

$P4_232$

$O^2$

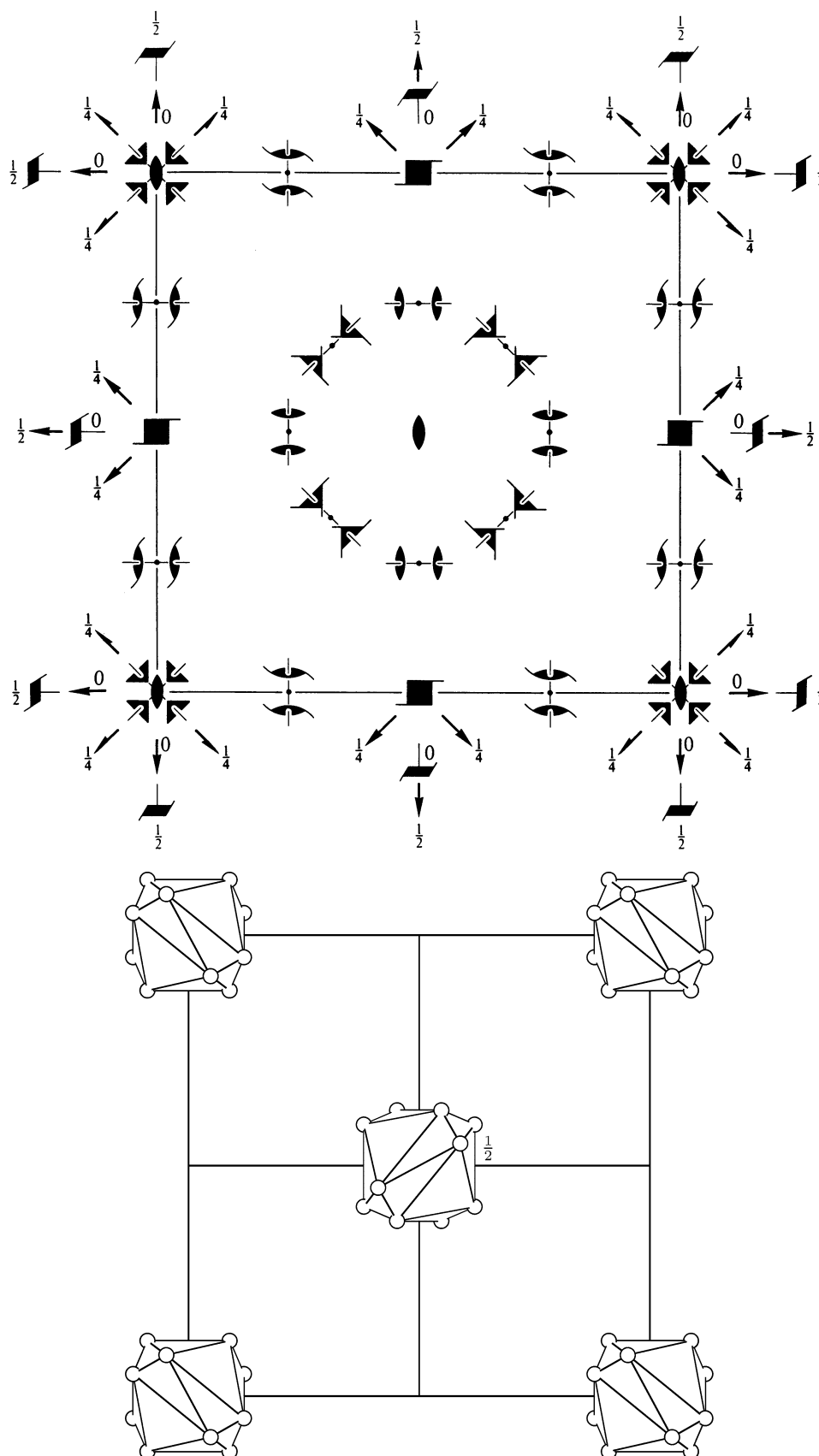
432

Cubic

No. 208

$P4_232$

Patterson symmetry  $Pm\bar{3}m$



Origin at 23

Asymmetric unit  $0 \leq x \leq \frac{1}{2}$ ;  $0 \leq y \leq \frac{1}{2}$ ;  $-\frac{1}{4} \leq z \leq \frac{1}{4}$ ;  $\max(-x, x - \frac{1}{2}, -y, y - \frac{1}{2}) \leq z \leq \min(x, \frac{1}{2} - x, y, \frac{1}{2} - y)$   
 Vertices  $0, 0, 0$   $\frac{1}{2}, 0, 0$   $\frac{1}{2}, \frac{1}{2}, 0$   $0, \frac{1}{2}, 0$   $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$   $\frac{1}{4}, \frac{1}{4}, -\frac{1}{4}$

## Symmetry operations

(1) 1	(2) 2 0,0,z	(3) 2 0,y,0	(4) 2 x,0,0
(5) 3 <sup>+</sup> x,x,x	(6) 3 <sup>+</sup> $\bar{x},x,\bar{x}$	(7) 3 <sup>+</sup> x, $\bar{x},\bar{x}$	(8) 3 <sup>+</sup> $\bar{x},\bar{x},x$
