frac{1}{4}$	$\frac{3}{4}, \bar{y}, \frac{1}{4}$	$\frac{3}{4}, \bar{y}, \frac{3}{4}$	$\frac{1}{4}, y, \frac{3}{4}$	$hkl : h = 2n$
16 <i>j</i> . . 2	$\frac{1}{4}, \frac{1}{4}, z$	$\frac{3}{4}, \frac{1}{4}, \bar{z}$	$\frac{3}{4}, \frac{3}{4}, \bar{z}$	$\frac{1}{4}, \frac{3}{4}, z$	$hkl : h = 2n$
8 <i>i</i> <i>m m</i> 2	$0, 0, z$	$0, 0, \bar{z}$			no extra conditions
8 <i>h</i> <i>m</i> 2 <i>m</i>	$0, y, 0$	$0, \bar{y}, 0$			no extra conditions
8 <i>g</i> 2 <i>m m</i>	$x, 0, 0$	$\bar{x}, 0, 0$			no extra conditions
8 <i>f</i> 2 2 2	$\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$	$\frac{3}{4}, \frac{3}{4}, \frac{3}{4}$			$hkl : h = 2n$
8 <i>e</i> . . 2/ <i>m</i>	$\frac{1}{4}, \frac{1}{4}, 0$	$\frac{3}{4}, \frac{1}{4}, 0$			$hkl : h = 2n$
8 <i>d</i> . 2/ <i>m</i> .	$\frac{1}{4}, 0, \frac{1}{4}$	$\frac{3}{4}, 0, \frac{1}{4}$			$hkl : h = 2n$
8 <i>c</i> 2/ <i>m</i> . .	$0, \frac{1}{4}, \frac{1}{4}$	$0, \frac{3}{4}, \frac{1}{4}$			$hkl : h = 2n$
4 <i>b</i> <i>m m m</i>	$0, 0, \frac{1}{2}$				no extra conditions
4 <i>a</i> <i>m m m</i>	$0, 0, 0$				no extra conditions

**Symmetry of special projections**

Along [001] *p2mm*  
 $\mathbf{a}' = \frac{1}{2}\mathbf{a}$      $\mathbf{b}' = \frac{1}{2}\mathbf{b}$   
 Origin at 0, 0, z

Along [100] *p2mm*  
 $\mathbf{a}' = \frac{1}{2}\mathbf{b}$      $\mathbf{b}' = \frac{1}{2}\mathbf{c}$   
 Origin at x, 0, 0

Along [010] *p2mm*  
 $\mathbf{a}' = \frac{1}{2}\mathbf{c}$      $\mathbf{b}' = \frac{1}{2}\mathbf{a}$   
 Origin at 0, y, 0

