

$I\bar{4}2m$

D_{2d}^{11}

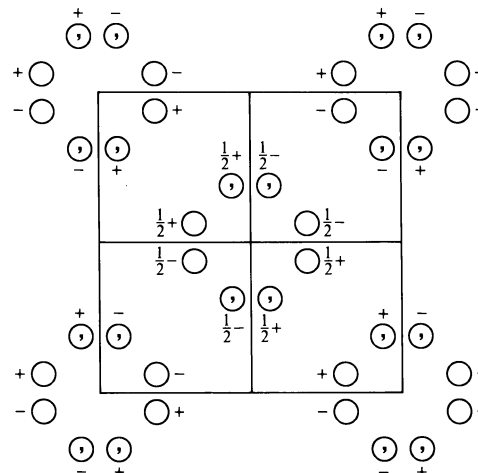
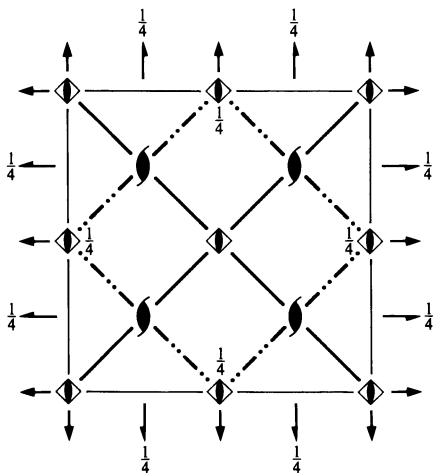
$\bar{4}2m$

Tetragonal

No. 121

$I\bar{4}2m$

Patterson symmetry $I4/mmm$



Origin at $\bar{4}2m$

Asymmetric unit $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq \frac{1}{2}; x \leq y$

Symmetry operations

For $(0,0,0)^+$ set

- | | | | |
|---------------|---------------|--------------------------------|--------------------------------|
| (1) 1 | (2) 2 $0,0,z$ | (3) $\bar{4}^+$ $0,0,z; 0,0,0$ | (4) $\bar{4}^-$ $0,0,z; 0,0,0$ |
| (5) 2 $0,y,0$ | (6) 2 $x,0,0$ | (7) m x,\bar{x},z | (8) m x,x,z |

For $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})^+$ set

- | | | | |
|---|---|--|--|
| (1) $t(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ | (2) 2 $(0,0, \frac{1}{2})$ $\frac{1}{4}, \frac{1}{4}, z$ | (3) $\bar{4}^+$ $\frac{1}{2}, 0, z; \frac{1}{2}, 0, \frac{1}{4}$ | (4) $\bar{4}^-$ $0, \frac{1}{2}, z; 0, \frac{1}{2}, \frac{1}{4}$ |
| (5) 2 $(0, \frac{1}{2}, 0)$ $\frac{1}{4}, y, \frac{1}{4}$ | (6) 2 $(\frac{1}{2}, 0, 0)$ $x, \frac{1}{4}, \frac{1}{4}$ | (7) c $x + \frac{1}{2}, \bar{x}, z$ | (8) $n(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ x, x, z |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$; (2); (3); (5)

Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions
	$(0,0,0)+ (\frac{1}{2},\frac{1}{2},\frac{1}{2})+$				General:
16 <i>j</i> 1	(1) x,y,z (5) \bar{x},y,\bar{z}	(2) \bar{x},\bar{y},z (6) x,\bar{y},\bar{z}	(3) y,\bar{x},\bar{z} (7) \bar{y},\bar{x},z	(4) \bar{y},x,\bar{z} (8) y,x,z	$hkl : h+k+l=2n$ $hk0 : h+k=2n$ $0kl : k+l=2n$ $hhl : l=2n$ $00l : l=2n$ $h00 : h=2n$
8 <i>i</i> . . <i>m</i>	x,x,z	\bar{x},\bar{x},z	x,\bar{x},\bar{z}	\bar{x},x,\bar{z}	Special: as above, plus no extra conditions
8 <i>h</i> 2 . .	$0,\frac{1}{2},z$	$\frac{1}{2},0,\bar{z}$	$0,\frac{1}{2},\bar{z}$	$\frac{1}{2},0,z$	$hkl : l=2n$
8 <i>g</i> . 2 .	$x,0,\frac{1}{2}$	$\bar{x},0,\frac{1}{2}$	$0,\bar{x},\frac{1}{2}$	$0,x,\frac{1}{2}$	no extra conditions
8 <i>f</i> . 2 .	$x,0,0$	$\bar{x},0,0$	$0,\bar{x},0$	$0,x,0$	no extra conditions
4 <i>e</i> 2 . <i>mm</i>	$0,0,z$	$0,0,\bar{z}$			no extra conditions
4 <i>d</i> $\bar{4}$. .	$0,\frac{1}{2},\frac{1}{4}$	$0,\frac{1}{2},\frac{3}{4}$			$hkl : l=2n$
4 <i>c</i> 2 2 2 .	$0,\frac{1}{2},0$	$\frac{1}{2},0,0$			$hkl : l=2n$
2 <i>b</i> $\bar{4}2m$	$0,0,\frac{1}{2}$				no extra conditions
2 <i>a</i> $\bar{4}2m$	$0,0,0$				no extra conditions

Symmetry of special projectionsAlong [001] $p4mm$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at $0,0,z$ Along [100] $c2mm$

$$\mathbf{a}' = \mathbf{b} \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x,0,0$ Along [110] $p1m1$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}\mathbf{c}$$

Origin at $x,x,0$ **Maximal non-isomorphic subgroups**

I	[2] $I\bar{4}11$ ($I\bar{4}$, 82)	(1; 2; 3; 4)+
	[2] $I21m$ ($Fmm2$, 42)	(1; 2; 7; 8)+
	[2] $I221$ ($I222$, 23)	(1; 2; 5; 6)+
IIa	[2] $P\bar{4}2_1c$ (114)	1; 2; 3; 4; (5; 6; 7; 8) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$
	[2] $P\bar{4}2_1m$ (113)	1; 2; 7; 8; (3; 4; 5; 6) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$
	[2] $P\bar{4}2c$ (112)	1; 2; 5; 6; (3; 4; 7; 8) + $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$
	[2] $P\bar{4}2m$ (111)	1; 2; 3; 4; 5; 6; 7; 8
IIb	none	

Maximal isomorphic subgroups of lowest index**IIc** [3] $I\bar{4}2m$ ($\mathbf{c}' = 3\mathbf{c}$) (121); [9] $I\bar{4}2m$ ($\mathbf{a}' = 3\mathbf{a}, \mathbf{b}' = 3\mathbf{b}$) (121)**Minimal non-isomorphic supergroups**

I	[2] $I4/mmm$ (139); [2] $I4/mcm$ (140); [3] $I\bar{4}3m$ (217)
II	[2] $C\bar{4}2m$ ($\mathbf{c}' = \frac{1}{2}\mathbf{c}$) ($P\bar{4}m2$, 115)