

3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

3.2.3. Tables of the crystallographic point-group types

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The crystallographic point-group types are listed in Tables 3.2.3.1 and 3.2.3.2 for two-dimensional and for three-dimensional space, respectively. No listings are presented for the noncrystallographic point-group types (*i.e.* having axes of orders other than 1, 2, 3, 4 and 6), but their symbols can be found in Tables 3.2.1.5, 3.2.1.6 and 3.2.3.3 (*cf.* Section 3.2.1.4 for a review of noncrystallographic point groups). The two icosahedral point groups 235 and $m\bar{3}5$ are treated in detail in Section 3.2.1.4.2, while their crystallographic data are shown in Table 3.2.3.3.

There is a physical difference between the point groups of crystals and those of molecules. For a molecule, the point group is the set of all symmetry operations that map its atoms onto one another. Macroscopic crystals, however, hardly ever exhibit their ideal symmetry because of the defects that occur during crystal

growth. For a crystal, its point group is the set of all symmetry operations that map the set of the vectors normal to the crystal faces onto one another; it does not operate in point space, but in vector space.

In Tables 3.2.3.1 and 3.2.3.2 the point-group types are presented for crystals as well as for molecules. However, parts of the tables concern either crystals only or molecules only. The names of crystal forms in the fifth column (in roman type) and the *hkl* face indices in the last column are only relevant for crystals. The names of the point forms in the second line of each pair of entries in the fifth column (given in italics) and the other data (multiplicities, Wyckoff letters, site symmetries and sets of symmetry-equivalent coordinates) concern both crystals and molecules. However, for point groups with an origin fixed by symmetry, the Wyckoff position with the Wyckoff letter *o* is only of interest for molecules.

Because the meanings of the entries are not identical for crystals and for molecules, they are not explained here, but in Sections 3.2.1 (for crystals) and 3.2.4 (for molecules).

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Table 3.2.3.1

The ten two-dimensional crystallographic point groups

The point groups are listed in blocks according to crystal system and are specified by their Hermann–Mauguin symbols. For each point group, the stereographic projections show (on the left) the general position and (on the right) the symmetry elements.

The list of Wyckoff positions includes:

Columns 1 to 4: multiplicity, Wyckoff letter, oriented site-symmetry symbol, coordinate doublets;

Under the stereographic projections: edge forms (in roman type) and point forms (in italics); if there are two entries, the second entry refers to a limiting (noncharacteristic) form;

Last column: Miller indices of equivalent edges [for hexagonal groups, Bravais–Miller indices (*hki*) are used].

OBLIQUE SYSTEM							
1							
1	<i>a</i>	1	<i>x, y</i>	Single edge Single point	(<i>hk</i>)		
2							
2	<i>a</i>	1	<i>x, y</i> \bar{x}, \bar{y}	Pair of parallel edges Line segment through origin	(<i>hk</i>) ($\bar{h}\bar{k}$)		
1	<i>o</i>	2	0, 0	Point in origin			

3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.1 (continued)

RECTANGULAR SYSTEM					
<i>m</i>					
2	<i>b</i>	1	$x, y \quad \bar{x}, y$	Pair of edges Line segment	$(hk) \quad (\bar{h}k)$
				Pair of parallel edges Line segment through origin	$(10) \quad (\bar{1}0)$
1	<i>a</i>	<i>.m.</i>	$0, y$	Single edge Single point	$(01) \text{ or } (0\bar{1})$
<i>2mm</i>					
4	<i>c</i>	1	$x, y \quad \bar{x}, \bar{y} \quad \bar{x}, y \quad x, \bar{y}$	Rhomb Rectangle	$(hk) \quad (\bar{h}\bar{k}) \quad (\bar{h}k) \quad (h\bar{k})$
2	<i>b</i>	<i>.m.</i>	$0, y \quad 0, \bar{y}$	Pair of parallel edges Line segment through origin	$(01) \quad (0\bar{1})$
2	<i>a</i>	<i>.m.</i>	$x, 0 \quad \bar{x}, 0$	Pair of parallel edges Line segment through origin	$(10) \quad (\bar{1}0)$
1	<i>o</i>	<i>2mm</i>	$0, 0$	Point in origin	
SQUARE SYSTEM					
4					
4	<i>a</i>	1	$x, y \quad \bar{x}, \bar{y} \quad \bar{y}, x \quad y, \bar{x}$	Square Square	$(hk) \quad (\bar{h}\bar{k}) \quad (\bar{k}h) \quad (k\bar{h})$
1	<i>o</i>	<i>4..</i>	$0, 0$	Point in origin	
<i>4mm</i>					
8	<i>c</i>	1	$x, y \quad \bar{x}, \bar{y} \quad \bar{y}, x \quad y, \bar{x}$ $\bar{x}, y \quad x, \bar{y} \quad y, x \quad \bar{y}, \bar{x}$	Ditetragon Truncated square	$(hk) \quad (\bar{h}\bar{k}) \quad (\bar{k}h) \quad (k\bar{h})$ $(\bar{h}k) \quad (h\bar{k}) \quad (kh) \quad (k\bar{h})$
4	<i>b</i>	<i>.m.</i>	$x, x \quad \bar{x}, \bar{x} \quad \bar{x}, x \quad x, \bar{x}$	Square Square	$(11) \quad (\bar{1}\bar{1}) \quad (\bar{1}1) \quad (1\bar{1})$
4	<i>a</i>	<i>.m.</i>	$x, 0 \quad \bar{x}, 0 \quad 0, x \quad 0, \bar{x}$	Square Square	$(10) \quad (\bar{1}0) \quad (01) \quad (0\bar{1})$
1	<i>o</i>	<i>4mm</i>	$0, 0$	Point in origin	

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Table 3.2.3.1 (continued)

HEXAGONAL SYSTEM						
3						
	3	<i>a</i>	1	$x, y \quad \bar{y}, x - y \quad \bar{x} + y, \bar{x}$	Trigon Trigon	$(hki) \quad (ihk) \quad (kih)$
	1	<i>o</i>	3..	0, 0	Point in origin	
3m1						
	6	<i>b</i>	1	$x, y \quad \bar{y}, x - y \quad \bar{x} + y, \bar{x}$ $\bar{y}, \bar{x} \quad \bar{x} + y, y \quad x, x - y$	Ditrigon Truncated trigon	$(hki) \quad (ihk) \quad (kih)$ $(\bar{h}\bar{k}\bar{i}) \quad (\bar{i}\bar{h}\bar{k}) \quad (\bar{k}\bar{i}\bar{h})$
	3	<i>a</i>	. <i>m</i> .	$x, \bar{x} \quad x, 2x \quad 2\bar{x}, \bar{x}$	Hexagon Hexagon	$(11\bar{2}) \quad (\bar{2}11) \quad (1\bar{2}1)$ $(\bar{1}\bar{1}2) \quad (2\bar{1}\bar{1}) \quad (\bar{1}2\bar{1})$
	3	<i>a</i>	. <i>m</i> .	$x, \bar{x} \quad x, 2x \quad 2\bar{x}, \bar{x}$	Trigon Trigon	$(10\bar{1}) \quad (\bar{1}10) \quad (0\bar{1}1)$ or $(101) \quad (110) \quad (011)$
1	<i>o</i>	3 <i>m</i> .	0, 0	Point in origin		
31m						
	6	<i>b</i>	1	$x, y \quad \bar{y}, x - y \quad \bar{x} + y, \bar{x}$ $y, x \quad x - y, \bar{y} \quad \bar{x}, \bar{x} + y$	Ditrigon Truncated trigon	$(hki) \quad (ihk) \quad (kih)$ $(khi) \quad (ikh) \quad (hik)$
	3	<i>a</i>	.. <i>m</i>	$x, 0 \quad 0, x \quad \bar{x}, \bar{x}$	Hexagon Hexagon	$(10\bar{1}) \quad (\bar{1}10) \quad (0\bar{1}1)$ $(01\bar{1}) \quad (\bar{1}01) \quad (1\bar{1}0)$
	3	<i>a</i>	.. <i>m</i>	$x, 0 \quad 0, x \quad \bar{x}, \bar{x}$	Trigon Trigon	$(11\bar{2}) \quad (\bar{2}11) \quad (1\bar{2}1)$ or $(\bar{1}\bar{1}2) \quad (2\bar{1}\bar{1}) \quad (\bar{1}2\bar{1})$
1	<i>o</i>	3 <i>m</i>	0, 0	Point in origin		
6						
	6	<i>a</i>	1	$x, y \quad \bar{y}, x - y \quad \bar{x} + y, \bar{x}$ $\bar{x}, \bar{y} \quad y, \bar{x} + y \quad x - y, x$	Hexagon Hexagon	$(hki) \quad (ihk) \quad (kih)$ $(\bar{h}\bar{k}\bar{i}) \quad (\bar{i}\bar{h}\bar{k}) \quad (\bar{k}\bar{i}\bar{h})$
	1	<i>o</i>	6..	0, 0	Point in origin	
6mm						
	12	<i>c</i>	1	$x, y \quad \bar{y}, x - y \quad \bar{x} + y, \bar{x}$ $\bar{x}, \bar{y} \quad y, \bar{x} + y \quad x - y, x$ $\bar{y}, \bar{x} \quad \bar{x} + y, y \quad x, x - y$ $y, x \quad x - y, \bar{y} \quad \bar{x}, \bar{x} + y$	Dihexagon Truncated hexagon	$(hki) \quad (ihk) \quad (kih)$ $(\bar{h}\bar{k}\bar{i}) \quad (\bar{i}\bar{h}\bar{k}) \quad (\bar{k}\bar{i}\bar{h})$ $(\bar{k}\bar{h}\bar{i}) \quad (\bar{i}\bar{k}\bar{h}) \quad (\bar{h}\bar{i}\bar{k})$ $(khi) \quad (ikh) \quad (hik)$
	6	<i>b</i>	. <i>m</i> .	$x, \bar{x} \quad x, 2x \quad 2\bar{x}, \bar{x}$ $\bar{x}, x \quad \bar{x}, 2\bar{x} \quad 2x, x$	Hexagon Hexagon	$(10\bar{1}) \quad (\bar{1}10) \quad (0\bar{1}1)$ $(\bar{1}01) \quad (110) \quad (011)$
	6	<i>a</i>	.. <i>m</i>	$x, 0 \quad 0, x \quad \bar{x}, \bar{x}$ $\bar{x}, 0 \quad 0, \bar{x} \quad x, x$	Hexagon Hexagon	$(11\bar{2}) \quad (\bar{2}11) \quad (1\bar{2}1)$ $(\bar{1}\bar{1}2) \quad (2\bar{1}\bar{1}) \quad (\bar{1}2\bar{1})$
	1	<i>o</i>	6 <i>mm</i>	0, 0	Point in origin	

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Table 3.2.3.2

The 32 three-dimensional crystallographic point groups

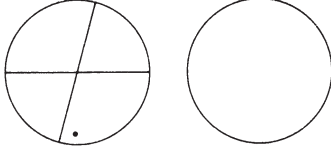
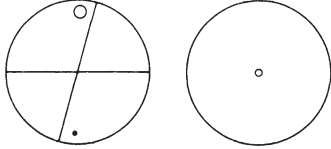
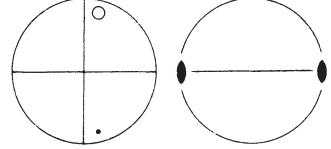
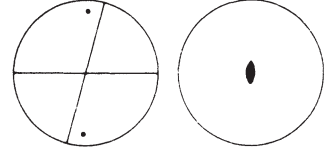
The point groups are listed in blocks according to crystal system and are specified by their short and (if different) full Hermann–Mauguin symbols and their Schoenflies symbols. For each point group, the stereographic projections show (on the left) the general position and (on the right) the symmetry elements.

The list of Wyckoff positions includes:

Columns 1 to 4: multiplicity, Wyckoff letter, oriented site-symmetry symbol, coordinate triplets;

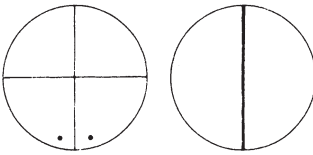
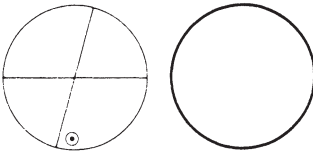
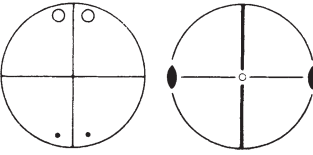
Under the stereographic projections: face forms (in roman type) and point forms (in italics); if there is more than one entry, subsequent entries refer to limiting (noncharacteristic) forms;

Last column: Miller indices of equivalent faces [for trigonal and hexagonal groups, Bravais–Miller indices (*hkl*) are used if referred to hexagonal axes].

TRICLINIC SYSTEM					
1	C_1				
1	<i>a</i>	1	<i>x, y, z</i>	Pedion or monohedron <i>Single point</i>	(<i>hkl</i>)
Symmetry of special projections Along any direction 1					
MONOCLINIC SYSTEM					
$\bar{1}$	C_i				
2	<i>a</i>	1	<i>x, y, z</i> $\bar{x}, \bar{y}, \bar{z}$	Pinacoid or parallelohedron <i>Line segment through origin</i>	(<i>hkl</i>) ($\bar{h}\bar{k}\bar{l}$)
1	<i>o</i>	$\bar{1}$	0, 0, 0	Point in origin	
Symmetry of special projections Along any direction 2					
MONOCLINIC SYSTEM					
2	C_2	UNIQUE AXIS <i>b</i>			
2	<i>b</i>	1	<i>x, y, z</i> $\bar{x}, \bar{y}, \bar{z}$	Sphenoid or dihedron <i>Line segment</i>	(<i>hkl</i>) ($\bar{h}\bar{k}\bar{l}$)
				Pinacoid or parallelohedron <i>Line segment through origin</i>	(<i>h0l</i>) ($\bar{h}\bar{0}\bar{l}$)
1	<i>a</i>	2	0, <i>y</i> , 0	Pedion or monohedron <i>Single point</i>	(010) or (0 $\bar{1}$ 0)
Symmetry of special projections Along [100] Along [010] Along [001] <i>m</i> 2 <i>m</i>					
2	C_2	UNIQUE AXIS <i>c</i>			
2	<i>b</i>	1	<i>x, y, z</i> $\bar{x}, \bar{y}, \bar{z}$	Sphenoid or dihedron <i>Line segment</i>	(<i>hkl</i>) ($\bar{h}\bar{k}\bar{l}$)
				Pinacoid or parallelohedron <i>Line segment through origin</i>	(<i>hk0</i>) ($\bar{h}\bar{k}\bar{0}$)
1	<i>a</i>	2	0, 0, <i>z</i>	Pedion or monohedron <i>Single point</i>	(001) or (00 $\bar{1}$)
Symmetry of special projections Along [100] Along [010] Along [001] <i>m</i> <i>m</i> 2					

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Table 3.2.3.2 (continued)

MONOCLINIC SYSTEM (<i>cont.</i>)					
m		C_s			
UNIQUÉ AXIS b					
2	b	1	x, y, z x, \bar{y}, z	Dome or dihedron Line segment	(hkl) $(h\bar{k}l)$
				Pinacoid or parallelohedron Line segment through origin	(010) $(0\bar{1}0)$
1	a	m	$x, 0, z$	Pedion or monohedron Single point	$(h0l)$
			Symmetry of special projections		
			Along [100]	Along [010]	Along [001]
			m	1	m
<hr/>					
m		C_s			
UNIQUÉ AXIS c					
2	b	1	x, y, z x, y, \bar{z}	Dome or dihedron Line segment	(hkl) $(h\bar{k}\bar{l})$
				Pinacoid or parallelohedron Line segment through origin	(001) $(00\bar{1})$
1	a	m	$x, y, 0$	Pedion or monohedron Single point	$(hk0)$
			Symmetry of special projections		
			Along [100]	Along [010]	Along [001]
			m	m	1
<hr/>					
$2/m$		C_{2h}			
UNIQUÉ AXIS b					
4	c	1	x, y, z \bar{x}, y, \bar{z} $\bar{x}, \bar{y}, \bar{z}$ x, \bar{y}, z	Rhombic prism Rectangle through origin	(hkl) $(\bar{h}\bar{k}\bar{l})$ $(\bar{h}\bar{k}l)$ $(h\bar{k}l)$
2	b	m	$x, 0, z$ $\bar{x}, 0, \bar{z}$	Pinacoid or parallelohedron Line segment through origin	$(h0l)$ $(\bar{h}0\bar{l})$
2	a	2	$0, y, 0$ $0, \bar{y}, 0$	Pinacoid or parallelohedron Line segment through origin	(010) $(0\bar{1}0)$
1	o	$2/m$	$0, 0, 0$	Point in origin	
			Symmetry of special projections		
			Along [100]	Along [010]	Along [001]
			$2mm$	2	$2mm$

