

$P4/nbm$

D_{4h}^3

$4/mmm$

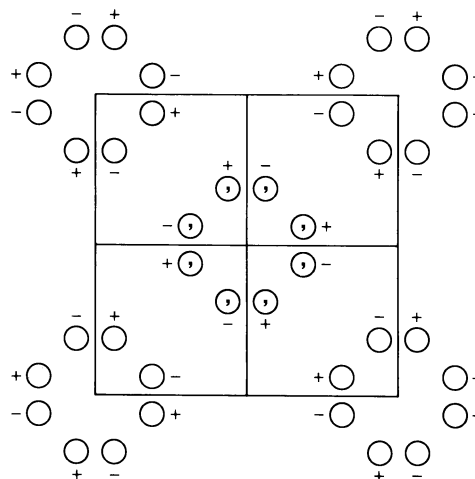
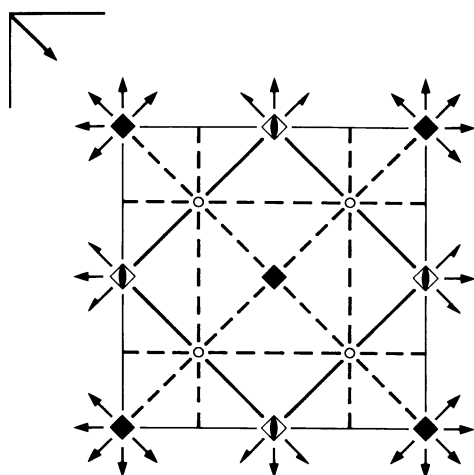
Tetragonal

No. 125

$P 4/n 2/b 2/m$

Patterson symmetry $P4/mmm$

ORIGIN CHOICE 1



Origin at 422 at $4/n22/g$, at $-\frac{1}{4}, -\frac{1}{4}, 0$ from centre ($2/m$)

Asymmetric unit $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq \frac{1}{2}; y \leq \frac{1}{2} - x$

Symmetry operations

- | | | | |
|---------------------------------------------|-------------------------------------------------|---------------------------------------------------------|---------------------------------------------------------|
| (1) 1 | (2) 2 $0, 0, z$ | (3) 4^+ $0, 0, z$ | (4) 4^- $0, 0, z$ |
| (5) 2 $0, y, 0$ | (6) 2 $x, 0, 0$ | (7) 2 $x, x, 0$ | (8) 2 $x, \bar{x}, 0$ |
| (9) $\bar{1}$ $\frac{1}{4}, \frac{1}{4}, 0$ | (10) $n(\frac{1}{2}, \frac{1}{2}, 0)$ $x, y, 0$ | (11) $\bar{4}^+$ $\frac{1}{2}, 0, z; \frac{1}{2}, 0, 0$ | (12) $\bar{4}^-$ $0, \frac{1}{2}, z; 0, \frac{1}{2}, 0$ |
| (13) a $x, \frac{1}{4}, z$ | (14) b $\frac{1}{4}, y, z$ | (15) m $x + \frac{1}{2}, \bar{x}, z$ | (16) $g(\frac{1}{2}, \frac{1}{2}, 0)$ x, x, z |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5); (9)

