

$P4/n$

$C_{4h}^3$

$4/m$

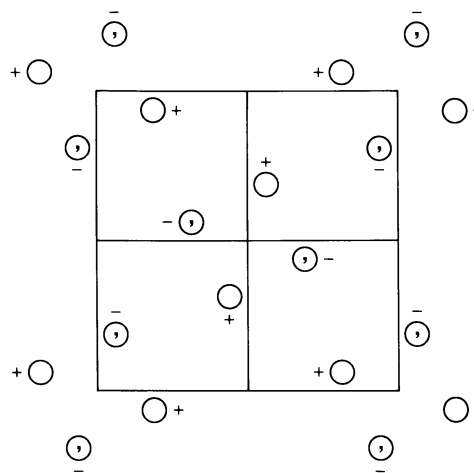
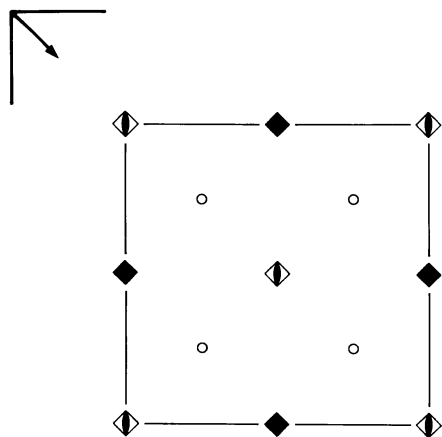
Tetragonal

No. 85

$P4/n$

Patterson symmetry  $P4/m$

ORIGIN CHOICE 1



**Origin** at  $\bar{4}$  on  $n$ , at  $-\frac{1}{4}, \frac{1}{4}, 0$  from  $\bar{1}$

**Asymmetric unit**  $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq \frac{1}{2}$

**Symmetry operations**

- |   |  |                                    |                                    |
|---|--|------------------------------------|------------------------------------|
| (1) 1                                       | (2) $2 \ 0, 0, z$                              | (3) $4^+ \ 0, \frac{1}{2}, z$      | (4) $4^- \ \frac{1}{2}, 0, z$      |
| (5) $\bar{1} \ \frac{1}{4}, \frac{1}{4}, 0$ | (6) $n(\frac{1}{2}, \frac{1}{2}, 0) \ x, y, 0$ | (7) $\bar{4}^+ \ 0, 0, z; 0, 0, 0$ | (8) $\bar{4}^- \ 0, 0, z; 0, 0, 0$ |

**Generators selected** (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ; (2); (3); (5)

**Positions**

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions
					General:
8 <i>g</i> 1	(1) $x, y, z$ (5) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, \bar{z}$	(2) $\bar{x}, \bar{y}, z$ (6) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$	(3) $\bar{y} + \frac{1}{2}, x + \frac{1}{2}, z$ (7) $y, \bar{x}, \bar{z}$	(4) $y + \frac{1}{2}, \bar{x} + \frac{1}{2}, z$ (8) $\bar{y}, x, \bar{z}$	$hk0 : h + k = 2n$ $h00 : h = 2n$
					Special: as above, plus
4 <i>f</i> 2..	0, 0, $z$	$\frac{1}{2}, \frac{1}{2}, z$	$\frac{1}{2}, \frac{1}{2}, \bar{z}$	0, 0, $\bar{z}$	$hkl : h + k = 2n$
4 <i>e</i> $\bar{1}$	$\frac{1}{4}, \frac{1}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{3}{4}, \frac{1}{2}$	$\frac{1}{4}, \frac{3}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{1}{4}, \frac{1}{2}$	$hkl : h, k = 2n$
4 <i>d</i> $\bar{1}$	$\frac{1}{4}, \frac{1}{4}, 0$	$\frac{3}{4}, \frac{3}{4}, 0$	$\frac{1}{4}, \frac{3}{4}, 0$	$\frac{3}{4}, \frac{1}{4}, 0$	$hkl : h, k = 2n$
2 <i>c</i> 4..	0, $\frac{1}{2}, z$	$\frac{1}{2}, 0, \bar{z}$			no extra conditions
2 <i>b</i> $\bar{4}$ ..	0, 0, $\frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$			$hkl : h + k = 2n$
2 <i>a</i> $\bar{4}$ ..	0, 0, 0	$\frac{1}{2}, \frac{1}{2}, 0$			$hkl : h + k = 2n$