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Table 3.2.3.2 (continued)

MONOCLINIC SYSTEM (cont.)									
$2/m$		C_{2h}							
UNIQUE AXIS c									
4	c	1	x, y, z	\bar{x}, \bar{y}, z	$\bar{x}, \bar{y}, \bar{z}$	x, y, \bar{z}	Rhombic prism <i>Rectangle through origin</i>	(hkl)	$(\bar{h}\bar{k}l)$ $(\bar{h}\bar{k}\bar{l})$ $(hk\bar{l})$
2	b	m	$x, y, 0$	$\bar{x}, \bar{y}, 0$			Pinacoid or parallelohedron <i>Line segment through origin</i>	$(hk0)$	$(\bar{h}\bar{k}0)$
2	a	2	$0, 0, z$	$0, 0, \bar{z}$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(001)	$(00\bar{1})$
1	o	$2/m$	$0, 0, 0$				<i>Point in origin</i>		
Symmetry of special projections									
			Along [100]	Along [010]	Along [001]				
			$2mm$	$2mm$	2				
ORTHORHOMBIC SYSTEM									
222		D_2							
4	d	1	x, y, z	\bar{x}, \bar{y}, z	\bar{x}, y, \bar{z}	x, \bar{y}, \bar{z}	Rhombic disphenoid or rhombic tetrahedron <i>Rhombic tetrahedron</i>	(hkl)	$(\bar{h}\bar{k}l)$ $(\bar{h}k\bar{l})$ $(h\bar{k}\bar{l})$
							Rhombic prism <i>Rectangle through origin</i>	$(hk0)$	$(\bar{h}\bar{k}0)$ $(\bar{h}k0)$ $(h\bar{k}0)$
							Rhombic prism <i>Rectangle through origin</i>	$(h0l)$	$(\bar{h}0l)$ $(\bar{h}0\bar{l})$ $(h0\bar{l})$
							Rhombic prism <i>Rectangle through origin</i>	$(0kl)$	$(0\bar{k}l)$ $(0k\bar{l})$ $(0\bar{k}\bar{l})$
2	c	$..2$	$0, 0, z$	$0, 0, \bar{z}$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(001)	$(00\bar{1})$
2	b	$.2.$	$0, y, 0$	$0, \bar{y}, 0$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(010)	$(0\bar{1}0)$
2	a	$2..$	$x, 0, 0$	$\bar{x}, 0, 0$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(100)	$(\bar{1}00)$
1	o	222	$0, 0, 0$				<i>Point in origin</i>		
Symmetry of special projections									
			Along [100]	Along [010]	Along [001]				
			$2mm$	$2mm$	$2mm$				

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Table 3.2.3.2 (continued)

ORTHORHOMBIC SYSTEM (<i>cont.</i>)											
$mm2$		C_{2v}									
4	d	1	x, y, z	\bar{x}, \bar{y}, z	x, \bar{y}, z	\bar{x}, y, z	Rhombic pyramid <i>Rectangle</i>	(hkl)	$(\bar{h}\bar{k}l)$	$(h\bar{k}l)$	$(\bar{h}kl)$
							Rhombic prism <i>Rectangle through origin</i>	$(hk0)$	$(\bar{h}\bar{k}0)$	$(h\bar{k}0)$	$(\bar{h}k0)$
2	c	$m..$	$0, y, z$	$0, \bar{y}, z$			Dome or dihedron <i>Line segment</i>	$(0kl)$	$(0\bar{k}l)$		
							Pinacoid or parallelohedron <i>Line segment through origin</i>	(010)	$(0\bar{1}0)$		
2	b	$.m.$	$x, 0, z$	$\bar{x}, 0, z$			Dome or dihedron <i>Line segment</i>	$(h0l)$	$(\bar{h}0l)$		
							Pinacoid or parallelohedron <i>Line segment through origin</i>	(100)	$(\bar{1}00)$		
1	a	$mm2$	$0, 0, z$				Pedion or monohedron <i>Single point</i>	(001)	or $(00\bar{1})$		
Symmetry of special projections											
			Along [100]	Along [010]	Along [001]						
			m	m	$2mm$						
$m m m$		D_{2h}									
8	g	1	x, y, z	\bar{x}, \bar{y}, z	\bar{x}, y, \bar{z}	x, \bar{y}, \bar{z}	Rhombic dipyrmaid <i>Rectangular prism</i>	(hkl)	$(\bar{h}\bar{k}l)$	$(\bar{h}k\bar{l})$	$(h\bar{k}\bar{l})$
			$\bar{x}, \bar{y}, \bar{z}$	x, y, \bar{z}	x, \bar{y}, z	\bar{x}, y, z		$(\bar{h}\bar{k}\bar{l})$	$(hk\bar{l})$	$(\bar{h}kl)$	$(h\bar{k}l)$
4	f	$.m$	$x, y, 0$	$\bar{x}, \bar{y}, 0$	$\bar{x}, y, 0$	$x, \bar{y}, 0$	Rhombic prism <i>Rectangle through origin</i>	$(hk0)$	$(\bar{h}\bar{k}0)$	$(\bar{h}k0)$	$(h\bar{k}0)$
4	e	$.m.$	$x, 0, z$	$\bar{x}, 0, z$	$\bar{x}, 0, \bar{z}$	$x, 0, \bar{z}$	Rhombic prism <i>Rectangle through origin</i>	$(h0l)$	$(\bar{h}0l)$	$(\bar{h}0\bar{l})$	$(h0\bar{l})$
4	d	$m..$	$0, y, z$	$0, \bar{y}, z$	$0, y, \bar{z}$	$0, \bar{y}, \bar{z}$	Rhombic prism <i>Rectangle through origin</i>	$(0kl)$	$(0\bar{k}l)$	$(0k\bar{l})$	$(0\bar{k}\bar{l})$
2	c	$mm2$	$0, 0, z$	$0, 0, \bar{z}$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(001)	$(00\bar{1})$		
2	b	$m2m$	$0, y, 0$	$0, \bar{y}, 0$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(010)	$(0\bar{1}0)$		
2	a	$2mm$	$x, 0, 0$	$\bar{x}, 0, 0$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(100)	$(\bar{1}00)$		
1	o	mmm	$0, 0, 0$				Point in origin				
Symmetry of special projections											
			Along [100]	Along [010]	Along [001]						
			$2mm$	$2mm$	$2mm$						

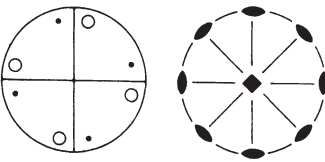
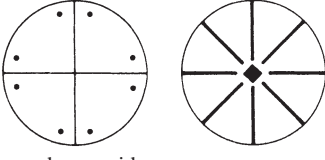
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Table 3.2.3.2 (continued)

TETRAGONAL SYSTEM																					
4	C_4																				
										4	b	1	x, y, z	\bar{x}, \bar{y}, z	\bar{y}, x, z	y, \bar{x}, z	Tetragonal pyramid Square	(hkl)	$(\bar{h}\bar{k}l)$	$(\bar{k}hl)$	$(k\bar{h}l)$
4	b	1	x, y, z	\bar{x}, \bar{y}, z	\bar{y}, x, z	y, \bar{x}, z	Tetragonal prism Square through origin	$(hk0)$	$(\bar{h}\bar{k}0)$	$(\bar{k}h0)$	$(k\bar{h}0)$										
1	a	4..	$0, 0, z$					Pedion or monohedron Single point	(001)	or	$(00\bar{1})$										
Symmetry of special projections																					
			Along [001]	Along [100]	Along [110]																
			4	m	m																
$\bar{4}$	S_4																				
										4	b	1	x, y, z	\bar{x}, \bar{y}, z	y, \bar{x}, \bar{z}	\bar{y}, x, \bar{z}	Tetragonal disphenoid or tetragonal tetrahedron Tetragonal tetrahedron	(hkl)	$(\bar{h}\bar{k}l)$	$(\bar{k}hl)$	$(k\bar{h}l)$
4	b	1	x, y, z	\bar{x}, \bar{y}, z	y, \bar{x}, \bar{z}	\bar{y}, x, \bar{z}	Tetragonal prism Square through origin	$(hk0)$	$(\bar{h}\bar{k}0)$	$(\bar{k}h0)$	$(k\bar{h}0)$										
2	a	2..	$0, 0, z$	$0, 0, \bar{z}$				Pinacoid or parallelohedron Line segment through origin	(001)		$(00\bar{1})$										
1	o	$\bar{4}..$	$0, 0, 0$					Point in origin													
Symmetry of special projections																					
			Along [001]	Along [100]	Along [110]																
			4	m	m																
$4/m$	C_{4h}																				
										8	c	1	x, y, z	\bar{x}, \bar{y}, z	\bar{y}, x, z	y, \bar{x}, z	Tetragonal dipyramid Tetragonal prism	(hkl)	$(\bar{h}\bar{k}l)$	$(\bar{k}hl)$	$(k\bar{h}l)$
													$\bar{x}, \bar{y}, \bar{z}$	x, y, \bar{z}	y, \bar{x}, \bar{z}	\bar{y}, x, \bar{z}					
4	b	m..	$x, y, 0$	$\bar{x}, \bar{y}, 0$	$\bar{y}, x, 0$	$y, \bar{x}, 0$	Tetragonal prism Square through origin	$(hk0)$	$(\bar{h}\bar{k}0)$	$(\bar{k}h0)$	$(k\bar{h}0)$										
2	a	4..	$0, 0, z$	$0, 0, \bar{z}$				Pinacoid or parallelohedron Line segment through origin	(001)		$(00\bar{1})$										
1	o	$4/m..$	$0, 0, 0$					Point in origin													
Symmetry of special projections																					
			Along [001]	Along [100]	Along [110]																
			4	2mm	2mm																

3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

TETRAGONAL SYSTEM (<i>cont.</i>)									
422		D_4							
8	<i>d</i>	1	x, y, z \bar{x}, \bar{y}, z \bar{y}, x, z y, \bar{x}, z \bar{x}, y, \bar{z} x, \bar{y}, \bar{z} y, x, \bar{z} $\bar{y}, \bar{x}, \bar{z}$		Tetragonal trapezohedron Twisted tetragonal antiprism	(hkl) $(\bar{h}\bar{k}l)$ $(\bar{k}hl)$ $(k\bar{h}l)$ $(\bar{h}k\bar{l})$ $(h\bar{k}\bar{l})$ (khl) $(\bar{k}\bar{h}\bar{l})$			
					Ditetragonal prism Truncated square through origin	$(hk0)$ $(\bar{h}\bar{k}0)$ $(\bar{k}h0)$ $(k\bar{h}0)$ $(\bar{h}k0)$ $(h\bar{k}0)$ $(kh0)$ $(\bar{k}\bar{h}0)$			
					Tetragonal dipyramid Tetragonal prism	$(h0l)$ $(\bar{h}0l)$ $(0hl)$ $(0\bar{h}l)$ $(\bar{h}0\bar{l})$ $(h0\bar{l})$ $(0h\bar{l})$ $(0\bar{h}\bar{l})$			
					Tetragonal dipyramid Tetragonal prism	(hhl) $(\bar{h}\bar{h}l)$ $(\bar{h}hl)$ $(h\bar{h}l)$ $(\bar{h}h\bar{l})$ $(h\bar{h}\bar{l})$ $(hh\bar{l})$ $(\bar{h}\bar{h}\bar{l})$			
4	<i>c</i>	.2	$x, 0, 0$ $\bar{x}, 0, 0$ $0, x, 0$ $0, \bar{x}, 0$		Tetragonal prism Square through origin	(100) $(\bar{1}00)$ (010) $(0\bar{1}0)$			
4	<i>b</i>	.2	$x, x, 0$ $\bar{x}, \bar{x}, 0$ $\bar{x}, x, 0$ $x, \bar{x}, 0$		Tetragonal prism Square through origin	(110) $(\bar{1}\bar{1}0)$ $(\bar{1}10)$ $(1\bar{1}0)$			
2	<i>a</i>	4.	$0, 0, z$ $0, 0, \bar{z}$		Pinacoid or parallelohedron Line segment through origin	(001) $(00\bar{1})$			
1	<i>o</i>	422	$0, 0, 0$		Point in origin				
Symmetry of special projections									
Along [001] Along [100] Along [110] 4mm 2mm 2mm									
$4mm$		C_{4v}							
8	<i>d</i>	1	x, y, z \bar{x}, \bar{y}, z \bar{y}, x, z y, \bar{x}, z x, \bar{y}, z \bar{x}, y, z \bar{y}, \bar{x}, z y, x, z		Ditetragonal pyramid Truncated square	(hkl) $(\bar{h}\bar{k}l)$ $(\bar{k}hl)$ $(k\bar{h}l)$ $(\bar{h}k\bar{l})$ $(h\bar{k}\bar{l})$ $(\bar{k}\bar{h}l)$ (khl)			
					Ditetragonal prism Truncated square through origin	$(hk0)$ $(\bar{h}\bar{k}0)$ $(\bar{k}h0)$ $(k\bar{h}0)$ $(\bar{h}k0)$ $(h\bar{k}0)$ $(\bar{k}\bar{h}0)$ $(kh0)$			
4	<i>c</i>	.m	$x, 0, z$ $\bar{x}, 0, z$ $0, x, z$ $0, \bar{x}, z$		Tetragonal pyramid Square	$(h0l)$ $(\bar{h}0l)$ $(0hl)$ $(0\bar{h}l)$			
					Tetragonal prism Square through origin	(100) $(\bar{1}00)$ (010) $(0\bar{1}0)$			
4	<i>b</i>	.m	x, x, z \bar{x}, \bar{x}, z \bar{x}, x, z x, \bar{x}, z		Tetragonal pyramid Square	(hhl) $(\bar{h}\bar{h}l)$ $(\bar{h}hl)$ $(h\bar{h}l)$			
					Tetragonal prism Square through origin	(110) $(\bar{1}\bar{1}0)$ $(\bar{1}10)$ $(1\bar{1}0)$			
1	<i>a</i>	4mm	$0, 0, z$		Pedion or monohedron Single point	(001) or $(00\bar{1})$			
Symmetry of special projections									
Along [001] Along [100] Along [110] 4mm m m									

3.2. POINT GROUPS AND CRYSTAL CLASSES

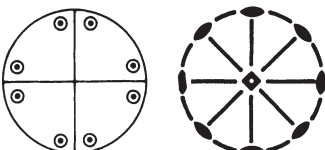
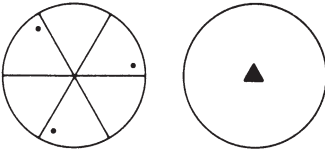
Table 3.2.3.2 (continued)