Positions

Multiplicity, Wyckoff letter, Site symmetry		Coordinates				Reflection conditions
						General:
16	<i>n</i> 1	(1) x, y, z (5) \bar{x}, y, \bar{z} (9) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, \bar{z}$ (13) $x + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$	(2) \bar{x}, \bar{y}, z (6) x, \bar{y}, \bar{z} (10) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$ (14) $\bar{x} + \frac{1}{2}, y + \frac{1}{2}, z$	(3) \bar{y}, x, z (7) y, x, \bar{z} (11) $y + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z}$ (15) $\bar{y} + \frac{1}{2}, \bar{x} + \frac{1}{2}, z$	(4) y, \bar{x}, z (8) $\bar{y}, \bar{x}, \bar{z}$ (12) $\bar{y} + \frac{1}{2}, x + \frac{1}{2}, \bar{z}$ (16) $y + \frac{1}{2}, x + \frac{1}{2}, z$	$hk0: h + k = 2n$ $0kl: k = 2n$ $h00: h = 2n$
8	<i>m</i> .. <i>m</i>	$x, x + \frac{1}{2}, z$ $\bar{x}, x + \frac{1}{2}, \bar{z}$	$\bar{x}, \bar{x} + \frac{1}{2}, z$ $x, \bar{x} + \frac{1}{2}, \bar{z}$	$\bar{x} + \frac{1}{2}, x, z$ $x + \frac{1}{2}, x, \bar{z}$	$x + \frac{1}{2}, \bar{x}, z$ $\bar{x} + \frac{1}{2}, \bar{x}, \bar{z}$	Special: as above, plus no extra conditions
8	<i>l</i> . 2 .	$x, 0, \frac{1}{2}$ $\bar{x} + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	$\bar{x}, 0, \frac{1}{2}$ $x + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	$0, x, \frac{1}{2}$ $\frac{1}{2}, \bar{x} + \frac{1}{2}, \frac{1}{2}$	$0, \bar{x}, \frac{1}{2}$ $\frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}$	$hkl: h + k = 2n$
8	<i>k</i> . 2 .	$x, 0, 0$ $\bar{x} + \frac{1}{2}, \frac{1}{2}, 0$	$\bar{x}, 0, 0$ $x + \frac{1}{2}, \frac{1}{2}, 0$	$0, x, 0$ $\frac{1}{2}, \bar{x} + \frac{1}{2}, 0$	$0, \bar{x}, 0$ $\frac{1}{2}, x + \frac{1}{2}, 0$	$hkl: h + k = 2n$
8	<i>j</i> .. 2	$x, x, \frac{1}{2}$ $\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, \frac{1}{2}$	$\bar{x}, \bar{x}, \frac{1}{2}$ $x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}$	$\bar{x}, x, \frac{1}{2}$ $x + \frac{1}{2}, \bar{x} + \frac{1}{2}, \frac{1}{2}$	$x, \bar{x}, \frac{1}{2}$ $\bar{x} + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}$	$hkl: h + k = 2n$
8	<i>i</i> .. 2	$x, x, 0$ $\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, 0$	$\bar{x}, \bar{x}, 0$ $x + \frac{1}{2}, x + \frac{1}{2}, 0$	$\bar{x}, x, 0$ $x + \frac{1}{2}, \bar{x} + \frac{1}{2}, 0$	$x, \bar{x}, 0$ $\bar{x} + \frac{1}{2}, x + \frac{1}{2}, 0$	$hkl: h + k = 2n$
4	<i>h</i> 2 . <i>mm</i>	$0, \frac{1}{2}, z$	$\frac{1}{2}, 0, z$	$0, \frac{1}{2}, \bar{z}$	$\frac{1}{2}, 0, \bar{z}$	$hkl: h + k = 2n$
4	<i>g</i> 4 ..	$0, 0, z$	$0, 0, \bar{z}$	$\frac{1}{2}, \frac{1}{2}, \bar{z}$	$\frac{1}{2}, \frac{1}{2}, z$	$hkl: h + k = 2n$
4	<i>f</i> .. 2/ <i>m</i>	$\frac{1}{4}, \frac{1}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{3}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{1}{4}, \frac{1}{2}$	$\frac{1}{4}, \frac{3}{4}, \frac{1}{2}$	$hkl: h, k = 2n$
4	<i>e</i> .. 2/ <i>m</i>	$\frac{1}{4}, \frac{1}{4}, 0$	$\frac{3}{4}, \frac{3}{4}, 0$	$\frac{3}{4}, \frac{1}{4}, 0$	$\frac{1}{4}, \frac{3}{4}, 0$	$hkl: h, k = 2n$
2	<i>d</i> $\bar{4}2m$	$0, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, 0, \frac{1}{2}$			$hkl: h + k = 2n$
2	<i>c</i> $\bar{4}2m$	$0, \frac{1}{2}, 0$	$\frac{1}{2}, 0, 0$			$hkl: h + k = 2n$
2	<i>b</i> 4 2 2	$0, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$			$hkl: h + k = 2n$
2	<i>a</i> 4 2 2	$0, 0, 0$	$\frac{1}{2}, \frac{1}{2}, 0$			$hkl: h + k = 2n$

Symmetry of special projections

Along [001] $p4mm$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at 0, 0, z

Along [100] $p2mm$

$$\mathbf{a}' = \frac{1}{2}\mathbf{b} \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x, 0, 0$