(9) 3 <sup>-</sup> x,x,x	(10) 3 <sup>-</sup> x, $\bar{x},\bar{x}$	(11) 3 <sup>-</sup> $\bar{x},\bar{x},x$	(12) 3 <sup>-</sup> $\bar{x},x,\bar{x}$
(13) 2( $\frac{1}{2},\frac{1}{2},0$ ) x,x, $\frac{1}{4}$	(14) 2 x, $\bar{x}+\frac{1}{2},\frac{1}{4}$	(15) 4 <sup>-</sup> (0,0, $\frac{1}{2}$ ) $\frac{1}{2},0,z$	(16) 4 <sup>+</sup> (0,0, $\frac{1}{2}$ ) 0, $\frac{1}{2},z$
(17) 4 <sup>-</sup> ( $\frac{1}{2},0,0$ ) x, $\frac{1}{2},0$	(18) 2(0, $\frac{1}{2},\frac{1}{2}$ ) $\frac{1}{4},y,y$	(19) 2 $\frac{1}{4},y+\frac{1}{2},\bar{y}$	(20) 4 <sup>+</sup> ( $\frac{1}{2},0,0$ ) x,0, $\frac{1}{2}$
(21) 4 <sup>+</sup> (0, $\frac{1}{2},0$ ) $\frac{1}{2},y,0$	(22) 2( $\frac{1}{2},0,\frac{1}{2}$ ) x, $\frac{1}{4},x$	(23) 4 <sup>-</sup> (0, $\frac{1}{2},0$ ) 0,y, $\frac{1}{2}$	(24) 2 $\bar{x}+\frac{1}{2},\frac{1}{4},x$

Generators selected (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ; (2); (3); (5); (13)

## Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates	Reflection conditions					
24 m 1	(1) x,y,z (5) z,x,y (9) y,z,x (13) $y+\frac{1}{2},x+\frac{1}{2},\bar{z}+\frac{1}{2}$ (17) $x+\frac{1}{2},z+\frac{1}{2},\bar{y}+\frac{1}{2}$ (21) $z+\frac{1}{2},y+\frac{1}{2},\bar{x}+\frac{1}{2}$	(2) $\bar{x},\bar{y},z$ (6) z, $\bar{x},\bar{y}$ (10) $\bar{y},z,\bar{x}$ (14) $\bar{y}+\frac{1}{2},\bar{x}+\frac{1}{2},\bar{z}+\frac{1}{2}$ (18) $\bar{x}+\frac{1}{2},z+\frac{1}{2},y+\frac{1}{2}$ (22) $z+\frac{1}{2},\bar{y}+\frac{1}{2},x+\frac{1}{2}$	(3) $\bar{x},y,\bar{z}$ (7) $\bar{z},\bar{x},y$ (11) y, $\bar{z},\bar{x}$ (15) $y+\frac{1}{2},\bar{x}+\frac{1}{2},z+\frac{1}{2}$ (19) $\bar{x}+\frac{1}{2},\bar{z}+\frac{1}{2},\bar{y}+\frac{1}{2}$ (23) $\bar{z}+\frac{1}{2},y+\frac{1}{2},x+\frac{1}{2}$	(4) x, $\bar{y},\bar{z}$ (8) $\bar{z},x,\bar{y}$ (12) $\bar{y},\bar{z},x$ (16) $\bar{y}+\frac{1}{2},x+\frac{1}{2},z+\frac{1}{2}$ (20) $x+\frac{1}{2},\bar{z}+\frac{1}{2},y+\frac{1}{2}$ (24) $\bar{z}+\frac{1}{2},\bar{y}+\frac{1}{2},\bar{x}+\frac{1}{2}$	h00: $h = 2n$		
12 l ..2	$\frac{1}{4},y,y+\frac{1}{2}$ $y+\frac{1}{2},\frac{3}{4},y$ $y,y+\frac{1}{2},\frac{1}{4}$	$\frac{3}{4},\bar{y},y+\frac{1}{2}$ $y+\frac{1}{2},\frac{3}{4},\bar{y}$ $\bar{y},y+\frac{1}{2},\frac{3}{4}$	$\frac{3}{4},y,\bar{y}+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{3}{4},y$ $y,\bar{y}+\frac{1}{2},\frac{3}{4}$	$\frac{1}{4},\bar{y},\bar{y}+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{1}{4},\bar{y}$ $\bar{y},\bar{y}+\frac{1}{2},\frac{1}{4}$	no extra conditions		
12 k ..2	$\frac{1}{4},y,\bar{y}+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{3}{4},y$ $y,\bar{y}+\frac{1}{2},\frac{3}{4}$	$\frac{3}{4},\bar{y},\bar{y}+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{3}{4},\bar{y}$ $\bar{y},\bar{y}+\frac{1}{2},\frac{3}{4}$	$\frac{3}{4},y,y+\frac{1}{2}$ $y+\frac{1}{2},\frac{3}{4},y$ $y,y+\frac{1}{2},\frac{3}{4}$	$\frac{1}{4},\bar{y},y+\frac{1}{2}$ $y+\frac{1}{2},\frac{1}{4},\bar{y}$ $\bar{y},y+\frac{1}{2},\frac{1}{4}$	no extra conditions		
12 j 2..	$x,\frac{1}{2},0$ $0,x+\frac{1}{2},\frac{1}{2}$	$\bar{x},\frac{1}{2},0$ $0,\bar{x}+\frac{1}{2},\frac{1}{2}$	$0,x,\frac{1}{2}$ $x+\frac{1}{2},\frac{1}{2},0$	$0,\bar{x},\frac{1}{2}$ $\bar{x}+\frac{1}{2},\frac{1}{2},0$	$\frac{1}{2},0,x$ $\frac{1}{2},0,\bar{x}+\frac{1}{2}$	$\frac{1}{2},0,\bar{x}$ $\frac{1}{2},0,x+\frac{1}{2}$	hkl: $h = 2n$ hhl: $l = 2n$