TETRAGONAL SYSTEM (cont.)											
$\bar{4}2m$		D_{2d}									
8	<i>d</i>	1	x, y, z $\bar{x}, \bar{y}, \bar{z}$	\bar{x}, \bar{y}, z x, \bar{y}, \bar{z}	y, \bar{x}, \bar{z} \bar{y}, \bar{x}, z	\bar{y}, x, \bar{z} y, x, z	Tetragonal scalenohedron <i>Tetragonal tetrahedron cut off by pinacoid</i>	(hkl) $(\bar{h}\bar{k}\bar{l})$	$(\bar{h}kl)$ $(h\bar{k}\bar{l})$	$(k\bar{h}\bar{l})$ $(\bar{k}hl)$	$(\bar{k}h\bar{l})$ $(kh\bar{l})$
							Ditetragonal prism <i>Truncated square through origin</i>	$(hk0)$ $(\bar{h}\bar{k}0)$	$(\bar{h}k0)$ $(h\bar{k}0)$	$(k\bar{h}0)$ $(\bar{k}h0)$	$(\bar{k}h0)$ $(kh0)$
							Tetragonal dipyramid <i>Tetragonal prism</i>	$(h0l)$ $(\bar{h}0\bar{l})$	$(\bar{h}0l)$ $(h0\bar{l})$	$(0\bar{h}\bar{l})$ $(0h\bar{l})$	$(0h\bar{l})$ $(0\bar{h}l)$
4	<i>c</i>	$.m$	x, x, z	\bar{x}, \bar{x}, z	x, \bar{x}, \bar{z}	\bar{x}, x, \bar{z}	Tetragonal disphenoid or tetragonal tetrahedron <i>Tetragonal tetrahedron</i>	(hhl)	$(\bar{h}\bar{h}l)$	$(h\bar{h}\bar{l})$	$(\bar{h}h\bar{l})$
							Tetragonal prism <i>Square through origin</i>	(110)	$(\bar{1}\bar{1}0)$	$(1\bar{1}0)$	$(\bar{1}10)$
4	<i>b</i>	$.2$	$x, 0, 0$	$\bar{x}, 0, 0$	$0, \bar{x}, 0$	$0, x, 0$	Tetragonal prism <i>Square through origin</i>	(100)	$(\bar{1}00)$	$(0\bar{1}0)$	(010)
2	<i>a</i>	$2mm$	$0, 0, z$	$0, 0, \bar{z}$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(001)	$(00\bar{1})$		
1	<i>o</i>	$\bar{4}2m$	$0, 0, 0$				Point in origin				
Symmetry of special projections											
			Along [001]	Along [100]			Along [110]				
			$4mm$	$2mm$			m				

$\bar{4}m2$		D_{2d}									
8	<i>d</i>	1	x, y, z x, \bar{y}, z	\bar{x}, \bar{y}, z \bar{x}, y, z	y, \bar{x}, \bar{z} y, x, \bar{z}	\bar{y}, x, \bar{z} $\bar{y}, \bar{x}, \bar{z}$	Tetragonal scalenohedron <i>Tetragonal tetrahedron cut off by pinacoid</i>	(hkl) $(\bar{h}\bar{k}\bar{l})$	$(\bar{h}kl)$ $(h\bar{k}\bar{l})$	$(k\bar{h}\bar{l})$ $(\bar{k}hl)$	$(\bar{k}h\bar{l})$ $(kh\bar{l})$
							Ditetragonal prism <i>Truncated square through origin</i>	$(hk0)$ $(\bar{h}\bar{k}0)$	$(\bar{h}k0)$ $(h\bar{k}0)$	$(k\bar{h}0)$ $(\bar{k}h0)$	$(\bar{k}h0)$ $(kh0)$
							Tetragonal dipyramid <i>Tetragonal prism</i>	(hhl) $(\bar{h}\bar{h}l)$	$(\bar{h}hl)$ $(h\bar{h}\bar{l})$	$(h\bar{h}\bar{l})$ $(\bar{h}h\bar{l})$	$(\bar{h}hl)$ $(h\bar{h}l)$
4	<i>c</i>	$.m$	$x, 0, z$	$\bar{x}, 0, z$	$0, \bar{x}, \bar{z}$	$0, x, \bar{z}$	Tetragonal disphenoid or tetragonal tetrahedron <i>Tetragonal tetrahedron</i>	$(h0l)$	$(\bar{h}0\bar{l})$	$(0\bar{h}\bar{l})$	$(0h\bar{l})$
							Tetragonal prism <i>Square through origin</i>	(100)	$(\bar{1}00)$	$(0\bar{1}0)$	(010)
4	<i>b</i>	$.2$	$x, x, 0$	$\bar{x}, \bar{x}, 0$	$x, \bar{x}, 0$	$\bar{x}, x, 0$	Tetragonal prism <i>Square through origin</i>	(110)	$(\bar{1}\bar{1}0)$	$(1\bar{1}0)$	$(\bar{1}10)$
2	<i>a</i>	$2mm$	$0, 0, z$	$0, 0, \bar{z}$			Pinacoid or parallelohedron <i>Line segment through origin</i>	(001)	$(00\bar{1})$		
1	<i>o</i>	$\bar{4}m2$	$0, 0, 0$				Point in origin				
Symmetry of special projections											
			Along [001]	Along [100]			Along [110]				
			$4mm$	m			$2mm$				

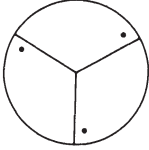
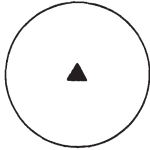
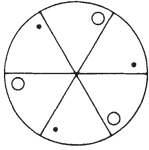
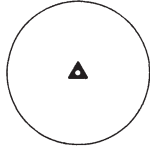
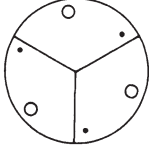
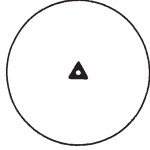
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

TETRAGONAL SYSTEM (cont.)									
$4/mmm$		D_{4h}							
$\frac{4}{m} \frac{2}{m} \frac{2}{m}$									
16	<i>g</i>	1	x, y, z \bar{x}, y, \bar{z} $\bar{x}, \bar{y}, \bar{z}$ x, \bar{y}, z	\bar{x}, \bar{y}, z x, \bar{y}, \bar{z} x, y, \bar{z} \bar{x}, y, z	\bar{y}, x, z y, x, \bar{z} y, \bar{x}, \bar{z} \bar{y}, x, z	y, \bar{x}, z $\bar{y}, \bar{x}, \bar{z}$ \bar{y}, x, \bar{z} y, x, z	Ditetragonal dipyramid Edge-truncated tetragonal prism	(hkl) $(\bar{h}\bar{k}\bar{l})$ $(\bar{h}k\bar{l})$ $(h\bar{k}l)$	$(\bar{k}hl)$ $(k\bar{h}l)$ (khl) $(\bar{k}\bar{h}l)$
8	<i>f</i>	<i>.m</i>	$x, 0, z$ $\bar{x}, 0, \bar{z}$	$\bar{x}, 0, z$ $x, 0, \bar{z}$	$0, x, z$ $0, x, \bar{z}$	$0, \bar{x}, z$ $0, \bar{x}, \bar{z}$	Tetragonal dipyramid Tetragonal prism	$(h0l)$ $(\bar{h}0\bar{l})$	$(0hl)$ $(0\bar{h}\bar{l})$
8	<i>e</i>	<i>.m</i>	x, x, z \bar{x}, x, \bar{z}	\bar{x}, \bar{x}, z x, \bar{x}, \bar{z}	\bar{x}, x, z x, x, \bar{z}	x, \bar{x}, z $\bar{x}, \bar{x}, \bar{z}$	Tetragonal dipyramid Tetragonal prism	(hhl) $(\bar{h}\bar{h}\bar{l})$	$(\bar{h}hl)$ (hhl)
8	<i>d</i>	<i>m.</i>	$x, y, 0$ $\bar{x}, y, 0$	$\bar{x}, \bar{y}, 0$ $x, \bar{y}, 0$	$\bar{y}, x, 0$ $y, x, 0$	$y, \bar{x}, 0$ $\bar{y}, \bar{x}, 0$	Ditetragonal prism Truncated square through origin	$(hk0)$ $(\bar{h}\bar{k}0)$	$(\bar{k}h0)$ $(k\bar{h}0)$
4	<i>c</i>	<i>m2m</i>	$x, 0, 0$	$\bar{x}, 0, 0$	$0, x, 0$	$0, \bar{x}, 0$	Tetragonal prism Square through origin	(100)	$(\bar{1}00)$ (010) $(0\bar{1}0)$
4	<i>b</i>	<i>m.m2</i>	$x, x, 0$	$\bar{x}, \bar{x}, 0$	$\bar{x}, x, 0$	$x, \bar{x}, 0$	Tetragonal prism Square through origin	(110)	$(\bar{1}\bar{1}0)$ $(\bar{1}10)$ $(1\bar{1}0)$
2	<i>a</i>	<i>4mm</i>	$0, 0, z$	$0, 0, \bar{z}$			Pinacoid or parallelohedron Line segment through origin	(001)	$(00\bar{1})$
1	<i>o</i>	<i>4/mmm</i>	$0, 0, 0$			Point in origin			
Symmetry of special projections									
			Along [001]	Along [100]	Along [110]				
			<i>4mm</i>	<i>2mm</i>	<i>2mm</i>				
TRIGONAL SYSTEM									
3		C_3							
HEXAGONAL AXES									
3	<i>b</i>	1	x, y, z	$\bar{y}, x - y, z$	$\bar{x} + y, \bar{x}, z$	Trigonal pyramid Trigon		(hki)	$(ihkl)$ $(kihl)$
						Trigonal prism Trigon through origin		$(hki0)$	$(ihk0)$ $(kih0)$
1	<i>a</i>	<i>3.</i>	$0, 0, z$			Pedion or monohedron Single point		(0001)	or $(000\bar{1})$
Symmetry of special projections									
			Along [001]	Along [100]	Along [210]				
			3	1	1				

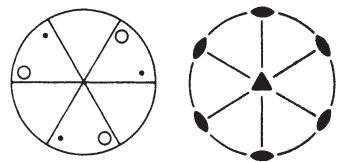
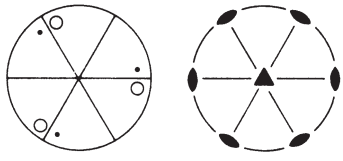
3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (<i>cont.</i>)					
3	C_3				
RHOMBOHEDRAL AXES					
3	b 1	$x, y, z \quad z, x, y \quad y, z, x$	Trigonal pyramid <i>Trigon</i>		$(hkl) \quad (lhk) \quad (klh)$
			Trigonal prism <i>Trigon through origin</i>		$(hk(\overline{h+k}) \quad ((\overline{h+k})hk) \quad (k(\overline{h+k})h)$
1	a 3.	x, x, x	Pedion or monohedron <i>Single point</i>		$(111) \text{ or } (\overline{1}\overline{1}\overline{1})$
			Symmetry of special projections		
			Along $[111]$	Along $[1\overline{1}0]$	Along $[2\overline{1}\overline{1}]$
			3	1	1
$\overline{3}$					
HEXAGONAL AXES					
	C_{3i}				
6	b 1	$x, y, z \quad \overline{y}, x - y, z \quad \overline{x} + y, \overline{x}, z$ $\overline{x}, \overline{y}, \overline{z} \quad y, \overline{x} + y, \overline{z} \quad x - y, x, \overline{z}$	Rhombohedron <i>Trigonal antiprism</i>		$(hkl) \quad (ihkl) \quad (kihl)$ $(\overline{h}\overline{k}\overline{l}) \quad (\overline{i}\overline{h}\overline{k}\overline{l}) \quad (\overline{k}\overline{i}\overline{h}\overline{l})$
			Hexagonal prism <i>Hexagon through origin</i>		$(hki0) \quad (ihk0) \quad (kih0)$ $(\overline{h}\overline{k}\overline{i}0) \quad (\overline{i}\overline{h}\overline{k}0) \quad (\overline{k}\overline{i}\overline{h}0)$
2	a 3..	$0, 0, z \quad 0, 0, \overline{z}$	Pinacoid or parallelohedron <i>Line segment through origin</i>		$(0001) \quad (000\overline{1})$
1	o $\overline{3}$..	$0, 0, 0$	<i>Point in origin</i>		
			Symmetry of special projections		
			Along $[001]$	Along $[100]$	Along $[210]$
			6	2	2
$\overline{3}$					
RHOMBOHEDRAL AXES					
	C_{3i}				
6	b 1	$x, y, z \quad z, x, y \quad y, z, x$ $\overline{x}, \overline{y}, \overline{z} \quad \overline{z}, \overline{x}, \overline{y} \quad \overline{y}, \overline{z}, \overline{x}$	Rhombohedron <i>Trigonal antiprism</i>		$(hkl) \quad (lhk) \quad (klh)$ $(\overline{h}\overline{k}\overline{l}) \quad (\overline{l}\overline{h}\overline{k}) \quad (\overline{k}\overline{l}\overline{h})$
			Hexagonal prism <i>Hexagon through origin</i>		$(hk(\overline{h+k}) \quad ((\overline{h+k})hk) \quad (k(\overline{h+k})h)$ $(\overline{h}\overline{k}(\overline{h+k}) \quad ((\overline{h+k})\overline{h}\overline{k}) \quad (\overline{k}(\overline{h+k})\overline{h})$
2	a 3.	$x, x, x \quad \overline{x}, \overline{x}, \overline{x}$	Pinacoid or parallelohedron <i>Line segment through origin</i>		$(111) \quad (\overline{1}\overline{1}\overline{1})$
1	o $\overline{3}$..	$0, 0, 0$	<i>Point in origin</i>		
			Symmetry of special projections		
			Along $[111]$	Along $[1\overline{1}0]$	Along $[2\overline{1}\overline{1}]$
			6	2	2

3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (<i>cont.</i>)									
312 D_3 HEXAGONAL AXES									
6	<i>c</i>	1	x, y, z $\bar{y}, \bar{x}, \bar{z}$	$\bar{y}, x - y, z$ $\bar{x} + y, y, \bar{z}$	$\bar{x} + y, \bar{x}, z$ $x, x - y, \bar{z}$	Trigonal trapezohedron Twisted trigonal antiprism Ditrigonal prism Truncated trigon through origin Trigonal dipyramid Trigonal prism Rhombohedron Trigonal antiprism Hexagonal prism Hexagon through origin	(hkl) $(\bar{k}h\bar{l})$ $(hki0)$ $(\bar{k}\bar{h}\bar{i}0)$ $(h0\bar{h}l)$ $(0\bar{h}hl)$ $(hh\bar{2}h\bar{l})$ $(\bar{h}\bar{h}2h\bar{l})$ $(11\bar{2}0)$ $(\bar{1}\bar{1}20)$	$(ihkl)$ $(\bar{h}i\bar{k}\bar{l})$ $(ihk0)$ $(\bar{h}\bar{i}\bar{k}0)$ $(\bar{h}h0l)$ $(\bar{h}h0\bar{l})$ $(\bar{2}h\bar{h}hl)$ $(\bar{h}2h\bar{h}\bar{l})$ $(\bar{2}110)$ $(\bar{1}2\bar{1}0)$	$(kihl)$ $(i\bar{k}h\bar{l})$ $(kih0)$ $(i\bar{k}\bar{h}0)$ $(0\bar{h}hl)$ $(h0\bar{h}\bar{l})$ $(h\bar{2}hhl)$ $(2h\bar{h}\bar{h}\bar{l})$ $(\bar{1}2\bar{1}0)$ $(2\bar{1}\bar{1}0)$
3	<i>b</i>	..2	$x, \bar{x}, 0$	$x, 2x, 0$	$2\bar{x}, \bar{x}, 0$	Trigonal prism Trigon through origin	$(10\bar{1}0)$ or $(\bar{1}010)$	$(\bar{1}100)$ or $(1\bar{1}00)$	$(0\bar{1}10)$ or $(01\bar{1}0)$
2	<i>a</i>	3..	$0, 0, z$	$0, 0, \bar{z}$		Pinacoid or parallelohedron Line segment through origin	(0001)	$(000\bar{1})$	
1	<i>o</i>	3.2	$0, 0, 0$			Point in origin			
Symmetry of special projections									
			Along [001]	Along [100]	Along [210]				
			3m	1	2				
321 D_3 HEXAGONAL AXES									
6	<i>c</i>	1	x, y, z y, x, \bar{z}	$\bar{y}, x - y, z$ $x - y, \bar{y}, \bar{z}$	$\bar{x} + y, \bar{x}, z$ $\bar{x}, \bar{x} + y, \bar{z}$	Trigonal trapezohedron Twisted trigonal antiprism Ditrigonal prism Truncated trigon through origin Trigonal dipyramid Trigonal prism Rhombohedron Trigonal antiprism Hexagonal prism Hexagon through origin	(hkl) $(kh\bar{l})$ $(hki0)$ $(khi0)$ $(hh\bar{2}h\bar{l})$ $(hh\bar{2}h\bar{l})$ $(h0\bar{h}l)$ $(0\bar{h}hl)$ $(10\bar{1}0)$ $(01\bar{1}0)$	$(ihkl)$ $(hik\bar{l})$ $(ihk0)$ $(hik0)$ $(\bar{2}h\bar{h}hl)$ $(h\bar{2}h\bar{h}\bar{l})$ $(\bar{h}h0l)$ $(h\bar{h}0\bar{l})$ $(\bar{1}100)$ $(1\bar{1}00)$	$(kihl)$ $(i\bar{k}h\bar{l})$ $(kih0)$ $(i\bar{k}h0)$ $(h\bar{2}hhl)$ $(2h\bar{h}\bar{h}\bar{l})$ $(0\bar{h}hl)$ $(\bar{h}0\bar{h}\bar{l})$ $(0\bar{1}10)$ $(\bar{1}010)$
3	<i>b</i>	.2.	$x, 0, 0$	$0, x, 0$	$\bar{x}, \bar{x}, 0$	Trigonal prism Trigon through origin	$(11\bar{2}0)$ or $(\bar{1}\bar{1}20)$	$(\bar{2}110)$ or $(2\bar{1}\bar{1}0)$	$(\bar{1}2\bar{1}0)$ or $(12\bar{1}0)$
2	<i>a</i>	3..	$0, 0, z$	$0, 0, \bar{z}$		Pinacoid or parallelohedron Line segment through origin	(0001)	$(000\bar{1})$	
1	<i>o</i>	32.	$0, 0, 0$			Point in origin			
Symmetry of special projections									
			Along [001]	Along [100]	Along [210]				
			3m	2	1				