Along [110] $p2mm$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x, x, 0$

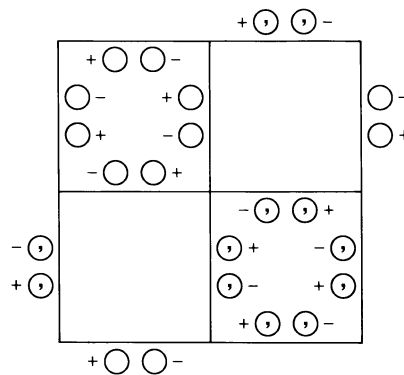
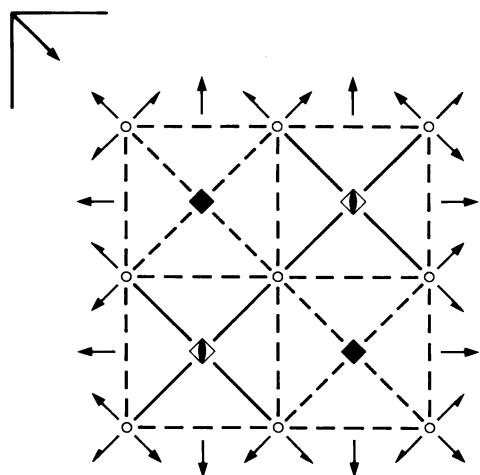
$P4/nbm$ D_{4h}^3 $4/mmm$

Tetragonal

No. 125

 $P 4/n 2/b 2/m$ Patterson symmetry $P4/mmm$

ORIGIN CHOICE 2



Origin at centre ($2/m$) at $n(b,a)(2_1/g,2/m)$, at $\frac{1}{4}, \frac{1}{4}, 0$ from 422

Asymmetric unit $-\frac{1}{4} \leq x \leq \frac{1}{4}; -\frac{1}{4} \leq y \leq \frac{1}{4}; 0 \leq z \leq \frac{1}{2}; x \leq -y$

Symmetry operations

- | | | | |
|---------------------------|-------------------------------------------------|-------------------------------------------------------------------------------|-------------------------------------------------------------------------------|
| (1) 1 | (2) 2 $\frac{1}{4}, \frac{1}{4}, z$ | (3) 4^+ $\frac{1}{4}, \frac{1}{4}, z$ | (4) 4^- $\frac{1}{4}, \frac{1}{4}, z$ |
| (5) 2 $\frac{1}{4}, y, 0$ | (6) 2 $x, \frac{1}{4}, 0$ | (7) 2 $x, x, 0$ | (8) 2 $x, \bar{x} + \frac{1}{2}, 0$ |
| (9) $\bar{1}$ $0, 0, 0$ | (10) $n(\frac{1}{2}, \frac{1}{2}, 0)$ $x, y, 0$ | (11) $\bar{4}^+$ $\frac{1}{4}, -\frac{1}{4}, z; \frac{1}{4}, -\frac{1}{4}, 0$ | (12) $\bar{4}^-$ $-\frac{1}{4}, \frac{1}{4}, z; -\frac{1}{4}, \frac{1}{4}, 0$ |
| (13) a $x, 0, z$ | (14) b $0, y, z$ | (15) m x, \bar{x}, z | (16) $g(\frac{1}{2}, \frac{1}{2}, 0)$ x, x, z |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5); (9)