12 i 2..	$x,0,\frac{1}{2}$ $\frac{1}{2},x+\frac{1}{2},0$	$\bar{x},0,\frac{1}{2}$ $\frac{1}{2},\bar{x}+\frac{1}{2},0$	$\frac{1}{2},x,0$ $x+\frac{1}{2},0,\frac{1}{2}$	$\frac{1}{2},\bar{x},0$ $\bar{x}+\frac{1}{2},0,\frac{1}{2}$	$0,\frac{1}{2},x$ $0,\frac{1}{2},\bar{x}+\frac{1}{2}$	$0,\frac{1}{2},\bar{x}$ $0,\frac{1}{2},x+\frac{1}{2}$	hkl: $h = 2n$ hhl: $l = 2n$
12 h 2..	$x,0,0$ $\frac{1}{2},x+\frac{1}{2},\frac{1}{2}$	$\bar{x},0,0$ $\frac{1}{2},\bar{x}+\frac{1}{2},\frac{1}{2}$	$0,x,0$ $x+\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$0,\bar{x},0$ $\bar{x}+\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$0,0,x$ $\frac{1}{2},\frac{1}{2},\bar{x}+\frac{1}{2}$	$0,0,\bar{x}$ $\frac{1}{2},\frac{1}{2},x+\frac{1}{2}$	hkl: $h+k+l = 2n$
8 g .3.	x,x,x $\bar{x},x,\bar{x}$ $x+\frac{1}{2},x+\frac{1}{2},\bar{x}+\frac{1}{2}$ $x+\frac{1}{2},\bar{x}+\frac{1}{2},x+\frac{1}{2}$	$\bar{x},\bar{x},x$ x, $\bar{x},\bar{x}$ $\bar{x}+\frac{1}{2},\bar{x}+\frac{1}{2},\bar{x}+\frac{1}{2}$ $\bar{x}+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$					Ok: $k+l = 2n$
6 f 2.22	$\frac{1}{4},\frac{1}{2},0$	$\frac{3}{4},\frac{1}{2},0$	$0,\frac{1}{4},\frac{1}{2}$	$0,\frac{3}{4},\frac{1}{2}$	$\frac{1}{2},0,\frac{1}{4}$	$\frac{1}{2},0,\frac{3}{4}$	hkl: $h+k+l = 2n$ or $h = 2n+1, k = 4n$ and $l = 4n+2$
6 e 2.22	$\frac{1}{4},0,\frac{1}{2}$	$\frac{3}{4},0,\frac{1}{2}$	$\frac{1}{2},\frac{1}{4},0$	$\frac{1}{2},\frac{3}{4},0$	$0,\frac{1}{2},\frac{1}{4}$	$0,\frac{1}{2},\frac{3}{4}$	
6 d 222..	$0,\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},0,\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},0$	$0,\frac{1}{2},0$	$\frac{1}{2},0,0$	$0,0,\frac{1}{2}$	hkl: $h+k+l = 2n$
4 c .32	$\frac{3}{4},\frac{3}{4},\frac{3}{4}$	$\frac{1}{4},\frac{1}{4},\frac{3}{4}$	$\frac{1}{4},\frac{3}{4},\frac{1}{4}$	$\frac{3}{4},\frac{1}{4},\frac{1}{4}$			hkl: $h+k, h+l, k+l = 2n$
4 b .32	$\frac{1}{4},\frac{1}{4},\frac{1}{4}$	$\frac{3}{4},\frac{3}{4},\frac{1}{4}$	$\frac{3}{4},\frac{1}{4},\frac{3}{4}$	$\frac{1}{4},\frac{3}{4},\frac{3}{4}$			hkl: $h+k, h+l, k+l = 2n$
2 a 23.	0,0,0	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$					hkl: $h+k+l = 2n$

## Symmetry of special projections

Along [001]  $p4mm$  $\mathbf{a}' = \mathbf{a}$   $\mathbf{b}' = \mathbf{b}$ Origin at 0,  $\frac{1}{2}, z$ Along [111]  $p3m1$  $\mathbf{a}' = \frac{1}{3}(2\mathbf{a} - \mathbf{b} - \mathbf{c})$   $\mathbf{b}' = \frac{1}{3}(-\mathbf{a} + 2\mathbf{b} - \mathbf{c})$ 

Origin at x, x, x

Along [110]  $p2mm$  $\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b})$   $\mathbf{b}' = \mathbf{c}$ Origin at x, x,  $\frac{1}{4}$