3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (cont.)									
32 D_3 RHOMBOHEDRAL AXES									
6	c	1	x, y, z $\bar{z}, \bar{y}, \bar{x}$	z, x, y $\bar{y}, \bar{x}, \bar{z}$	y, z, x $\bar{x}, \bar{z}, \bar{y}$	Trigonal trapezohedron <i>Twisted trigonal antiprism</i>	(hkl) $(\bar{k}\bar{h}\bar{l})$	(lhk) $(\bar{h}\bar{l}\bar{k})$	(klh) $(\bar{l}\bar{k}\bar{h})$
						Ditrigonal prism <i>Truncated trigon through origin</i>	$(hk(\bar{h}+\bar{k}))$ $(\bar{k}\bar{h}(h+k))$	$((\bar{h}+\bar{k})hk)$ $(\bar{h}(h+k)\bar{k})$	$(k(\bar{h}+\bar{k})h)$ $((h+k)\bar{k}\bar{h})$
						Trigonal dipyramid <i>Trigonal prism</i>	$(hk(2k-h))$ $(\bar{k}\bar{h}(h-2k))$	$((2k-h)hk)$ $(\bar{h}(h-2k)\bar{k})$	$(k(2k-h)h)$ $((h-2k)\bar{k}\bar{h})$
						Rhombohedron <i>Trigonal antiprism</i>	(hhl) $(\bar{h}\bar{h}\bar{l})$	(lhh) $(\bar{h}\bar{l}\bar{h})$	(hll) $(\bar{l}\bar{h}\bar{h})$
						Hexagonal prism <i>Hexagon through origin</i>	$(11\bar{2})$ $(\bar{1}\bar{1}2)$	$(\bar{2}11)$ $(\bar{1}2\bar{1})$	$(\bar{1}2\bar{1})$ $(2\bar{1}\bar{1})$
3	b	2	$x, \bar{x}, 0$	$0, x, \bar{x}$	$\bar{x}, 0, x$	Trigonal prism <i>Trigon through origin</i>	$(01\bar{1})$ or $(0\bar{1}1)$	$(\bar{1}01)$ $(10\bar{1})$	$(\bar{1}10)$ $(\bar{1}10)$
2	a	3	x, x, x	$\bar{x}, \bar{x}, \bar{x}$		Pinacoid or parallelohedron <i>Line segment through origin</i>	(111)	$(\bar{1}\bar{1}\bar{1})$	
1	o	32	$0, 0, 0$			<i>Point in origin</i>			
Symmetry of special projections									
			Along $[111]$	Along $[1\bar{1}0]$	Along $[2\bar{1}\bar{1}]$				
			$3m$	2	1				
$3m1$ C_{3v} HEXAGONAL AXES									
6	c	1	x, y, z \bar{y}, \bar{x}, z	$\bar{y}, x-y, z$ $\bar{x}+y, y, z$	$\bar{x}+y, \bar{x}, z$ $x, x-y, z$	Ditrigonal pyramid <i>Truncated trigon</i>	$(hki\bar{l})$ $(\bar{k}\bar{h}\bar{i}\bar{l})$	$(ihk\bar{l})$ $(\bar{h}\bar{i}\bar{k}\bar{l})$	$(kihl)$ $(\bar{i}\bar{k}\bar{h}\bar{l})$
						Ditrigonal prism <i>Truncated trigon through origin</i>	$(hki0)$ $(\bar{k}\bar{h}\bar{i}0)$	$(ihk0)$ $(\bar{h}\bar{i}\bar{k}0)$	$(kih0)$ $(\bar{i}\bar{k}\bar{h}0)$
						Hexagonal pyramid <i>Hexagon</i>	$(hh\bar{2}hl)$ $(\bar{h}\bar{h}2hl)$	$(\bar{2}hhhl)$ $(h2hhl)$	$(h\bar{2}hhl)$ $(\bar{h}2hhl)$
						Hexagonal prism <i>Hexagon through origin</i>	$(11\bar{2}0)$ $(\bar{1}\bar{1}20)$	$(\bar{2}110)$ $(\bar{1}2\bar{1}0)$	$(\bar{1}2\bar{1}0)$ $(2\bar{1}\bar{1}0)$
3	b	$m.$	x, \bar{x}, z	$x, 2x, z$	$2\bar{x}, \bar{x}, z$	Trigonal pyramid <i>Trigon</i>	$(h0\bar{h}l)$	$(\bar{h}0l)$	$(0\bar{h}hl)$
						Trigonal prism <i>Trigon through origin</i>	$(10\bar{1}0)$ or $(\bar{1}010)$	$(\bar{1}100)$ $(\bar{1}100)$	$(0\bar{1}10)$ $(01\bar{1}0)$
1	a	$3m.$	$0, 0, z$			Pedion or monohedron <i>Single point</i>	(0001) or $(000\bar{1})$		
Symmetry of special projections									
			Along $[001]$	Along $[100]$	Along $[210]$				
			$3m$	1	m				

3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (<i>cont.</i>)									
31m		C_{3v}							
HEXAGONAL AXES									
6	c	1	x, y, z y, x, z	$\bar{y}, x - y, z$ $x - y, \bar{y}, z$	$\bar{x} + y, \bar{x}, z$ $\bar{x}, \bar{x} + y, z$	Ditrigonal pyramid Truncated trigon Ditrigonal prism Truncated trigon through origin Hexagonal pyramid Hexagon Hexagonal prism Hexagon through origin	(hkl) $(ihkl)$ $(kihl)$ (khl) $(hikl)$ (ikh) $(hki0)$ $(ihk0)$ $(kih0)$ $(khi0)$ $(hik0)$ $(ikh0)$ $(h\bar{0}hl)$ $(\bar{h}h0l)$ $(0\bar{h}hl)$ $(0h\bar{h}l)$ $(h\bar{h}0l)$ $(\bar{h}0hl)$ $(10\bar{1}0)$ $(\bar{1}100)$ $(0\bar{1}10)$ $(01\bar{1}0)$ $(\bar{1}\bar{1}00)$ $(\bar{1}010)$		
3	b	.m	$x, 0, z$ $0, x, z$	\bar{x}, \bar{x}, z		Trigonal pyramid Trigon Trigonal prism Trigon through origin	$(hh\bar{2}hl)$ $(\bar{2}hhhl)$ $(h\bar{2}hhl)$ $(11\bar{2}0)$ $(\bar{2}110)$ $(1\bar{2}10)$ or $(\bar{1}\bar{1}20)$ $(2\bar{1}\bar{1}0)$ $(\bar{1}2\bar{1}0)$		
1	a	3.m	$0, 0, z$			Pedion or monohedron Single point	(0001) or $(000\bar{1})$		
Symmetry of special projections									
Along [001] Along [100] Along [210] 3m m 1									
3m		C_{3v}							
RHOMBOHEDRAL AXES									
6	c	1	x, y, z z, y, x	z, x, y y, x, z	y, z, x x, z, y	Ditrigonal pyramid Truncated trigon Ditrigonal prism Truncated trigon through origin Hexagonal pyramid Hexagon Hexagonal prism Hexagon through origin	(hkl) (lkh) (klh) (khl) (hlk) (lkh) $(hk(\bar{h}+\bar{k}))$ $((\bar{h}+\bar{k})hk)$ $(k(\bar{h}+\bar{k})h)$ $(kh(\bar{h}+\bar{k}))$ $(h(\bar{h}+\bar{k})k)$ $((\bar{h}+\bar{k})kh)$ $(hk(2k-h))$ $((2k-h)hk)$ $(k(2k-h)h)$ $(kh(2k-h))$ $(h(2k-h)k)$ $((2k-h)kh)$ $(0\bar{1}\bar{1})$ $(\bar{1}0\bar{1})$ $(\bar{1}\bar{1}0)$ $(10\bar{1})$ $(0\bar{1}1)$ $(\bar{1}10)$		
3	b	.m	x, y, x x, x, y	y, x, x		Trigonal pyramid Trigon Trigonal prism Trigon through origin	(hhl) (lhh) (hll) $(11\bar{2})$ $(\bar{2}11)$ $(1\bar{2}1)$ or $(\bar{1}\bar{1}2)$ $(2\bar{1}\bar{1})$ $(\bar{1}2\bar{1})$		
1	a	3m	x, x, x			Pedion or monohedron Single point	(111) or $(\bar{1}\bar{1}\bar{1})$		
Symmetry of special projections									
Along [111] Along [1 $\bar{1}$ 0] Along [2 $\bar{1}\bar{1}$] 3m 1 m									

3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (<i>cont.</i>)									
$\bar{3}1m$		D_{3d}							
$\bar{3}1\frac{2}{m}$									
HEXAGONAL AXES									
12	<i>d</i>	1	x, y, z	$\bar{y}, x - y, z$	$\bar{x} + y, \bar{x}, z$	Ditrigonal scalenohedron or hexagonal scalenohedron	(hkl)	$(ihkl)$	$(kihl)$
			$\bar{y}, \bar{x}, \bar{z}$	$\bar{x} + y, y, \bar{z}$	$x, x - y, \bar{z}$	Trigonal antiprism sliced off by pinacoid	$(\bar{k}\bar{h}\bar{l})$	$(\bar{h}\bar{i}\bar{k}\bar{l})$	$(\bar{i}\bar{k}\bar{h}\bar{l})$
			$\bar{x}, \bar{y}, \bar{z}$	$y, \bar{x} + y, \bar{z}$	$x - y, x, \bar{z}$		$(\bar{h}\bar{k}\bar{l})$	$(\bar{i}\bar{h}\bar{k}\bar{l})$	$(\bar{k}\bar{i}\bar{h}\bar{l})$
			y, x, z	$x - y, \bar{y}, z$	$\bar{x}, \bar{x} + y, z$	Dihexagonal prism	(khl)	$(hikl)$	(ikh)
						Truncated hexagon through origin	$(hki0)$	$(ihk0)$	$(kih0)$
							$(\bar{k}\bar{h}\bar{i}0)$	$(\bar{h}\bar{i}\bar{k}0)$	$(\bar{i}\bar{k}\bar{h}0)$
							$(\bar{h}\bar{k}\bar{i}0)$	$(\bar{i}\bar{h}\bar{k}0)$	$(\bar{k}\bar{i}\bar{h}0)$
							$(khi0)$	$(hik0)$	$(ikh0)$
						Hexagonal dipyrmaid	$(h0\bar{h}l)$	$(\bar{h}h0l)$	$(0\bar{h}hl)$
						Hexagonal prism	$(0\bar{h}h\bar{l})$	$(\bar{h}h0\bar{l})$	$(h0\bar{h}\bar{l})$
							$(\bar{h}0h\bar{l})$	$(h\bar{h}0\bar{l})$	$(0h\bar{h}\bar{l})$
							$(0hh\bar{l})$	$(h\bar{h}0l)$	$(h0hl)$
6	<i>c</i>	$\dots m$	$x, 0, z$	$0, x, z$	\bar{x}, \bar{x}, z	Rhombohedron	$(hh\bar{2}hl)$	$(\bar{2}hhhl)$	$(h\bar{2}hhl)$
			$0, \bar{x}, \bar{z}$	$\bar{x}, 0, \bar{z}$	x, x, \bar{z}	Trigonal antiprism	$(\bar{h}\bar{h}2hl)$	$(h\bar{2}h\bar{h}\bar{l})$	$(2hh\bar{h}\bar{l})$
						Hexagonal prism	$(11\bar{2}0)$	$(\bar{2}110)$	$(1\bar{2}10)$
						Hexagon through origin	$(\bar{1}\bar{1}20)$	$(\bar{1}\bar{2}10)$	$(2\bar{1}\bar{1}0)$
6	<i>b</i>	$\dots 2$	$x, \bar{x}, 0$	$x, 2x, 0$	$2\bar{x}, \bar{x}, 0$	Hexagonal prism	$(10\bar{1}0)$	$(\bar{1}100)$	$(0\bar{1}10)$
			$\bar{x}, x, 0$	$\bar{x}, 2\bar{x}, 0$	$2x, x, 0$	Hexagon through origin	$(\bar{1}010)$	$(1\bar{1}00)$	$(01\bar{1}0)$
2	<i>a</i>	$\dots 3m$	$0, 0, z$	$0, 0, \bar{z}$		Pinacoid or parallelohedron	(0001)	$(000\bar{1})$	
						Line segment through origin			
1	<i>o</i>	$\bar{3}.m$	$0, 0, 0$			Point in origin			
Symmetry of special projections									
			Along [001]	Along [100]	Along [210]				
			6mm	2mm	2				

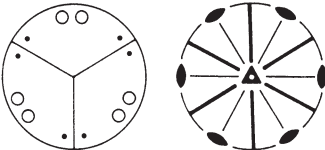
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (<i>cont.</i>)						
$\bar{3}m1$						
$\bar{3}2$						
$\bar{3}1$						
m						
HEXAGONAL AXES						
12	<i>d</i>	1	x, y, z $\bar{y}, x - y, z$ $\bar{x} + y, \bar{x}, z$ y, x, \bar{z} $x - y, \bar{y}, \bar{z}$ $\bar{x}, \bar{x} + y, \bar{z}$ $\bar{x}, \bar{y}, \bar{z}$ $y, \bar{x} + y, \bar{z}$ $x - y, x, \bar{z}$ \bar{y}, \bar{x}, z $\bar{x} + y, y, z$ $x, x - y, z$	Ditrigonal scalenohedron or hexagonal scalenohedron <i>Trigonal antiprism sliced off by pinacoid</i> Dihexagonal prism <i>Truncated hexagon through origin</i> Hexagonal dipyrmaid <i>Hexagonal prism</i>	(hkl) $(ihkl)$ $(kihl)$ $(k\bar{h}l)$ $(h\bar{i}l)$ $(i\bar{k}l)$ $(\bar{h}k\bar{l})$ $(\bar{i}h\bar{k}l)$ $(k\bar{i}\bar{h}l)$ $(\bar{k}\bar{h}\bar{l})$ $(\bar{h}\bar{i}\bar{k}l)$ $(\bar{i}\bar{k}\bar{h}l)$ $(hki0)$ $(ihk0)$ $(kih0)$ $(khi0)$ $(hik0)$ $(ikh0)$ $(\bar{h}k\bar{i}0)$ $(\bar{i}h\bar{k}0)$ $(\bar{k}\bar{i}\bar{h}0)$ $(\bar{k}\bar{h}\bar{i}0)$ $(\bar{h}\bar{i}\bar{k}0)$ $(\bar{i}\bar{k}\bar{h}0)$ $(hh\bar{2}hl)$ $(\bar{2}hhhl)$ $(h\bar{2}hhl)$ $(h\bar{h}\bar{2}h\bar{l})$ $(\bar{h}\bar{2}hh\bar{l})$ $(\bar{2}hh\bar{h}\bar{l})$ $(\bar{h}\bar{h}\bar{2}h\bar{l})$ $(2hh\bar{h}\bar{l})$ $(\bar{h}2h\bar{h}\bar{l})$ $(\bar{h}\bar{h}2hl)$ $(\bar{h}2h\bar{h}l)$ $(2h\bar{h}\bar{h}l)$	
6	<i>c</i>	<i>.m.</i>	x, \bar{x}, z $x, 2x, z$ $2\bar{x}, \bar{x}, z$ \bar{x}, x, \bar{z} $2x, x, \bar{z}$ $\bar{x}, 2\bar{x}, \bar{z}$	Rhombohedron <i>Trigonal antiprism</i> Hexagonal prism <i>Hexagon through origin</i>	$(h0\bar{h}l)$ $(\bar{h}h0l)$ $(0\bar{h}hl)$ $(0h\bar{h}l)$ $(h\bar{h}0l)$ $(h0\bar{h}l)$ $(10\bar{1}0)$ $(\bar{1}100)$ $(0\bar{1}10)$ $(01\bar{1}0)$ $(1\bar{1}00)$ (1010)	
6	<i>b</i>	<i>.2.</i>	$x, 0, 0$ $0, x, 0$ $\bar{x}, \bar{x}, 0$ $\bar{x}, 0, 0$ $0, \bar{x}, 0$ $x, x, 0$	Hexagonal prism <i>Hexagon through origin</i>	$(11\bar{2}0)$ $(\bar{2}110)$ $(1\bar{2}10)$ $(\bar{1}\bar{1}20)$ $(\bar{1}\bar{2}10)$ $(2\bar{1}\bar{1}0)$	
2	<i>a</i>	<i>3m.</i>	$0, 0, z$ $0, 0, \bar{z}$	Pinacoid or parallelohedron <i>Line segment through origin</i>	(0001) $(000\bar{1})$	
1	<i>o</i>	$\bar{3}m.$	$0, 0, 0$	Point in origin		
Symmetry of special projections						
Along [001] Along [100] Along [210] 6mm 2 2mm						