Positions

Multiplicity, Wyckoff letter, Site symmetry		Coordinates				Reflection conditions
General:						
16	<i>n</i> 1	(1) x, y, z (5) $\bar{x} + \frac{1}{2}, y, \bar{z}$ (9) $\bar{x}, \bar{y}, \bar{z}$ (13) $x + \frac{1}{2}, \bar{y}, z$	(2) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$ (6) $x, \bar{y} + \frac{1}{2}, \bar{z}$ (10) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$ (14) $\bar{x}, y + \frac{1}{2}, z$	(3) $\bar{y} + \frac{1}{2}, x, z$ (7) y, x, \bar{z} (11) $y + \frac{1}{2}, \bar{x}, \bar{z}$ (15) \bar{y}, \bar{x}, z	(4) $y, \bar{x} + \frac{1}{2}, z$ (8) $\bar{y} + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z}$ (12) $\bar{y}, x + \frac{1}{2}, \bar{z}$ (16) $y + \frac{1}{2}, x + \frac{1}{2}, z$	$hk0: h+k=2n$ $0kl: k=2n$ $h00: h=2n$
Special: as above, plus						
8	<i>m</i> .. <i>m</i>	x, \bar{x}, z $\bar{x} + \frac{1}{2}, \bar{x}, \bar{z}$	$\bar{x} + \frac{1}{2}, x + \frac{1}{2}, z$ $x, x + \frac{1}{2}, \bar{z}$	$x + \frac{1}{2}, x, z$ \bar{x}, x, \bar{z}	$\bar{x}, \bar{x} + \frac{1}{2}, z$ $x + \frac{1}{2}, \bar{x} + \frac{1}{2}, \bar{z}$	no extra conditions
8	<i>l</i> .2.	$x, \frac{1}{4}, \frac{1}{2}$ $\bar{x}, \frac{3}{4}, \frac{1}{2}$	$\bar{x} + \frac{1}{2}, \frac{1}{4}, \frac{1}{2}$ $x + \frac{1}{2}, \frac{3}{4}, \frac{1}{2}$	$\frac{1}{4}, x, \frac{1}{2}$ $\frac{3}{4}, \bar{x}, \frac{1}{2}$	$\frac{1}{4}, \bar{x} + \frac{1}{2}, \frac{1}{2}$ $\frac{3}{4}, x + \frac{1}{2}, \frac{1}{2}$	$hkl: h+k=2n$
8	<i>k</i> .2.	$x, \frac{1}{4}, 0$ $\bar{x}, \frac{3}{4}, 0$	$\bar{x} + \frac{1}{2}, \frac{1}{4}, 0$ $x + \frac{1}{2}, \frac{3}{4}, 0$	$\frac{1}{4}, x, 0$ $\frac{3}{4}, \bar{x}, 0$	$\frac{1}{4}, \bar{x} + \frac{1}{2}, 0$ $\frac{3}{4}, x + \frac{1}{2}, 0$	$hkl: h+k=2n$
8	<i>j</i> ..2	$x, x, \frac{1}{2}$ $\bar{x}, \bar{x}, \frac{1}{2}$	$\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, \frac{1}{2}$ $x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}$	$\bar{x} + \frac{1}{2}, x, \frac{1}{2}$ $x + \frac{1}{2}, \bar{x}, \frac{1}{2}$	$x, \bar{x} + \frac{1}{2}, \frac{1}{2}$ $\bar{x}, x + \frac{1}{2}, \frac{1}{2}$	$hkl: h+k=2n$
8	<i>i</i> ..2	$x, x, 0$ $\bar{x}, \bar{x}, 0$	$\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, 0$ $x + \frac{1}{2}, x + \frac{1}{2}, 0$	$\bar{x} + \frac{1}{2}, x, 0$ $x + \frac{1}{2}, \bar{x}, 0$	$x, \bar{x} + \frac{1}{2}, 0$ $\bar{x}, x + \frac{1}{2}, 0$	$hkl: h+k=2n$
4	<i>h</i> 2. <i>mm</i>	$\frac{3}{4}, \frac{1}{4}, z$	$\frac{1}{4}, \frac{3}{4}, z$	$\frac{3}{4}, \frac{1}{4}, \bar{z}$	$\frac{1}{4}, \frac{3}{4}, \bar{z}$	$hkl: h+k=2n$
4	<i>g</i> 4..	$\frac{1}{4}, \frac{1}{4}, z$	$\frac{1}{4}, \frac{1}{4}, \bar{z}$	$\frac{3}{4}, \frac{3}{4}, \bar{z}$	$\frac{3}{4}, \frac{3}{4}, z$	$hkl: h+k=2n$
4	<i>f</i> ..2/ <i>m</i>	$0, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, 0, \frac{1}{2}$	$0, \frac{1}{2}, \frac{1}{2}$	$hkl: h, k=2n$
4	<i>e</i> ..2/ <i>m</i>	$0, 0, 0$	$\frac{1}{2}, \frac{1}{2}, 0$	$\frac{1}{2}, 0, 0$	$0, \frac{1}{2}, 0$	$hkl: h, k=2n$
2	<i>d</i> $\bar{4}2m$	$\frac{3}{4}, \frac{1}{4}, \frac{1}{2}$	$\frac{1}{4}, \frac{3}{4}, \frac{1}{2}$			$hkl: h+k=2n$
2	<i>c</i> $\bar{4}2m$	$\frac{3}{4}, \frac{1}{4}, 0$	$\frac{1}{4}, \frac{3}{4}, 0$			$hkl: h+k=2n$
2	<i>b</i> 422	$\frac{1}{4}, \frac{1}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{3}{4}, \frac{1}{2}$			$hkl: h+k=2n$
2	<i>a</i> 422	$\frac{1}{4}, \frac{1}{4}, 0$	$\frac{3}{4}, \frac{3}{4}, 0$			$hkl: h+k=2n$

Symmetry of special projectionsAlong [001] $p4mm$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at $\frac{1}{4}, \frac{1}{4}, z$ Along [100] $p2mm$

$$\mathbf{a}' = \frac{1}{2}\mathbf{b} \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x, 0, 0$ Along [110] $p2mm$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x, x, 0$