**Maximal non-isomorphic subgroups**

<b>I</b>	[2] <i>F m m 2</i> (42)	(1; 2; 7; 8)+
	[2] <i>F m 2 m</i> ( <i>F m m 2</i> , 42)	(1; 3; 6; 8)+
	[2] <i>F 2 m m</i> ( <i>F m m 2</i> , 42)	(1; 4; 6; 7)+
	[2] <i>F 2 2 2</i> (22)	(1; 2; 3; 4)+
	[2] <i>F 1 1 2/m</i> ( <i>C 2/m</i> , 12)	(1; 2; 5; 6)+
	[2] <i>F 1 2/m 1</i> ( <i>C 2/m</i> , 12)	(1; 3; 5; 7)+
	[2] <i>F 2/m 1 1</i> ( <i>C 2/m</i> , 12)	(1; 4; 5; 8)+
<b>IIa</b>	[2] <i>A e a a</i> ( <i>C c c e</i> , 68)	1; 2; 3; 4; (1; 2; 3; 4) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (5; 6; 7; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (5; 6; 7; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>B b e b</i> ( <i>C c c e</i> , 68)	1; 2; 3; 4; (1; 2; 3; 4) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (5; 6; 7; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (5; 6; 7; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>C c c e</i> (68)	1; 2; 3; 4; (1; 2; 3; 4) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (5; 6; 7; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (5; 6; 7; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>C m m e</i> (67)	1; 2; 7; 8; (1; 2; 7; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (3; 4; 5; 6) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (3; 4; 5; 6) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>B m e m</i> ( <i>C m m e</i> , 67)	1; 3; 6; 8; (1; 3; 6; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 4; 5; 7) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 4; 5; 7) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>A e m m</i> ( <i>C m m e</i> , 67)	1; 4; 6; 7; (1; 4; 6; 7) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 3; 5; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 3; 5; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>C c c m</i> (66)	1; 2; 5; 6; (1; 2; 5; 6) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (3; 4; 7; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (3; 4; 7; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>B b m b</i> ( <i>C c c m</i> , 66)	1; 3; 5; 7; (1; 3; 5; 7) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 4; 6; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 4; 6; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>A m a a</i> ( <i>C c c m</i> , 66)	1; 4; 5; 8; (1; 4; 5; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 3; 6; 7) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 3; 6; 7) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>A m m m</i> ( <i>C m m m</i> , 65)	1; 2; 3; 4; 5; 6; 7; 8; (1; 2; 3; 4; 5; 6; 7; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ )
	[2] <i>B m m m</i> ( <i>C m m m</i> , 65)	1; 2; 3; 4; 5; 6; 7; 8; (1; 2; 3; 4; 5; 6; 7; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>C m m m</i> (65)	1; 2; 3; 4; 5; 6; 7; 8; (1; 2; 3; 4; 5; 6; 7; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>A e a m</i> ( <i>C m c e</i> , 64)	1; 2; 5; 6; (1; 2; 5; 6) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (3; 4; 7; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (3; 4; 7; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>B b e m</i> ( <i>C m c e</i> , 64)	1; 2; 5; 6; (1; 2; 5; 6) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (3; 4; 7; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (3; 4; 7; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>A e m a</i> ( <i>C m c e</i> , 64)	1; 3; 5; 7; (1; 3; 5; 7) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 4; 6; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 4; 6; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>C c m e</i> ( <i>C m c e</i> , 64)	1; 3; 5; 7; (1; 3; 5; 7) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (2; 4; 6; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 4; 6; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>B m e b</i> ( <i>C m c e</i> , 64)	1; 4; 5; 8; (1; 4; 5; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 3; 6; 7) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 3; 6; 7) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>C m c e</i> (64)	1; 4; 5; 8; (1; 4; 5; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (2; 3; 6; 7) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 3; 6; 7) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>A m a m</i> ( <i>C m c m</i> , 63)	1; 3; 6; 8; (1; 3; 6; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 4; 5; 7) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 4; 5; 7) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>A m m a</i> ( <i>C m c m</i> , 63)	1; 2; 7; 8; (1; 2; 7; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (3; 4; 5; 6) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (3; 4; 5; 6) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>B m m b</i> ( <i>C m c m</i> , 63)	1; 2; 7; 8; (1; 2; 7; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (3; 4; 5; 6) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (3; 4; 5; 6) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>B b m m</i> ( <i>C m c m</i> , 63)	1; 4; 6; 7; (1; 4; 6; 7) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ ); (2; 3; 5; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 3; 5; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0)
	[2] <i>C m c m</i> (63)	1; 3; 6; 8; (1; 3; 6; 8) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (2; 4; 5; 7) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 4; 5; 7) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )
	[2] <i>C c m m</i> ( <i>C m c m</i> , 63)	1; 4; 6; 7; (1; 4; 6; 7) + ( $\frac{1}{2}$ , $\frac{1}{2}$ , 0); (2; 3; 5; 8) + (0, $\frac{1}{2}$ , $\frac{1}{2}$ ); (2; 3; 5; 8) + ( $\frac{1}{2}$ , 0, $\frac{1}{2}$ )

**IIb** none

**Maximal isomorphic subgroups of lowest index**

**IIc** [3] *F m m m* ( $\mathbf{a}' = 3\mathbf{a}$  or  $\mathbf{b}' = 3\mathbf{b}$  or  $\mathbf{c}' = 3\mathbf{c}$ ) (69)

**Minimal non-isomorphic supergroups**

**I** [2] *I 4/m m m* (139); [2] *I 4/m c m* (140); [3] *F m 3* (202)

**II** [2] *P m m m* ( $\mathbf{a}' = \frac{1}{2}\mathbf{a}$ ,  $\mathbf{b}' = \frac{1}{2}\mathbf{b}$ ,  $\mathbf{c}' = \frac{1}{2}\mathbf{c}$ ) (47)