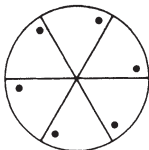
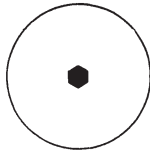
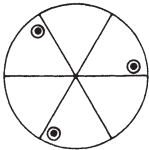
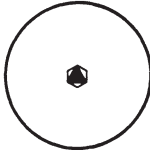
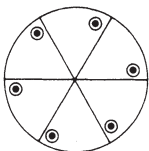
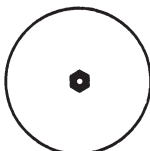
3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

TRIGONAL SYSTEM (<i>cont.</i>)							
$\bar{3}m$							
$\bar{2}$							
$\bar{3}$							
m							
		D_{3d}					
							
RHOMBOHEDRAL AXES							
12	<i>d</i>	1	x, y, z $\bar{z}, \bar{y}, \bar{x}$ $\bar{x}, \bar{y}, \bar{z}$ z, y, x	z, x, y $\bar{y}, \bar{x}, \bar{z}$ $\bar{z}, \bar{x}, \bar{y}$ y, x, z	y, z, x $\bar{x}, \bar{z}, \bar{y}$ $\bar{y}, \bar{z}, \bar{x}$ x, z, y	Ditrigonal scalenohedron or hexagonal scalenohedron Trigonal antiprism sliced off by pinacoid Dihexagonal prism Truncated hexagon through origin Hexagonal dipyramid Hexagonal prism	(hkl) (lhk) (klh) $(\bar{k}\bar{h}\bar{l})$ $(\bar{h}\bar{l}\bar{k})$ $(\bar{l}\bar{k}\bar{h})$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{l}\bar{h}\bar{k})$ $(\bar{k}\bar{l}\bar{h})$ (khl) (hlk) (lkh) $(hk(\bar{h}+\bar{k}))$ $(\bar{h}+\bar{k})hk$ $(k(\bar{h}+\bar{k})h)$ $(\bar{k}\bar{h}(h+k))$ $(\bar{h}(h+k)\bar{k})$ $((h+k)\bar{k}\bar{h})$ $(\bar{h}\bar{k}(h+k))$ $((h+k)\bar{h}\bar{k})$ $(\bar{k}(h+k)\bar{h})$ $(kh(\bar{h}+\bar{k}))$ $(h(\bar{h}+\bar{k})k)$ $((\bar{h}+\bar{k})kh)$ $(hk(2k-h))$ $((2k-h)hk)$ $(k(2k-h)h)$ $(\bar{k}\bar{h}(h-2k))$ $(\bar{h}(h-2k)\bar{k})$ $((h-2k)\bar{k}\bar{h})$ $(\bar{h}\bar{k}(h-2k))$ $((h-2k)\bar{h}\bar{k})$ $(\bar{k}(h-2k)\bar{h})$ $(kh(2k-h))$ $(h(2k-h)k)$ $((2k-h)kh)$
6	<i>c</i>	<i>.m</i>	x, y, x $\bar{x}, \bar{y}, \bar{x}$	x, x, y $\bar{y}, \bar{x}, \bar{x}$	y, x, x $\bar{x}, \bar{x}, \bar{y}$	Rhombohedron Trigonal antiprism Hexagonal prism Hexagon through origin	(hhl) (lhh) (hll) $(\bar{h}\bar{h}\bar{l})$ $(\bar{h}\bar{l}\bar{h})$ $(\bar{l}\bar{h}\bar{h})$ $(11\bar{2})$ $(\bar{2}11)$ $(1\bar{2}1)$ $(\bar{1}\bar{1}2)$ $(\bar{1}\bar{2}1)$ $(2\bar{1}\bar{1})$
6	<i>b</i>	<i>.2</i>	$x, \bar{x}, 0$ $\bar{x}, x, 0$	$0, x, \bar{x}$ $0, \bar{x}, x$	$\bar{x}, 0, x$ $x, 0, \bar{x}$	Hexagonal prism Hexagon through origin	$(01\bar{1})$ $(\bar{1}01)$ $(1\bar{1}0)$ $(0\bar{1}1)$ $(10\bar{1})$ $(\bar{1}10)$
2	<i>a</i>	<i>3m</i>	x, x, x	$\bar{x}, \bar{x}, \bar{x}$		Pinacoid or parallelohedron Line segment through origin	(111) $(\bar{1}\bar{1}\bar{1})$
1	<i>o</i>	$\bar{3}m$	$0, 0, 0$			Point in origin	
Symmetry of special projections							
			Along [111]	Along [1 $\bar{1}$ 0]	Along [2 $\bar{1}\bar{1}$]		
			6mm	2	2mm		

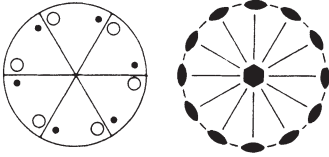
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

HEXAGONAL SYSTEM									
6	b	1	x, y, z \bar{x}, \bar{y}, z	$\bar{y}, x - y, z$ $y, \bar{x} + y, z$	$\bar{x} + y, \bar{x}, z$ $x - y, x, z$	 	Hexagonal pyramid Hexagon Hexagonal prism Hexagon through origin	(hkl) $(ihkl)$ $(kihl)$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ $(hki0)$ $(ihk0)$ $(kih0)$ $(\bar{h}\bar{k}\bar{i}0)$ $(\bar{i}\bar{h}\bar{k}0)$ $(\bar{k}\bar{i}\bar{h}0)$	
									1 a 6.. 0, 0, z Pedion or monohedron Single point
Symmetry of special projections Along [001] Along [100] Along [210] 6 m m									
6	c	1	x, y, z x, y, \bar{z}	$\bar{y}, x - y, z$ $\bar{y}, x - y, \bar{z}$	$\bar{x} + y, \bar{x}, z$ $\bar{x} + y, \bar{x}, \bar{z}$	 	Trigonal dipyrmaid Trigonal prism Trigonal prism Trigon through origin	(hkl) $(ihkl)$ $(kihl)$ $(h\bar{k}\bar{l})$ $(i\bar{h}\bar{k}\bar{l})$ $(k\bar{i}\bar{h}\bar{l})$ $(hki0)$ $(ihk0)$ $(kih0)$	
									3 b m.. $x, y, 0$ $\bar{y}, x - y, 0$ $\bar{x} + y, \bar{x}, 0$ Pinacoid or parallelohedron Line segment through origin
2	a	3..	0, 0, z	0, 0, \bar{z}			Pinacoid or parallelohedron Line segment through origin	(0001) $(000\bar{1})$	
1	o	6..	0, 0, 0				Point in origin		
Symmetry of special projections Along [001] Along [100] Along [210] 3 m m									
6/m	b	m..	x, y, z \bar{x}, \bar{y}, z $\bar{x}, \bar{y}, \bar{z}$ x, y, \bar{z}	$\bar{y}, x - y, z$ $y, \bar{x} + y, z$ $y, \bar{x} + y, \bar{z}$ $\bar{y}, x - y, \bar{z}$	$\bar{x} + y, \bar{x}, z$ $x - y, x, z$ $x - y, x, \bar{z}$ $\bar{x} + y, \bar{x}, \bar{z}$	 	Hexagonal dipyrmaid Hexagonal prism Hexagonal prism Hexagon through origin	(hkl) $(ihkl)$ $(kihl)$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ $(h\bar{k}\bar{l})$ $(i\bar{h}\bar{k}\bar{l})$ $(k\bar{i}\bar{h}\bar{l})$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$	
									6 b m.. $x, y, 0$ $\bar{y}, x - y, 0$ $\bar{x} + y, \bar{x}, 0$ $\bar{x}, \bar{y}, 0$ $y, \bar{x} + y, 0$ $x - y, x, 0$ Pinacoid or parallelohedron Line segment through origin
2	a	6..	0, 0, z	0, 0, \bar{z}			Pinacoid or parallelohedron Line segment through origin	(0001) $(000\bar{1})$	
1	o	6/m..	0, 0, 0				Point in origin		
Symmetry of special projections Along [001] Along [100] Along [210] 6 2mm 2mm									

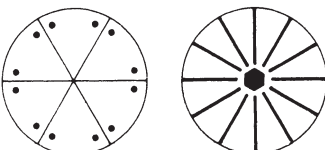
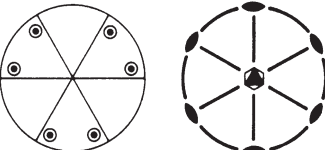
3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

HEXAGONAL SYSTEM (<i>cont.</i>)						
622	D_6					
12	<i>d</i>	1	x, y, z $\bar{y}, x - y, z$ $\bar{x} + y, \bar{x}, z$ \bar{x}, \bar{y}, z $y, \bar{x} + y, z$ $x - y, x, z$ y, x, \bar{z} $x - y, \bar{y}, \bar{z}$ $\bar{x}, \bar{x} + y, \bar{z}$ $\bar{y}, \bar{x}, \bar{z}$ $\bar{x} + y, y, \bar{z}$ $x, x - y, \bar{z}$	Hexagonal trapezohedron Twisted hexagonal antiprism	(hkl) $(ihkl)$ $(kihl)$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ $(kh\bar{l})$ $(hik\bar{l})$ $(ikh\bar{l})$ $(k\bar{h}\bar{l})$ $(\bar{h}i\bar{k}\bar{l})$ $(\bar{i}k\bar{h}\bar{l})$	
				Dihexagonal prism Truncated hexagon through origin	$(hki0)$ $(ihk0)$ $(kih0)$ $(\bar{h}\bar{k}\bar{i}0)$ $(\bar{i}\bar{h}\bar{k}0)$ $(\bar{k}\bar{i}\bar{h}0)$ $(khi0)$ $(hik0)$ $(ikh0)$ $(\bar{k}\bar{h}\bar{i}0)$ $(\bar{h}\bar{i}\bar{k}0)$ $(\bar{i}\bar{k}\bar{h}0)$	
				Hexagonal dipyramid Hexagonal prism	$(h0hl)$ $(\bar{h}0hl)$ $(0\bar{h}hl)$ $(h0hl)$ $(h\bar{h}0l)$ $(0hhl)$ $(0hhl)$ $(h\bar{h}0l)$ $(h0hl)$ $(0\bar{h}hl)$ $(\bar{h}h0l)$ $(h0\bar{h}l)$	
				Hexagonal dipyramid Hexagonal prism	$(hh\bar{2}hl)$ $(\bar{2}hhhl)$ $(h\bar{2}hhl)$ $(\bar{h}\bar{h}2hl)$ $(2hh\bar{h}l)$ $(\bar{h}2h\bar{h}l)$ $(hh\bar{2}hl)$ $(h\bar{2}hhl)$ $(\bar{2}hhhl)$ $(\bar{h}\bar{h}2hl)$ $(\bar{h}2h\bar{h}l)$ $(2h\bar{h}\bar{h}l)$	
6	<i>c</i>	.2	$x, \bar{x}, 0$ $x, 2x, 0$ $2\bar{x}, \bar{x}, 0$ $\bar{x}, x, 0$ $\bar{x}, 2\bar{x}, 0$ $2x, x, 0$	Hexagonal prism Hexagon through origin	$(10\bar{1}0)$ $(\bar{1}100)$ $(0\bar{1}10)$ $(\bar{1}010)$ $(\bar{1}\bar{1}00)$ $(01\bar{1}0)$	
6	<i>b</i>	.2	$x, 0, 0$ $0, x, 0$ $\bar{x}, \bar{x}, 0$ $\bar{x}, 0, 0$ $0, \bar{x}, 0$ $x, x, 0$	Hexagonal prism Hexagon through origin	$(11\bar{2}0)$ $(\bar{2}110)$ $(\bar{1}210)$ $(\bar{1}\bar{1}20)$ $(\bar{2}\bar{1}\bar{1}0)$ $(\bar{1}2\bar{1}0)$	
2	<i>a</i>	6.	$0, 0, z$ $0, 0, \bar{z}$	Pinacoid or parallelohedron Line segment through origin	(0001) $(000\bar{1})$	
1	<i>o</i>	622	$0, 0, 0$	Point in origin		
				Symmetry of special projections		
				Along [001]	Along [100]	Along [210]
				<i>6mm</i>	<i>2mm</i>	<i>2mm</i>

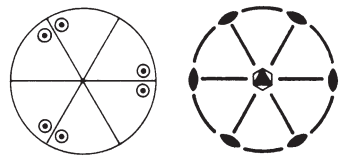
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

