

$I4cm$

C_{4v}^{10}

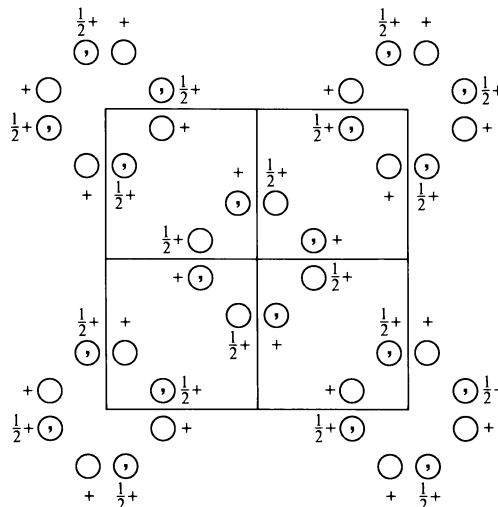
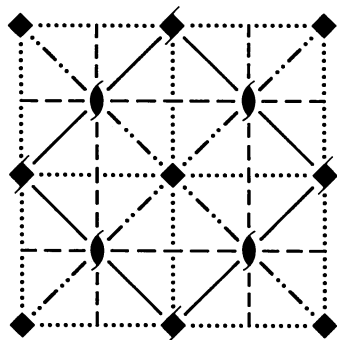
$4mm$

Tetragonal

No. 108

$I4cm$

Patterson symmetry $I4/mmm$



Origin on $4c$

Asymmetric unit $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq \frac{1}{2}; y \leq \frac{1}{2} - x$

Symmetry operations

For $(0,0,0)+$ set

- | | | | |
|----------------|----------------|----------------------|-----------------|
| (1) 1 | (2) $2\ 0,0,z$ | (3) $4^+ 0,0,z$ | (4) $4^- 0,0,z$ |
| (5) $c\ x,0,z$ | (6) $c\ 0,y,z$ | (7) $c\ x,\bar{x},z$ | (8) $c\ x,x,z$ |

For $(\frac{1}{2},\frac{1}{2},\frac{1}{2})+$ set

- | | | | |
|--|---|---|---|
| (1) $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$ | (2) $2(0,0,\frac{1}{2})\ \frac{1}{4},\frac{1}{4},z$ | (3) $4^+(0,0,\frac{1}{2})\ 0,\frac{1}{2},z$ | (4) $4^-(0,0,\frac{1}{2})\ \frac{1}{2},0,z$ |
| (5) $a\ x,\frac{1}{4},z$ | (6) $b\ \frac{1}{4},y,z$ | (7) $m\ x+\frac{1}{2},\bar{x},z$ | (8) $g(\frac{1}{2},\frac{1}{2},0)\ x,x,z$ |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$; (2); (3); (5)

Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions
	(0,0,0) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$ +				General:
16 <i>d</i> 1	(1) x,y,z (5) $x,\bar{y},z+\frac{1}{2}$	(2) \bar{x},\bar{y},z (6) $\bar{x},y,z+\frac{1}{2}$	(3) \bar{y},x,z (7) $\bar{y},\bar{x},z+\frac{1}{2}$	(4) y,\bar{x},z (8) $y,x,z+\frac{1}{2}$	$hkl : h+k+l=2n$ $hk0 : h+k=2n$ $0kl : k,l=2n$ $hhl : l=2n$ $00l : l=2n$ $h00 : h=2n$
8 <i>c</i> . . <i>m</i>	$x,x+\frac{1}{2},z$	$\bar{x},\bar{x}+\frac{1}{2},z$	$\bar{x}+\frac{1}{2},x,z$	$x+\frac{1}{2},\bar{x},z$	Special: as above, plus no extra conditions
4 <i>b</i> 2 . <i>mm</i>	$\frac{1}{2},0,z$	$0,\frac{1}{2},z$			$hkl : l=2n$
4 <i>a</i> 4 . .	$0,0,z$	$0,0,z+\frac{1}{2}$			$hkl : l=2n$

Symmetry of special projections

Along [001] $p4mm$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at 0,0,z

Along [100] $p1m1$

$$\mathbf{a}' = \frac{1}{2}\mathbf{b} \quad \mathbf{b}' = \frac{1}{2}\mathbf{c}$$

Origin at x,0,0

Along [110] $p1m1$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}\mathbf{c}$$

Origin at x,x,0

Maximal non-isomorphic subgroups

I	[2] $I411$ ($I4, 79$)	(1; 2; 3; 4)+
	[2] $I2c1$ ($Iba2, 45$)	(1; 2; 5; 6)+
	[2] $I21m$ ($Fmm2, 42$)	(1; 2; 7; 8)+
IIa	[2] $P4_2bc$ (106)	1; 2; 7; 8; (3; 4; 5; 6) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$
	[2] $P4cc$ (103)	1; 2; 3; 4; 5; 6; 7; 8
	[2] $P4_2cm$ (101)	1; 2; 5; 6; (3; 4; 7; 8) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$
	[2] $P4bm$ (100)	1; 2; 3; 4; (5; 6; 7; 8) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$
IIb	none	

Maximal isomorphic subgroups of lowest index

IIc [3] $I4cm$ ($\mathbf{c}' = 3\mathbf{c}$) (108); [9] $I4cm$ ($\mathbf{a}' = 3\mathbf{a}, \mathbf{b}' = 3\mathbf{b}$) (108)

Minimal non-isomorphic supergroups

I	[2] $I4/mcm$ (140)
II	[2] $C4mm$ ($\mathbf{c}' = \frac{1}{2}\mathbf{c}$) ($P4mm, 99$)