**Symmetry of special projections**

Along [001]  $p4$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at 0, 0,  $z$

Along [100]  $p2mg$

$$\mathbf{a}' = \mathbf{b} \quad \mathbf{b}' = \mathbf{c}$$

Origin at  $x, \frac{1}{4}, 0$

Along [110]  $p2mm$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \mathbf{c}$$

Origin at  $x, x, 0$

**Maximal non-isomorphic subgroups**

<b>I</b>	[2] $P\bar{4}$ (81)	1; 2; 7; 8
	[2] $P4$ (75)	1; 2; 3; 4
	[2] $P2/n(P2/c, 13)$	1; 2; 5; 6

**IIa** none

**IIb** [2]  $P4_2/n(c' = 2c)$  (86)

**Maximal isomorphic subgroups of lowest index**

**IIc** [2]  $P4/n(c' = 2c)$  (85); [5]  $P4/n(a' = a + 2b, b' = -2a + b$  or  $a' = a - 2b, b' = 2a + b)$  (85)

**Minimal non-isomorphic supergroups**

**I** [2]  $P4/nbm$  (125); [2]  $P4/nnc$  (126); [2]  $P4/nmm$  (129); [2]  $P4/ncc$  (130)

**II** [2]  $C4/m(P4/m, 83)$ ; [2]  $I4/m$  (87)

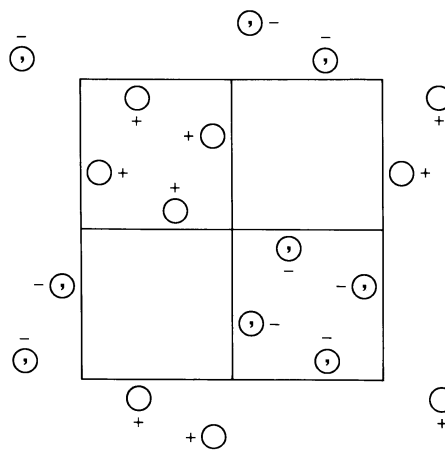
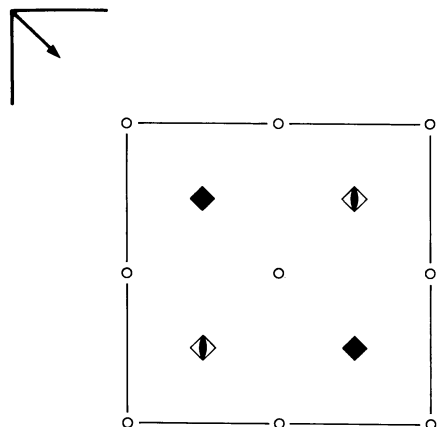
$P4/n$  $C_{4h}^3$  $4/m$ 

Tetragonal

No. 85

 $P4/n$ Patterson symmetry  $P4/m$ 

ORIGIN CHOICE 2



**Origin** at  $\bar{1}$  on  $n$ , at  $\frac{1}{4}, -\frac{1}{4}, 0$  from  $\bar{4}$

**Asymmetric unit**  $-\frac{1}{4} \leq x \leq \frac{1}{4}; -\frac{1}{4} \leq y \leq \frac{1}{4}; 0 \leq z \leq \frac{1}{2}$

**Symmetry operations**

- |                       |  |  |  |
|-----------------------|--|--|--|
| (1) 1                 | (2) $2 \frac{1}{4}, \frac{1}{4}, z$          | (3) $4^+ \frac{1}{4}, \frac{1}{4}, z$                                      | (4) $4^- \frac{1}{4}, \frac{1}{4}, z$                                      |
| (5) $\bar{1} 0, 0, 0$ | (6) $n(\frac{1}{2}, \frac{1}{2}, 0) x, y, 0$ | (7) $\bar{4}^+ \frac{1}{4}, -\frac{1}{4}, z; \frac{1}{4}, -\frac{1}{4}, 0$ | (8) $\bar{4}^- -\frac{1}{4}, \frac{1}{4}, z; -\frac{1}{4}, \frac{1}{4}, 0$ |