HEXAGONAL SYSTEM (<i>cont.</i>)									
$6mm$	C_{6v}								
12	d	1	x, y, z $\bar{y}, x - y, z$ $\bar{x} + y, \bar{x}, z$ \bar{x}, \bar{y}, z $y, \bar{x} + y, z$ $x - y, x, z$ \bar{y}, \bar{x}, z $\bar{x} + y, y, z$ $x, x - y, z$ y, x, z $x - y, \bar{y}, z$ $\bar{x}, \bar{x} + y, z$	Dihexagonal pyramid Truncated hexagon	(hkl) $(ihkl)$ $(kihl)$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ (khl) $(hikl)$ $(ikh\bar{l})$ $(\bar{k}\bar{h}\bar{l})$ $(\bar{h}\bar{i}\bar{k}\bar{l})$ $(\bar{i}\bar{k}\bar{h}\bar{l})$				
				Dihexagonal prism Truncated hexagon through origin	$(hki0)$ $(ihk0)$ $(kih0)$ $(\bar{h}\bar{k}\bar{i}0)$ $(\bar{i}\bar{h}\bar{k}0)$ $(\bar{k}\bar{i}\bar{h}0)$ $(khi0)$ $(hik0)$ $(ikh0)$ $(\bar{k}\bar{h}\bar{i}0)$ $(\bar{h}\bar{i}\bar{k}0)$ $(\bar{i}\bar{k}\bar{h}0)$				
6	c	$.m$	x, \bar{x}, z $x, 2x, z$ $2\bar{x}, \bar{x}, z$ \bar{x}, x, z $\bar{x}, 2\bar{x}, z$ $2x, x, z$	Hexagonal pyramid Hexagon	$(h0\bar{h}l)$ $(\bar{h}h0l)$ $(0\bar{h}hl)$ $(\bar{h}0hl)$ $(hh0l)$ $(0hhl)$				
				Hexagonal prism Hexagon through origin	$(10\bar{1}0)$ $(\bar{1}100)$ $(0\bar{1}10)$ $(\bar{1}010)$ (1100) $(01\bar{1}0)$				
6	b	$.m$	$x, 0, z$ $0, x, z$ \bar{x}, \bar{x}, z $\bar{x}, 0, z$ $0, \bar{x}, z$ x, x, z	Hexagonal pyramid Hexagon	$(hh\bar{2}hl)$ $(\bar{2}hhhl)$ $(h\bar{2}hhl)$ $(\bar{h}\bar{h}2hl)$ $(2h\bar{h}\bar{h}l)$ $(\bar{h}2h\bar{h}l)$				
				Hexagonal prism Hexagon through origin	$(11\bar{2}0)$ $(\bar{2}210)$ $(1\bar{2}10)$ $(\bar{1}\bar{1}20)$ $(2\bar{1}\bar{1}0)$ $(12\bar{1}0)$				
1	a	$6mm$	$0, 0, z$	Pedion or monohedron Single point	(0001) or $(000\bar{1})$				
Symmetry of special projections									
Along [001] Along [100] Along [210]									
$6mm$ m m									
$\bar{6}m2$	D_{3h}								
12	e	1	x, y, z $\bar{y}, x - y, z$ $\bar{x} + y, \bar{x}, z$ x, y, \bar{z} $\bar{y}, x - y, \bar{z}$ $\bar{x} + y, \bar{x}, \bar{z}$ \bar{y}, \bar{x}, z $\bar{x} + y, y, z$ $x, x - y, z$ $\bar{y}, \bar{x}, \bar{z}$ $\bar{x} + y, y, \bar{z}$ $x, x - y, \bar{z}$	Ditrigonal dipyramid Edge-truncated trigonal prism	(hkl) $(ihkl)$ $(kihl)$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ (khl) $(hikl)$ $(ikh\bar{l})$ $(\bar{k}\bar{h}\bar{l})$ $(\bar{h}\bar{i}\bar{k}\bar{l})$ $(\bar{i}\bar{k}\bar{h}\bar{l})$				
				Hexagonal dipyramid Hexagonal prism	$(hh\bar{2}hl)$ $(\bar{2}hhhl)$ $(h\bar{2}hhl)$ $(\bar{h}\bar{h}2\bar{h}\bar{l})$ $(\bar{2}\bar{h}\bar{h}\bar{h}\bar{l})$ $(h\bar{2}\bar{h}\bar{h}\bar{l})$ $(\bar{h}\bar{h}2hl)$ $(\bar{h}2h\bar{h}l)$ $(2h\bar{h}\bar{h}l)$ $(\bar{h}\bar{h}2hl)$ $(\bar{h}2h\bar{h}l)$ $(2h\bar{h}\bar{h}l)$				
6	d	$.m$	$x, y, 0$ $\bar{y}, x - y, 0$ $\bar{x} + y, \bar{x}, 0$ $\bar{y}, \bar{x}, 0$ $\bar{x} + y, y, 0$ $x, x - y, 0$	Ditrigonal prism Truncated trigon through origin	$(hki0)$ $(ihk0)$ $(kih0)$ $(\bar{k}\bar{h}\bar{i}0)$ $(\bar{h}\bar{i}\bar{k}0)$ $(\bar{i}\bar{k}\bar{h}0)$				
				Hexagonal prism Hexagon through origin	$(11\bar{2}0)$ $(\bar{2}210)$ $(1\bar{2}10)$ $(\bar{1}\bar{1}20)$ $(\bar{1}2\bar{1}0)$ $(2\bar{1}\bar{1}0)$				
6	c	$.m$	x, \bar{x}, z $x, 2x, z$ $2\bar{x}, \bar{x}, z$ x, \bar{x}, \bar{z} $x, 2x, \bar{z}$ $2\bar{x}, \bar{x}, \bar{z}$	Trigonal dipyramid Trigonal prism	$(h0\bar{h}l)$ $(\bar{h}h0l)$ $(0\bar{h}hl)$ $(\bar{h}0\bar{h}l)$ $(\bar{h}h0l)$ $(0hhl)$				
3	b	$mm2$	$x, \bar{x}, 0$ $x, 2x, 0$ $2\bar{x}, \bar{x}, 0$	Trigonal prism Trigon through origin	$(10\bar{1}0)$ $(\bar{1}100)$ $(0\bar{1}10)$ or (1010) $(1\bar{1}00)$ $(01\bar{1}0)$				
2	a	$3m$	$0, 0, z$ $0, 0, \bar{z}$	Pinacoid or parallelohedron Line segment through origin	(0001) $(000\bar{1})$				
1	o	$\bar{6}m2$	$0, 0, 0$	Point in origin					
Symmetry of special projections									
Along [001] Along [100] Along [210]									
$3m$ m $2mm$									

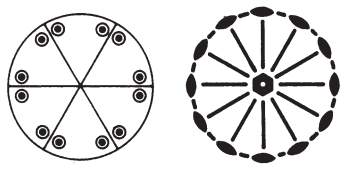
3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

HEXAGONAL SYSTEM (<i>cont.</i>)									
$\bar{6}2m$		D_{3h}							
12	<i>e</i>	1	x, y, z x, y, \bar{z} y, x, \bar{z} y, x, z	$\bar{y}, x - y, z$ $\bar{y}, x - y, \bar{z}$ $x - y, \bar{y}, \bar{z}$ $x - y, \bar{y}, z$	$\bar{x} + y, \bar{x}, z$ $\bar{x} + y, \bar{x}, \bar{z}$ $\bar{x}, \bar{x} + y, \bar{z}$ $\bar{x}, \bar{x} + y, z$	Ditrigonal dipyramid Edge-truncated trigonal prism	$(hki\bar{l})$ $(hk\bar{i}l)$ $(kh\bar{i}l)$ $(khi\bar{l})$	$(ihkl)$ $(ihk\bar{l})$ $(hik\bar{l})$ $(hikl)$	$(kihl)$ $(kih\bar{l})$ $(ikh\bar{l})$ $(ikh\bar{l})$
						Hexagonal dipyramid Hexagonal prism	$(h0\bar{h}l)$ $(h0\bar{h}\bar{l})$ $(0h\bar{h}l)$ $(0h\bar{h}\bar{l})$	$(\bar{h}h0l)$ $(\bar{h}h0\bar{l})$ $(h\bar{h}0l)$ $(h\bar{h}0\bar{l})$	$(0\bar{h}hl)$ $(0\bar{h}h\bar{l})$ $(\bar{h}0hl)$ $(\bar{h}0h\bar{l})$
6	<i>d</i>	<i>m.</i>	$x, y, 0$ $y, x, 0$	$\bar{y}, x - y, 0$ $x - y, \bar{y}, 0$	$\bar{x} + y, \bar{x}, 0$ $\bar{x}, \bar{x} + y, 0$	Ditrigonal prism Truncated trigon through origin	$(hki0)$ $(khi0)$	$(ihk0)$ $(hik0)$	$(kih0)$ $(ikh0)$
						Hexagonal prism Hexagon through origin	$(10\bar{1}0)$ $(01\bar{1}0)$	$(\bar{1}100)$ $(1\bar{1}00)$	$(0\bar{1}10)$ $(\bar{1}010)$
6	<i>c</i>	<i>.m</i>	$x, 0, z$ $x, 0, \bar{z}$	$0, x, z$ $0, x, \bar{z}$	\bar{x}, \bar{x}, z $\bar{x}, \bar{x}, \bar{z}$	Trigonal dipyramid Trigonal prism	$(hh\bar{2}hl)$ $(hh\bar{2}h\bar{l})$	$(\bar{2}hhhl)$ $(\bar{2}hhh\bar{l})$	$(h\bar{2}hhl)$ $(h\bar{2}hh\bar{l})$
3	<i>b</i>	<i>m2m</i>	$x, 0, 0$	$0, x, 0$	$\bar{x}, \bar{x}, 0$	Trigonal prism Trigon through origin	$(11\bar{2}0)$ or $(\bar{1}\bar{1}20)$	$(\bar{2}110)$ $(2\bar{1}\bar{1}0)$	$(1\bar{2}10)$ $(\bar{1}2\bar{1}0)$
2	<i>a</i>	<i>3.m</i>	$0, 0, z$	$0, 0, \bar{z}$		Pinacoid or parallelohedron Line segment through origin	(0001)	$(000\bar{1})$	
1	<i>o</i>	$\bar{6}2m$	$0, 0, 0$			Point in origin			
Symmetry of special projections									
Along [001] Along [100] Along [210]									
$3m$ $2mm$ m									

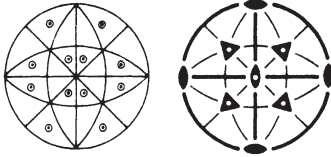
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

HEXAGONAL SYSTEM (<i>cont.</i>)					
$6/mmm$					
$\frac{6}{m} \frac{2}{m} \frac{2}{m}$	D_{6h}				
24	<i>g</i>	1	x, y, z $\bar{y}, x - y, z$ $\bar{x} + y, \bar{x}, z$ \bar{x}, \bar{y}, z $y, \bar{x} + y, z$ $x - y, x, z$ y, x, \bar{z} $x - y, \bar{y}, \bar{z}$ $\bar{x}, \bar{x} + y, \bar{z}$ $\bar{y}, \bar{x}, \bar{z}$ $\bar{x} + y, y, \bar{z}$ $x, x - y, \bar{z}$	Dihexagonal dipyrmaid Edge-truncated hexagonal prism	(hkl) $(ihkl)$ $(kihl)$ $(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ $(k\bar{h}\bar{l})$ $(h\bar{k}\bar{l})$ $(i\bar{k}\bar{h}\bar{l})$ $(\bar{k}\bar{h}\bar{l})$ $(\bar{h}\bar{i}\bar{k}\bar{l})$ $(\bar{i}\bar{k}\bar{h}\bar{l})$
			$\bar{x}, \bar{y}, \bar{z}$ $y, \bar{x} + y, \bar{z}$ $x - y, x, \bar{z}$ x, y, \bar{z} $\bar{y}, x - y, \bar{z}$ $\bar{x} + y, \bar{x}, \bar{z}$ \bar{y}, \bar{x}, z $\bar{x} + y, y, z$ $x, x - y, z$ y, x, z $x - y, \bar{y}, z$ $\bar{x}, \bar{x} + y, z$		$(\bar{h}\bar{k}\bar{l})$ $(\bar{i}\bar{h}\bar{k}\bar{l})$ $(\bar{k}\bar{i}\bar{h}\bar{l})$ $(h\bar{k}\bar{l})$ $(ih\bar{k}\bar{l})$ $(ki\bar{h}\bar{l})$ $(\bar{k}\bar{h}\bar{l})$ $(\bar{h}\bar{i}\bar{k}\bar{l})$ $(\bar{i}\bar{k}\bar{h}\bar{l})$ $(k\bar{h}\bar{l})$ $(h\bar{k}\bar{l})$ $(i\bar{k}\bar{h}\bar{l})$
12	<i>f</i>	<i>m.</i>	$x, y, 0$ $\bar{y}, x - y, 0$ $\bar{x} + y, \bar{x}, 0$ $\bar{x}, \bar{y}, 0$ $y, \bar{x} + y, 0$ $x - y, x, 0$ $y, x, 0$ $x - y, \bar{y}, 0$ $\bar{x}, \bar{x} + y, 0$ $\bar{y}, \bar{x}, 0$ $\bar{x} + y, y, 0$ $x, x - y, 0$	Dihexagonal prism Truncated hexagon through origin	$(hki0)$ $(ihk0)$ $(kih0)$ $(\bar{h}\bar{k}\bar{i}0)$ $(\bar{i}\bar{h}\bar{k}0)$ $(\bar{k}\bar{i}\bar{h}0)$ $(k\bar{h}\bar{i}0)$ $(h\bar{k}\bar{i}0)$ $(i\bar{k}\bar{h}0)$ $(\bar{k}\bar{h}\bar{i}0)$ $(\bar{h}\bar{i}\bar{k}0)$ $(\bar{i}\bar{k}\bar{h}0)$
12	<i>e</i>	<i>.m.</i>	$x, 2x, z$ $2\bar{x}, \bar{x}, z$ x, \bar{x}, z $\bar{x}, 2\bar{x}, z$ $2x, x, z$ \bar{x}, x, z $2x, x, \bar{z}$ $\bar{x}, 2\bar{x}, \bar{z}$ \bar{x}, x, \bar{z} $2\bar{x}, \bar{x}, \bar{z}$ $x, 2x, \bar{z}$ x, \bar{x}, \bar{z}	Hexagonal dipyrmaid Hexagonal prism	$(h0\bar{h}l)$ $(\bar{h}h0l)$ $(0\bar{h}hl)$ $(h0hl)$ $(h\bar{h}0l)$ $(0hhl)$ $(0h\bar{h}l)$ $(h\bar{h}0l)$ $(\bar{h}0hl)$ $(0hhl)$ $(\bar{h}h0l)$ $(h0\bar{h}l)$
12	<i>d</i>	<i>.m</i>	$x, 0, z$ $0, x, z$ \bar{x}, \bar{x}, z $\bar{x}, 0, z$ $0, \bar{x}, z$ x, x, z $0, x, \bar{z}$ $x, 0, \bar{z}$ $\bar{x}, \bar{x}, \bar{z}$ $0, \bar{x}, \bar{z}$ $\bar{x}, 0, \bar{z}$ x, x, \bar{z}	Hexagonal dipyrmaid Hexagonal prism	$(hh2\bar{h}l)$ $(\bar{2}hhhl)$ $(h\bar{2}hhhl)$ $(\bar{h}h2hl)$ $(2hhhl)$ $(h2hhhl)$ $(hh2\bar{h}l)$ $(h\bar{2}hhhl)$ $(2hhhl)$ $(\bar{h}h2hl)$ $(\bar{h}2hhhl)$ $(2hhhl)$
6	<i>c</i>	<i>mm2</i>	$x, 2x, 0$ $2\bar{x}, \bar{x}, 0$ $x, \bar{x}, 0$ $\bar{x}, 2\bar{x}, 0$ $2x, x, 0$ $\bar{x}, x, 0$	Hexagonal prism Hexagon through origin	$(10\bar{1}0)$ $(\bar{1}100)$ $(0\bar{1}10)$ $(\bar{1}010)$ $(1\bar{1}00)$ $(01\bar{1}0)$
6	<i>b</i>	<i>m2m</i>	$x, 0, 0$ $0, x, 0$ $\bar{x}, \bar{x}, 0$ $\bar{x}, 0, 0$ $0, \bar{x}, 0$ $x, x, 0$	Hexagonal prism Hexagon through origin	$(11\bar{2}0)$ $(\bar{2}110)$ $(1\bar{2}10)$ $(\bar{1}120)$ $(2\bar{1}\bar{1}0)$ $(\bar{1}2\bar{1}0)$
2	<i>a</i>	<i>6mm</i>	$0, 0, z$ $0, 0, \bar{z}$	Pinacoid or parallelohedron Line segment through origin	(0001) $(000\bar{1})$
1	<i>o</i>	<i>6mmm</i>	$0, 0, 0$	Point in origin	
Symmetry of special projections					
		Along [001]	Along [100]	Along [210]	
		6mm	2mm	2mm	

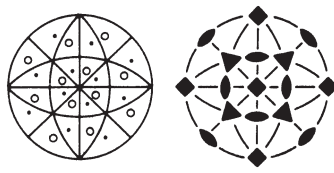
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

