

## 3. ADVANCED TOPICS ON SPACE-GROUP SYMMETRY

Table 3.2.1.4

Names and symbols of the 32 crystal classes

System used in this volume	Point group		Schoenflies symbol	Class names	
	International symbol			Groth (1921)	Friedel (1926)
	Short	Full			
Triclinic	1 $\bar{1}$	1 $\bar{1}$	$C_1$ $C_1(S_2)$	Pedial (asymmetric) Pinacoidal	Hemihedry Holohedry
Monoclinic	2 <i>m</i> $2/m$	2 <i>m</i> $\frac{2}{m}$	$C_2$ $C_2(C_{1h})$ $C_{2h}$	Sphenoidal Domestic Prismatic	Holoaxial hemihedry Antihemihedry Holohedry
Orthorhombic	222 <i>mm2</i> <i>mmm</i>	222 <i>mm2</i> $\frac{2}{m} \frac{2}{m} \frac{2}{m}$	$D_2(V)$ $C_{2v}$ $D_{2h}(V_h)$	Disphenoidal Pyramidal Dipyramidal	Holoaxial hemihedry Antihemihedry Holohedry
Tetragonal	4 $\bar{4}$ $4/m$ 422 <i>4mm</i> $\bar{4}2m$ $4/mmm$	4 $\bar{4}$ $\frac{4}{m}$ 422 <i>4mm</i> $\bar{4}2m$ $\frac{4}{m} \frac{2}{m} \frac{2}{m}$	$C_4$ $S_4$ $C_{4h}$ $D_4$ $C_{4v}$ $D_{2d}(V_d)$ $D_{4h}$	Pyramidal Disphenoidal Dipyramidal Trapezohedral Ditetragonal-pyramidal Scalenohedral Ditetragonal-dipyramidal	Tetartohedry with 4-axis Sphenohedral tetartohedry Parahemihedry Holoaxial hemihedry Antihemihedry with 4-axis Sphenohedral antihemihedry Holohedry
Trigonal	3 $\bar{3}$ 32 $3m$ $\bar{3}m$	3 $\bar{3}$ 32 $3m$ $\frac{3}{m} \frac{2}{m}$	$C_3$ $C_{3i}(S_6)$ $D_3$ $C_{3v}$ $D_{3d}$	Pyramidal Rhombohedral Trapezohedral Ditrigonal-pyramidal Ditrigonal-scalenohedral	<i>Hexagonal</i> Ogdohedry Paratetartohedry Holoaxial tetartohedry with 3-axis Hemimorphic antitetartohedry Parahemihedry with 3-axis <i>Rhombohedral</i> Tetartohedry Parahemihedry Holoaxial hemihedry Antihemihedry Holohedry
Hexagonal	6 $\bar{6}$ $6/m$ 622 <i>6mm</i> $\bar{6}2m$ $6/mmm$	6 $\bar{6}$ $\frac{6}{m}$ 622 <i>6mm</i> $\bar{6}2m$ $\frac{6}{m} \frac{2}{m} \frac{2}{m}$	$C_6$ $C_{3h}$ $C_{6h}$ $D_6$ $C_{6v}$ $D_{3h}$ $D_{6h}$	Pyramidal Trigonal-dipyramidal Dipyramidal Trapezohedral Dihexagonal-pyramidal Ditrigonal-dipyramidal Dihexagonal-dipyramidal	Tetartohedry with 6-axis Trigonal antitetartohedry Parahemihedry with 6-axis Holoaxial hemihedry Antihemihedry with 6-axis Trigonal antihemihedry Holohedry
Cubic	23 $m\bar{3}$ 432 $\bar{4}3m$ $m\bar{3}m$	23 $\frac{2}{m} \frac{3}{m}$ 432 $\bar{4}3m$ $\frac{4}{m} \frac{3}{m} \frac{2}{m}$	$T$ $T_h$ $O$ $T_d$ $O_h$	Tetrahedral-pentagonododecahedral (= tetartoidal) Disdodecahedral (= diploidal) Pentagon-icositetrahedral (= gyroidal) Hexakistetrahedral (= hextetrahedral) Hexakisoctahedral (= hexoctahedral)	Tetartohedry Parahemihedry Holoaxial hemihedry Antihemihedry Holohedry

types of crystal form. Frequently, 48 are quoted because 'sphenoid' and 'dome' are considered as two different forms. It is customary, however, to regard them as the same form, with the name 'dihedron'.

*Name of point form* (printed in italics). There exists no general convention on the names of the point forms. Here, only one name is given, which does not always agree with that of other authors. The names of the point forms are also contained in Table 3.2.1.3.

Note that the same point form, 'line segment', corresponds to both sphenoid and dome.

Column 6: *Miller indices* (*hkl*) for the symmetry-equivalent faces (edges) of a crystal form. In the trigonal and hexagonal crystal systems, when referring to hexagonal axes, Bravais–Miller indices (*hkil*) are used, with  $h + k + i = 0$ .

With a few exceptions, the triplets of Miller indices (*hkl*) and point coordinates  $x, y, z$  are arranged in such a way as to show