**Generators selected** (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ; (2); (3); (5)

**Positions**

Multiplicity, Wyckoff letter, Site symmetry		Coordinates				Reflection conditions
8	<i>g</i> 1	(1) $x, y, z$ (5) $\bar{x}, \bar{y}, \bar{z}$	(2) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$ (6) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$	(3) $\bar{y} + \frac{1}{2}, x, z$ (7) $y + \frac{1}{2}, \bar{x}, \bar{z}$	(4) $y, \bar{x} + \frac{1}{2}, z$ (8) $\bar{y}, x + \frac{1}{2}, \bar{z}$	General: $hk0 : h + k = 2n$ $h00 : h = 2n$  Special: as above, plus $hkl : h + k = 2n$ $hkl : h, k = 2n$ $hkl : h, k = 2n$ no extra conditions $hkl : h + k = 2n$ $hkl : h + k = 2n$
4	<i>f</i> 2..	$\frac{1}{4}, \frac{3}{4}, z$	$\frac{3}{4}, \frac{1}{4}, z$	$\frac{3}{4}, \frac{1}{4}, \bar{z}$	$\frac{1}{4}, \frac{3}{4}, \bar{z}$	
4	<i>e</i> $\bar{1}$	$0, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, 0, \frac{1}{2}$	$0, \frac{1}{2}, \frac{1}{2}$	
4	<i>d</i> $\bar{1}$	$0, 0, 0$	$\frac{1}{2}, \frac{1}{2}, 0$	$\frac{1}{2}, 0, 0$	$0, \frac{1}{2}, 0$	
2	<i>c</i> 4..	$\frac{1}{4}, \frac{1}{4}, z$	$\frac{3}{4}, \frac{3}{4}, \bar{z}$			
2	<i>b</i> $\bar{4}$ ..	$\frac{1}{4}, \frac{3}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{1}{4}, \frac{1}{2}$			
2	<i>a</i> $\bar{4}$ ..	$\frac{1}{4}, \frac{3}{4}, 0$	$\frac{3}{4}, \frac{1}{4}, 0$			

**Symmetry of special projections**

Along [001]  $p4$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at  $\frac{1}{4}, \frac{1}{4}, z$

Along [100]  $p2mg$

$$\mathbf{a}' = \mathbf{b} \quad \mathbf{b}' = \mathbf{c}$$

Origin at  $x, 0, 0$

Along [110]  $p2mm$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \mathbf{c}$$

Origin at  $x, x, 0$

**Maximal non-isomorphic subgroups**

<b>I</b>	[2] $P\bar{4}$ (81)	1; 2; 7; 8
	[2] $P4$ (75)	1; 2; 3; 4
	[2] $P2/n$ ( $P2/c$ , 13)	1; 2; 5; 6

**IIa** none

**IIb** [2]  $P4_2/n$  ( $\mathbf{c}' = 2\mathbf{c}$ ) (86)

**Maximal isomorphic subgroups of lowest index**

**IIc** [2]  $P4/n$  ( $\mathbf{c}' = 2\mathbf{c}$ ) (85); [5]  $P4/n$  ( $\mathbf{a}' = \mathbf{a} + 2\mathbf{b}, \mathbf{b}' = -2\mathbf{a} + \mathbf{b}$  or  $\mathbf{a}' = \mathbf{a} - 2\mathbf{b}, \mathbf{b}' = 2\mathbf{a} + \mathbf{b}$ ) (85)

**Minimal non-isomorphic supergroups**

**I** [2]  $P4/nbm$  (125); [2]  $P4/nnc$  (126); [2]  $P4/nmm$  (129); [2]  $P4/ncc$  (130)

**II** [2]  $C4/m$  ( $P4/m$ , 83); [2]  $I4/m$  (87)