CUBIC SYSTEM (cont.)						
$m\bar{3}$	T_h					
$\frac{2}{m}$						
m						
24	d	1	x, y, z \bar{x}, \bar{y}, z \bar{x}, y, \bar{z} x, \bar{y}, \bar{z} z, x, y z, \bar{x}, \bar{y} \bar{z}, \bar{x}, y \bar{z}, x, \bar{y} y, z, x \bar{y}, z, \bar{x} y, \bar{z}, \bar{x} \bar{y}, \bar{z}, x $\bar{x}, \bar{y}, \bar{z}$ x, y, \bar{z} x, \bar{y}, z \bar{x}, y, z $\bar{z}, \bar{x}, \bar{y}$ \bar{z}, x, y z, x, \bar{y} z, \bar{x}, y $\bar{y}, \bar{z}, \bar{x}$ \bar{y}, \bar{z}, x \bar{y}, z, x y, z, \bar{x}	Didodecahedron or diploid or dyakisdodecahedron Cube & octahedron & pentagon-dodecahedron	(hkl) $(\bar{h}\bar{k}l)$ $(\bar{h}k\bar{l})$ $(h\bar{k}\bar{l})$ (lhk) $(l\bar{h}\bar{k})$ $(l\bar{h}k)$ $(l\bar{h}\bar{k})$ (klh) $(k\bar{l}h)$ $(k\bar{l}\bar{h})$ $(kl\bar{h})$ $(\bar{h}\bar{k}l)$ $(h\bar{k}l)$ $(h\bar{k}\bar{l})$ $(\bar{h}kl)$ $(l\bar{h}k)$ $(l\bar{h}\bar{k})$ $(lh\bar{k})$ $(l\bar{h}k)$ $(k\bar{l}h)$ $(k\bar{l}\bar{h})$ $(kl\bar{h})$ $(kl\bar{h})$	
			{ Tetragon-trioctahedron or trapezohedron or deltoid-icositetrahedron (for $ h < l $) Cube & octahedron & rhomb- dodecahedron (for $ x < z $) Trigon-trioctahedron or trisoctahedron (for $ h > l $) Cube truncated by octahedron (for $ x > z $)	(hhl) $(\bar{h}\bar{h}l)$ $(\bar{h}hl)$ $(h\bar{h}l)$ (lhh) $(l\bar{h}\bar{h})$ $(l\bar{h}h)$ $(l\bar{h}h)$ (hlh) $(\bar{h}l\bar{h})$ $(\bar{h}lh)$ $(\bar{h}lh)$ $(\bar{h}\bar{h}l)$ $(h\bar{h}l)$ $(\bar{h}hl)$ $(\bar{h}hl)$ $(l\bar{h}h)$ $(l\bar{h}h)$ $(lh\bar{h})$ $(l\bar{h}h)$ $(h\bar{h}l)$ $(h\bar{h}l)$ $(\bar{h}lh)$ $(\bar{h}lh)$		
12	c	m..	$0, y, z$ $0, \bar{y}, z$ $0, y, \bar{z}$ $0, \bar{y}, \bar{z}$ $z, 0, y$ $z, 0, \bar{y}$ $\bar{z}, 0, y$ $\bar{z}, 0, \bar{y}$ $y, z, 0$ $\bar{y}, z, 0$ $y, \bar{z}, 0$ $\bar{y}, \bar{z}, 0$	Pentagon-dodecahedron or dihexahedron or pyritohedron Irregular icosahedron (= pentagon-dodecahedron + octahedron)	$(0kl)$ $(0\bar{k}l)$ $(0k\bar{l})$ $(0\bar{k}\bar{l})$ $(l0k)$ $(l0\bar{k})$ $(l0k)$ $(l0\bar{k})$ $(k\bar{l}0)$ $(\bar{k}l0)$ $(k\bar{l}0)$ $(\bar{k}l0)$	
			Rhomb-dodecahedron Cuboctahedron	(011) $(0\bar{1}\bar{1})$ $(01\bar{1})$ $(0\bar{1}\bar{1})$ (101) $(10\bar{1})$ (101) $(10\bar{1})$ (110) $(1\bar{1}0)$ (110) $(1\bar{1}0)$		
8	b	.3.	x, x, x \bar{x}, \bar{x}, x \bar{x}, x, \bar{x} x, \bar{x}, \bar{x} $\bar{x}, \bar{x}, \bar{x}$ x, x, \bar{x} x, \bar{x}, x \bar{x}, x, x	Octahedron Cube	(111) $(\bar{1}\bar{1}\bar{1})$ $(\bar{1}\bar{1}\bar{1})$ $(\bar{1}\bar{1}\bar{1})$ $(\bar{1}\bar{1}\bar{1})$ (111) (111) (111)	
6	a	2mm..	$x, 0, 0$ $\bar{x}, 0, 0$ $0, x, 0$ $0, \bar{x}, 0$ $0, 0, x$ $0, 0, \bar{x}$	Cube or hexahedron Octahedron	(100) $(\bar{1}00)$ (010) $(0\bar{1}0)$ (001) $(00\bar{1})$	
1	o	$m\bar{3}$.	$0, 0, 0$	Point in origin		
Symmetry of special projections						
Along [001] Along [111] Along [110]						
$2mm$ 6 $2mm$						

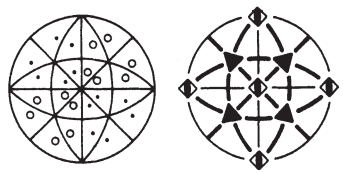
3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

CUBIC SYSTEM (cont.)							
432		<i>O</i>					
24	<i>d</i>	1	x, y, z \bar{x}, \bar{y}, z \bar{x}, y, \bar{z} x, \bar{y}, \bar{z} z, x, y z, \bar{x}, \bar{y} \bar{z}, \bar{x}, y \bar{z}, x, \bar{y} y, z, x \bar{y}, z, \bar{x} y, \bar{z}, \bar{x} \bar{y}, \bar{z}, x y, x, \bar{z} $\bar{y}, \bar{x}, \bar{z}$ y, \bar{x}, z \bar{y}, x, z x, z, \bar{y} \bar{x}, z, y $\bar{x}, \bar{z}, \bar{y}$ x, \bar{z}, y z, y, \bar{x} \bar{z}, \bar{y}, x \bar{z}, y, x $\bar{z}, \bar{y}, \bar{x}$	Pentagon-tri octahedron or gyroid or pentagon-icositetrahedron <i>Snub cube</i> (= cube + octahedron + pentagon- tri octahedron)	(hkl) $(\bar{h}\bar{k}l)$ $(\bar{h}k\bar{l})$ $(h\bar{k}\bar{l})$ (lhk) $(\bar{l}\bar{h}k)$ $(\bar{l}hk)$ $(l\bar{h}k)$ (klh) $(\bar{k}\bar{l}h)$ $(\bar{k}lh)$ $(k\bar{l}h)$ $(kh\bar{l})$ $(\bar{k}\bar{h}\bar{l})$ $(\bar{k}h\bar{l})$ $(k\bar{h}\bar{l})$ $(h\bar{l}k)$ $(\bar{h}\bar{l}k)$ $(\bar{h}l\bar{k})$ $(h\bar{l}k)$ $(l\bar{k}h)$ $(\bar{l}k\bar{h})$ $(\bar{l}kh)$ $(l\bar{k}h)$		
			{ Tetragon-tri octahedron or trapezohedron or deltoid-icositetrahedron (for $ h < l $) <i>Cube & octahedron &</i> <i>rhomb-dodecahedron</i> (for $ x < z $) Trigon-tri octahedron or trisoctahedron (for $ h > l $) <i>Cube truncated by octahedron</i> (for $ x > z $)	(hhl) $(\bar{h}\bar{h}l)$ $(\bar{h}h\bar{l})$ $(h\bar{h}\bar{l})$ (lhh) $(\bar{l}\bar{l}h)$ $(\bar{l}lh)$ $(l\bar{l}h)$ $(h\bar{l}h)$ $(\bar{h}\bar{l}h)$ $(\bar{h}l\bar{h})$ $(h\bar{l}h)$ $(h\bar{h}\bar{l})$ $(\bar{h}\bar{h}\bar{l})$ $(\bar{h}h\bar{l})$ $(h\bar{h}l)$ $(h\bar{l}h)$ $(\bar{h}\bar{l}h)$ $(\bar{h}l\bar{h})$ $(h\bar{l}h)$ $(l\bar{h}h)$ $(\bar{l}h\bar{h})$ $(\bar{l}hh)$ $(l\bar{h}h)$			
				$(0kl)$ $(0\bar{k}l)$ $(0k\bar{l})$ $(0\bar{k}\bar{l})$ $(l0k)$ $(\bar{l}0k)$ $(l0\bar{k})$ $(\bar{l}0\bar{k})$ $(k\bar{l}0)$ $(\bar{k}l0)$ $(k\bar{l}0)$ $(\bar{k}l0)$ Tetrahexahedron or tetrakis hexahedron <i>Octahedron truncated by cube</i>	$(k0\bar{l})$ $(\bar{k}0\bar{l})$ $(k0l)$ $(\bar{k}0l)$ $(0l\bar{k})$ $(0lk)$ $(0\bar{l}k)$ $(0lk)$ $(lk0)$ $(\bar{l}k0)$ $(lk0)$ $(\bar{l}k0)$		
12	<i>c</i>	.2	$0, y, y$ $0, \bar{y}, y$ $0, y, \bar{y}$ $0, \bar{y}, \bar{y}$ $y, 0, y$ $y, 0, \bar{y}$ $\bar{y}, 0, y$ $\bar{y}, 0, \bar{y}$ $y, y, 0$ $\bar{y}, y, 0$ $y, \bar{y}, 0$ $\bar{y}, \bar{y}, 0$	Rhomb-dodecahedron <i>Cuboctahedron</i>	(011) $(0\bar{1}\bar{1})$ $(01\bar{1})$ $(0\bar{1}\bar{1})$ (101) $(10\bar{1})$ $(\bar{1}01)$ $(\bar{1}0\bar{1})$ (110) $(\bar{1}\bar{1}0)$ $(1\bar{1}0)$ $(\bar{1}\bar{1}0)$		
8	<i>b</i>	.3	x, x, x \bar{x}, \bar{x}, x \bar{x}, x, \bar{x} x, \bar{x}, \bar{x} x, x, \bar{x} $\bar{x}, \bar{x}, \bar{x}$ x, \bar{x}, x \bar{x}, x, x	Octahedron <i>Cube</i>	(111) $(\bar{1}\bar{1}\bar{1})$ $(\bar{1}\bar{1}1)$ $(1\bar{1}\bar{1})$ $(1\bar{1}\bar{1})$ $(\bar{1}\bar{1}1)$ $(\bar{1}11)$ $(11\bar{1})$		
6	<i>a</i>	4.	$x, 0, 0$ $\bar{x}, 0, 0$ $0, x, 0$ $0, \bar{x}, 0$ $0, 0, x$ $0, 0, \bar{x}$	Cube or hexahedron <i>Octahedron</i>	(100) $(\bar{1}00)$ (010) $(0\bar{1}0)$ (001) $(00\bar{1})$		
1	<i>o</i>	432	0, 0, 0	Point in origin			
				Symmetry of special projections			
				Along [001]	Along [111]	Along [110]	
				4mm	3m	2mm	

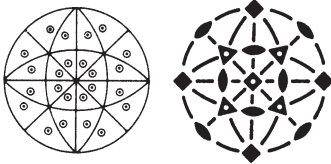
3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.2 (continued)

CUBIC SYSTEM (cont.)			
$\bar{4}3m$	T_d		
24	d	1	<p> x, y, z \bar{x}, \bar{y}, z \bar{x}, y, \bar{z} x, \bar{y}, \bar{z} z, x, y z, \bar{x}, \bar{y} \bar{z}, \bar{x}, y \bar{z}, x, \bar{y} y, z, x \bar{y}, z, \bar{x} y, \bar{z}, \bar{x} \bar{y}, \bar{z}, x </p> <p> y, x, z \bar{y}, \bar{x}, z y, \bar{x}, \bar{z} \bar{y}, x, \bar{z} x, z, y \bar{x}, z, \bar{y} \bar{x}, \bar{z}, y x, \bar{z}, \bar{y} z, y, x z, \bar{y}, \bar{x} \bar{z}, y, \bar{x} \bar{z}, \bar{y}, x </p> <p> Hexatetrahedron or hexakistetrahedron <i>Cube truncated by two tetrahedra</i> </p> <p> (hkl) $(\bar{h}\bar{k}l)$ $(\bar{h}k\bar{l})$ $(h\bar{k}\bar{l})$ (lhk) $(\bar{l}\bar{h}k)$ $(\bar{l}hk)$ $(l\bar{h}\bar{k})$ (klh) $(\bar{k}\bar{l}h)$ $(\bar{k}lh)$ $(k\bar{l}\bar{h})$ </p> <p> (khl) $(\bar{k}\bar{h}l)$ $(\bar{k}h\bar{l})$ $(k\bar{h}\bar{l})$ (hlk) $(\bar{h}\bar{l}k)$ $(\bar{h}lk)$ $(h\bar{l}\bar{k})$ (lkh) $(\bar{l}\bar{k}h)$ $(\bar{l}kh)$ $(l\bar{k}\bar{h})$ </p> <p> $(0kl)$ $(0\bar{k}l)$ $(0k\bar{l})$ $(0\bar{k}\bar{l})$ $(l0k)$ $(l0\bar{k})$ $(\bar{l}0k)$ $(\bar{l}0\bar{k})$ $(k10)$ $(\bar{k}10)$ $(k1\bar{0})$ $(\bar{k}1\bar{0})$ </p> <p> Tetrahexahedron or tetrakisshexahedron <i>Octahedron truncated by cube</i> </p> <p> $(k0l)$ $(\bar{k}0l)$ $(k0\bar{l})$ $(\bar{k}0\bar{l})$ $(0lk)$ $(0l\bar{k})$ $(0\bar{l}k)$ $(0\bar{l}\bar{k})$ $(lk0)$ $(l\bar{k}0)$ $(lk0)$ $(l\bar{k}0)$ </p>
12	c	$.m$	<p> x, x, z \bar{x}, \bar{x}, z \bar{x}, x, \bar{z} x, \bar{x}, \bar{z} z, x, x z, \bar{x}, \bar{x} \bar{z}, \bar{x}, x \bar{z}, x, \bar{x} x, z, x \bar{x}, z, \bar{x} x, \bar{z}, \bar{x} \bar{x}, \bar{z}, x </p> <p> Trigon-tritetrahedron or tristetrahedron (for $h < l$) <i>Tetrahedron truncated by tetrahedron</i> (for $x < z$) </p> <p> Tetragon-tritetrahedron or deltohedron or deltoid-dodecahedron (for $h > l$) <i>Cube & two tetrahedra</i> (for $x > z$) </p> <p> (hhl) $(\bar{h}\bar{h}l)$ $(\bar{h}h\bar{l})$ $(h\bar{h}\bar{l})$ (lhh) $(\bar{l}\bar{h}h)$ $(\bar{l}h\bar{h})$ $(l\bar{h}\bar{h})$ $(h\bar{h}l)$ $(\bar{h}h\bar{l})$ $(\bar{h}\bar{h}l)$ $(h\bar{h}l)$ </p> <p> Rhomb-dodecahedron <i>Cuboctahedron</i> </p> <p> (110) $(\bar{1}\bar{1}0)$ $(\bar{1}10)$ $(1\bar{1}0)$ (011) $(0\bar{1}\bar{1})$ $(0\bar{1}1)$ $(01\bar{1})$ (101) $(\bar{1}0\bar{1})$ $(10\bar{1})$ $(\bar{1}01)$ </p>
6	b	$2.mm$	<p> $x, 0, 0$ $\bar{x}, 0, 0$ $0, x, 0$ $0, \bar{x}, 0$ $0, 0, x$ $0, 0, \bar{x}$ </p> <p> Cube or hexahedron <i>Octahedron</i> </p> <p> (100) $(\bar{1}00)$ (010) $(0\bar{1}0)$ (001) $(00\bar{1})$ </p>
4	a	$.3m$	<p> x, x, x \bar{x}, \bar{x}, x \bar{x}, x, \bar{x} x, \bar{x}, \bar{x} </p> <p> Tetrahedron <i>Tetrahedron</i> </p> <p> (111) $(\bar{1}\bar{1}\bar{1})$ $(\bar{1}\bar{1}1)$ $(1\bar{1}\bar{1})$ or $(\bar{1}\bar{1}\bar{1})$ $(11\bar{1})$ $(1\bar{1}1)$ $(\bar{1}11)$ </p>
1	o	$\bar{4}3m$	<p> $0, 0, 0$ </p> <p> Point in origin </p>
Symmetry of special projections Along [001] Along [111] Along [110] $4mm$ $3m$ m			

3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.2 (continued)

CUBIC SYSTEM (cont.)													
$m\bar{3}m$	O_h												
$\frac{4}{m} \frac{3}{m} \frac{2}{m}$													
48	f	1											
	x, y, z	$\bar{x}, \bar{y}, \bar{z}$	\bar{x}, y, \bar{z}	x, \bar{y}, \bar{z}	Hexaoctahedron or hexakisoctahedron Cube truncated by octahedron and by rhomb- dodecahedron	(hkl)	$(\bar{h}\bar{k}\bar{l})$	$(\bar{h}k\bar{l})$	$(h\bar{k}\bar{l})$				
	z, x, y	$\bar{z}, \bar{x}, \bar{y}$	\bar{z}, x, \bar{y}	\bar{z}, x, \bar{y}		(lhk)	$(\bar{l}\bar{h}\bar{k})$	$(\bar{l}h\bar{k})$	$(l\bar{h}\bar{k})$				
	y, z, x	$\bar{y}, \bar{z}, \bar{x}$	\bar{y}, z, \bar{x}	\bar{y}, z, \bar{x}		(kly)	$(\bar{k}\bar{l}\bar{h})$	$(\bar{k}l\bar{h})$	$(k\bar{l}\bar{h})$				
	y, x, \bar{z}	$\bar{y}, \bar{x}, \bar{z}$	\bar{y}, x, \bar{z}	\bar{y}, x, \bar{z}		$(k\bar{h}\bar{l})$	$(\bar{k}\bar{h}l)$	$(\bar{k}hl)$	(khl)				
	x, z, \bar{y}	$\bar{x}, \bar{z}, \bar{y}$	\bar{x}, z, \bar{y}	\bar{x}, z, \bar{y}		$(h\bar{l}k)$	$(\bar{h}\bar{l}k)$	$(\bar{h}lk)$	$(h\bar{l}k)$				
	z, y, \bar{x}	$\bar{z}, \bar{y}, \bar{x}$	\bar{z}, y, \bar{x}	\bar{z}, y, \bar{x}		$(l\bar{k}h)$	$(\bar{l}\bar{k}h)$	$(\bar{l}kh)$	$(lk\bar{h})$				
	$\bar{x}, \bar{y}, \bar{z}$	x, y, \bar{z}	x, \bar{y}, \bar{z}	x, y, \bar{z}		$(\bar{h}\bar{k}\bar{l})$	$(h\bar{k}\bar{l})$	$(\bar{h}k\bar{l})$	$(\bar{h}\bar{k}l)$				
	$\bar{z}, \bar{x}, \bar{y}$	\bar{z}, x, y	\bar{z}, x, \bar{y}	\bar{z}, x, \bar{y}		$(\bar{l}\bar{h}\bar{k})$	$(l\bar{h}\bar{k})$	$(\bar{l}h\bar{k})$	$(\bar{l}\bar{h}k)$				
	$\bar{y}, \bar{z}, \bar{x}$	\bar{y}, z, x	\bar{y}, z, \bar{x}	\bar{y}, z, \bar{x}		$(\bar{k}\bar{l}\bar{h})$	$(k\bar{l}\bar{h})$	$(\bar{k}l\bar{h})$	$(\bar{k}\bar{l}h)$				
	$\bar{y}, \bar{x}, \bar{z}$	\bar{y}, x, \bar{z}	\bar{y}, x, \bar{z}	\bar{y}, x, \bar{z}		$(\bar{k}\bar{h}\bar{l})$	$(k\bar{h}\bar{l})$	$(\bar{k}h\bar{l})$	$(\bar{k}\bar{h}l)$				
	$\bar{x}, \bar{z}, \bar{y}$	\bar{x}, z, \bar{y}	\bar{x}, z, \bar{y}	\bar{x}, z, \bar{y}		$(\bar{h}\bar{l}k)$	$(h\bar{l}k)$	$(\bar{h}lk)$	$(\bar{h}\bar{l}k)$				
	$\bar{z}, \bar{y}, \bar{x}$	\bar{z}, y, \bar{x}	\bar{z}, y, \bar{x}	\bar{z}, y, \bar{x}		$(\bar{l}\bar{k}h)$	$(lk\bar{h})$	$(\bar{l}kh)$	$(\bar{l}kh)$				
24	e	$.m$	x, x, z	$\bar{x}, \bar{x}, \bar{z}$	\bar{x}, x, \bar{z}	x, \bar{x}, \bar{z}	<div style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 10px;"> Tetragon-trioctahedron or trapezohedron or deltoid-icositetrahedron (for $h < l$) Cube & octahedron & rhomb- dodecahedron (for $x < z$) Trigon-trioctahedron or trisoctahedron (for $h > l$) Cube truncated by octahedron (for $x > z$) </div>			(hhl)	$(\bar{h}\bar{h}l)$	$(\bar{h}hl)$	$(h\bar{h}l)$
			z, x, x	$\bar{z}, \bar{x}, \bar{x}$	\bar{z}, x, \bar{x}	\bar{z}, x, \bar{x}				(lhh)	$(\bar{l}\bar{h}\bar{h})$	$(\bar{l}hh)$	$(l\bar{h}\bar{h})$
			x, z, x	$\bar{x}, \bar{z}, \bar{x}$	x, \bar{z}, \bar{x}	$\bar{x}, \bar{z}, \bar{x}$				(hlh)	$(\bar{h}\bar{l}\bar{h})$	$(\bar{h}lh)$	$(h\bar{l}\bar{h})$
			x, x, \bar{z}	$\bar{x}, \bar{x}, \bar{z}$	x, \bar{x}, \bar{z}	\bar{x}, x, \bar{z}				$(h\bar{h}l)$	$(\bar{h}\bar{h}l)$	$(\bar{h}hl)$	$(h\bar{h}l)$
			x, z, \bar{x}	$\bar{x}, \bar{z}, \bar{x}$	$\bar{x}, \bar{z}, \bar{x}$	x, \bar{z}, \bar{x}				$(hl\bar{h})$	$(\bar{h}l\bar{h})$	$(\bar{h}l\bar{h})$	$(hl\bar{h})$
			z, x, \bar{x}	$\bar{z}, \bar{x}, \bar{x}$	\bar{z}, x, \bar{x}	$\bar{z}, \bar{x}, \bar{x}$				$(lh\bar{h})$	$(\bar{l}h\bar{h})$	$(\bar{l}h\bar{h})$	$(lh\bar{h})$
24	d	$m..$	$0, y, z$	$0, \bar{y}, \bar{z}$	$0, y, \bar{z}$	$0, \bar{y}, \bar{z}$	Tetrahexahedron or tetrakisshexahedron Octahedron truncated by cube	$(0kl)$	$(0\bar{k}\bar{l})$	$(0k\bar{l})$	$(0\bar{k}l)$		
			$z, 0, y$	$\bar{z}, 0, \bar{y}$	$\bar{z}, 0, \bar{y}$	$\bar{z}, 0, \bar{y}$		$(l0k)$	$(\bar{l}0\bar{k})$	$(\bar{l}0k)$	$(l0\bar{k})$		
			$y, z, 0$	$\bar{y}, \bar{z}, 0$	$\bar{y}, z, 0$	$\bar{y}, z, 0$		$(k0l)$	$(\bar{k}0\bar{l})$	$(\bar{k}0l)$	$(k0\bar{l})$		
			$y, 0, \bar{z}$	$\bar{y}, 0, \bar{z}$	$y, 0, \bar{z}$	$\bar{y}, 0, \bar{z}$		$(k0\bar{l})$	$(\bar{k}0l)$	$(k0l)$	$(\bar{k}0\bar{l})$		
			$0, z, \bar{y}$	$0, \bar{z}, \bar{y}$	$0, \bar{z}, \bar{y}$	$0, \bar{z}, \bar{y}$		$(0lk)$	$(0\bar{l}\bar{k})$	$(0lk)$	$(0\bar{l}k)$		
			$z, y, 0$	$\bar{z}, \bar{y}, 0$	$\bar{z}, y, 0$	$\bar{z}, y, 0$		$(lk0)$	$(\bar{l}\bar{k}0)$	$(\bar{l}k0)$	$(lk0)$		
12	c	$m.m2$	$0, y, y$	$0, \bar{y}, \bar{y}$	$0, y, \bar{y}$	$0, \bar{y}, \bar{y}$	Rhomb-dodecahedron Cuboctahedron	(011)	$(0\bar{1}\bar{1})$	$(01\bar{1})$	$(0\bar{1}1)$		
			$y, 0, y$	$\bar{y}, 0, \bar{y}$	$\bar{y}, 0, \bar{y}$	$\bar{y}, 0, \bar{y}$		(101)	$(10\bar{1})$	(101)	$(10\bar{1})$		
			$y, y, 0$	$\bar{y}, \bar{y}, 0$	$\bar{y}, \bar{y}, 0$	$\bar{y}, \bar{y}, 0$		(110)	$(1\bar{1}0)$	(110)	$(1\bar{1}0)$		
8	b	$.3m$	x, x, x	$\bar{x}, \bar{x}, \bar{x}$	\bar{x}, x, \bar{x}	x, \bar{x}, \bar{x}	Octahedron Cube	(111)	$(\bar{1}\bar{1}\bar{1})$	$(\bar{1}\bar{1}1)$	$(1\bar{1}\bar{1})$		
			x, x, \bar{x}	$\bar{x}, \bar{x}, \bar{x}$	x, \bar{x}, \bar{x}	\bar{x}, x, x		$(11\bar{1})$	$(\bar{1}\bar{1}1)$	(111)	$(\bar{1}\bar{1}\bar{1})$		
6	a	$4m.m$	$x, 0, 0$	$\bar{x}, 0, 0$			Cube or hexahedron Octahedron	(100)	$(\bar{1}00)$				
			$0, x, 0$	$0, \bar{x}, 0$				(010)	$(0\bar{1}0)$				
			$0, 0, x$	$0, 0, \bar{x}$				(001)	$(00\bar{1})$				
1	o	$m\bar{3}m$	$0, 0, 0$				Point in origin						

Symmetry of special projections
 Along [001] Along [111] Along [110]
 $4mm$ $6mm$ $2mm$

3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.3.3

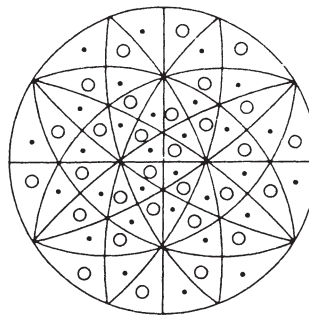
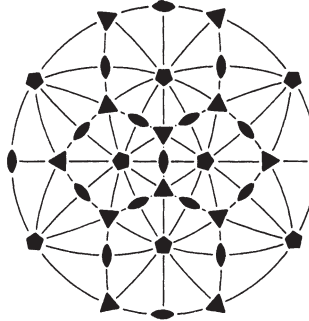
The two icosahedral point groups

Each point group is specified by its Hermann–Mauguin and Schoenflies symbol. For each point group, the stereographic projections show (on the left) the general position and (on the right) the symmetry elements.

The list of the Wyckoff positions includes:

Columns 1 to 3: multiplicity, Wyckoff letter, oriented site-symmetry symbol;

Under the left stereographic projection: face forms (in roman type) and point forms (in italics), corresponding to the values for the Miller indices and coordinates listed in the last column; only 'initial' Miller indices and coordinates are given (see text).

235	<i>I</i>									
60	<i>d</i>	1	<p>Pentagon-hexecontahedron <i>Snub pentagon-dodecahedron</i> (= <i>pentagon-dodecahedron</i> + <i>icosahedron</i> + <i>pentagon-hexecontahedron</i>)</p>	<p>6 + 10 + 15 </p> <p>(<i>hkl</i>) <i>x, y, z</i></p>						
			<p>Tricosahedron <i>Pentagon-dodecahedron truncated by icosahedron</i> (poles between axes 2 and 3)</p>	<p>(<i>0kl</i>) with $l < 0.382 k$ $0, y, z$ with $z < 0.382 y$</p>						
			<p>Deltoid-hexecontahedron <i>Rhomb-triacontahedron</i> & <i>pentagon-dodecahedron</i> & <i>icosahedron</i> (poles between axes 3 and 5)</p>	<p>(<i>0kl</i>) with $0.382 k < l < 1.618 k$ $0, y, z$ with $0.382 y < z < 1.618 y$</p>						
			<p>Pentakisidodecahedron <i>Icosahedron truncated by pentagon-dodecahedron</i> (poles between axes 5 and 2)</p>	<p>(<i>0kl</i>) with $l > 1.618 k$ $0, y, z$ with $z > 1.618 y$</p>						
30	<i>c</i>	2..	<p>Rhomb-triacontahedron <i>Icosadodecahedron</i> (= <i>pentagon-dodecahedron</i> & <i>icosahedron</i>)</p>	<p>(100) $x, 0, 0$</p>						
20	<i>b</i>	.3.	<p>Regular icosahedron <i>Regular pentagon-dodecahedron</i></p>	<p>(111) x, x, x</p>						
12	<i>a</i>	.5	<p>Regular pentagon-dodecahedron <i>Regular icosahedron</i></p>	<p>(01τ) $0, y, \tau y$ } with $\tau = \frac{1}{2}(\sqrt{5} + 1) = 1.618$</p>						
1	<i>o</i>	235	<p><i>Point in origin</i></p>	<p>0, 0, 0</p>						
<p>Symmetry of special projections</p> <table style="margin: auto; border: none;"> <tr> <td style="padding: 0 10px;">Along [001]</td> <td style="padding: 0 10px;">Along [111]</td> <td style="padding: 0 10px;">Along [1τ0]</td> </tr> <tr> <td style="padding: 0 10px;"><i>2mm</i></td> <td style="padding: 0 10px;"><i>3m</i></td> <td style="padding: 0 10px;"><i>5m</i></td> </tr> </table>					Along [001]	Along [111]	Along [1 τ 0]	<i>2mm</i>	<i>3m</i>	<i>5m</i>
Along [001]	Along [111]	Along [1 τ 0]								
<i>2mm</i>	<i>3m</i>	<i>5m</i>								

3.2. POINT GROUPS AND CRYSTAL CLASSES

Table 3.2.3.3 (continued)

$m\bar{3}\bar{5}$	I_h			
		$\frac{2}{m}\bar{3}\bar{5}$	m	
120	<i>e</i>	1	Hecatonicosahedron or hexaicosahedron <i>Pentagon-dodecahedron truncated by icosahedron and by rhomb-triacontahedron</i>	$6\blacklozenge + 10\blacktriangle + 15\bullet + 15m + \text{Centre}$ (<i>hkl</i>) <i>x, y, z</i>
60	<i>d</i>	<i>m.</i>	<div style="border-left: 1px solid black; padding-left: 5px;"> Trisicosahedron <i>Pentagon-dodecahedron truncated by icosahedron (poles between axes 2 and $\bar{3}$)</i> </div> <div style="border-left: 1px solid black; padding-left: 5px; margin-top: 5px;"> Deltoid-hexecontahedron <i>Rhomb-triacontahedron & pentagon-dodecahedron & icosahedron (poles between axes $\bar{3}$ and $\bar{5}$)</i> </div> <div style="border-left: 1px solid black; padding-left: 5px; margin-top: 5px;"> Pentakis-dodecahedron <i>Icosahedron truncated by pentagon-dodecahedron (poles between axes $\bar{5}$ and 2)</i> </div>	(0 <i>kl</i>) with $ l < 0.382 k $ 0, <i>y, z</i> with $ z < 0.382 y $ (0 <i>kl</i>) with $0.382 k < l < 1.618 k $ 0, <i>y, z</i> with $0.382 y < z < 1.618 y $
30	<i>c</i>	$2mm.$	Rhomb-triacontahedron <i>Icosadodecahedron (= pentagon-dodecahedron & icosahedron)</i>	(100) <i>x, 0, 0</i>
20	<i>b</i>	$3m (m\bar{3}.)$	Regular icosahedron <i>Regular pentagon-dodecahedron</i>	(111) <i>x, x, x</i>
12	<i>a</i>	$5m (m\bar{5}.)$	Regular pentagon-dodecahedron <i>Regular icosahedron</i>	(01 τ) 0, <i>y, τy</i> } with $\tau = \frac{1}{2}(\sqrt{5} + 1) = 1.618$
1	<i>o</i>	$2/m\bar{3}\bar{5}$	<i>Point in origin</i>	0, 0, 0
Symmetry of special projections				
<div style="display: flex; justify-content: space-around;"> Along [001] <i>2mm</i> Along [111] <i>6mm</i> Along [1τ0] <i>10mm</i> </div>				