

4. DIFFUSE SCATTERING AND RELATED TOPICS

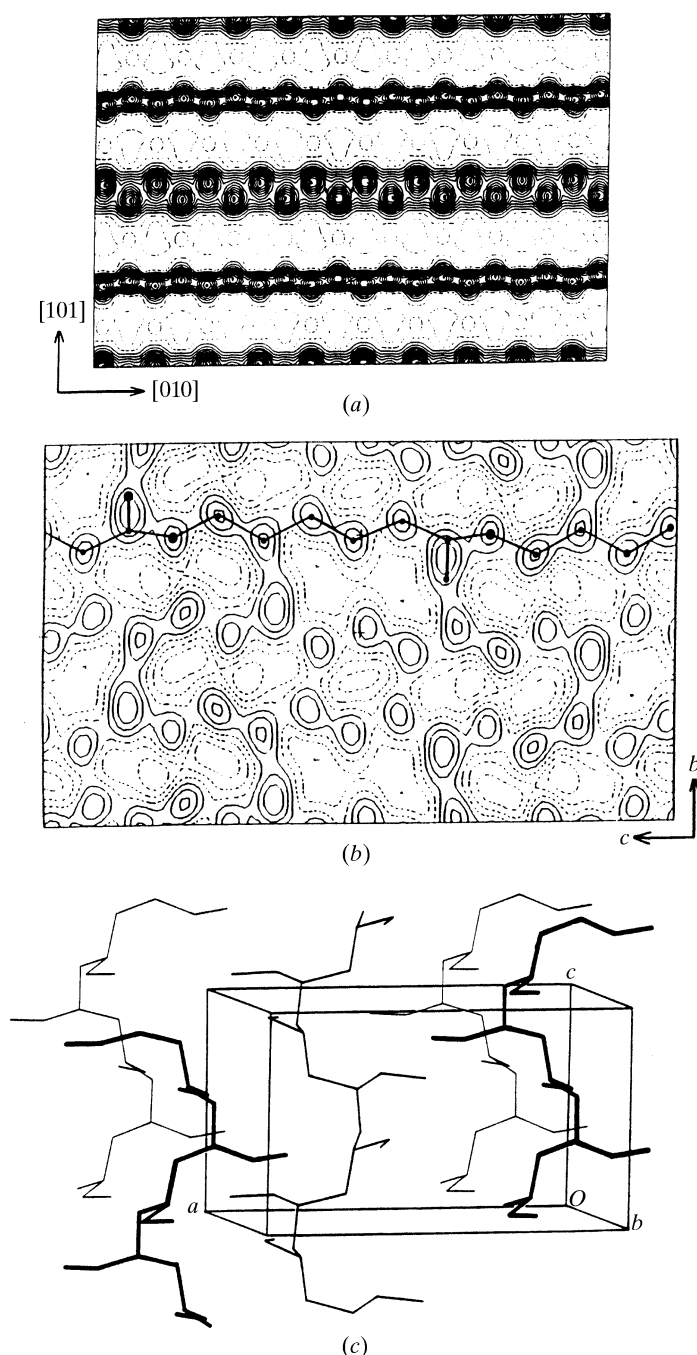


Fig. 4.5.3.2. Crystal structures of linear polymers determined from three-dimensional data. (a) Polyethylene; (b) poly(ϵ -caprolactone); (c) poly(1-butene), form (III).

orthogonal projections of the same polymer polymorph can be obtained, respectively, by self-seeding and epitaxial orientation. While tilting these specimens, all of reciprocal space can be sampled for intensity data collection.

Polyethylene crystals were used to collect 50 unique maxima (Hu & Dorset, 1989) and, *via* symbolic addition, the centrosymmetric phases of 40 reflections (space group $Pnma$) could be readily determined (Dorset, 1991b). The structural features were readily observed in the three-dimensional potential maps (Fig. 4.5.3.2a), and atomic coordinates (with estimated values for hydrogen-atom positions) could be refined by least squares (Dorset, 1995b) to give a final R value of 0.19.

Poly(ϵ -caprolactone) was epitaxially crystallized on benzoic acid and, with $hk0$ data from solution-crystallized samples, a unique set of 47 intensities was collected for the noncentrosymmetric orthorhombic unit cell (space group $P2_12_12_1$) (Hu & Dorset, 1990). Direct phase determination was achieved *via*

symbolic addition, using one algebraic unknown to assign values to 30 reflections (Dorset, 1991c). Atomic positions along the chain repeat, including the carbonyl position, were clearly discerned in the [100] projection (Fig. 4.5.3.2b) and the three-dimensional model was constructed to fit to the map calculated from all phased data, yielding a final crystallographic residual $R = 0.21$. This independent determination was able to distinguish between two rival fibre X-ray structures, in favour of the one that predicted a nonplanar chain conformation. Because of the methylene repeat, this is actually a difficult structure to solve by automated techniques. For example, the tangent formula and SnB (Miller *et al.*, 1993) could only find chain zigzag positions and not the position of the carbonyl oxygen atom (Dorset, 1995b).

The most complicated complete polymer crystal structure solved so far by direct methods using electron diffraction data (Dorset *et al.*, 1994) was based on 125 unique data (space group $P2_12_12_1$) from isotactic poly(1-butene), form (III), using orthogonal molecular orientations crystallized in Strasbourg (Kopp *et al.*, 1994). Initially, the standard NQUEST figure of merit (FOM) (De Titta *et al.*, 1975) was not suitable for identifying the correct solution among the multiple sets generated with the tangent formula. A solution could only be found when a separate phase determination was carried out with the $hk0$ data to compare with the multiple solutions generated. More recently, the minimal principle (Hauptman, 1993), used as a FOM with the tangent formula or with a multiple random structure generator, SnB , correctly identified the structure on the first try (Dorset, 1995b). The maps clearly show individual carbon-atom positions in a 4_1 helix that parallels 2_1 helices of the space group (Fig. 4.5.3.2c). After Fourier refinement, the crystallographic residual was $R = 0.26$. The previous powder X-ray diffraction determination was based on only 21 diffraction maxima, some of which had as many as 15 individual contributors.

The work of both RPM and DLD was supported by the US National Science Foundation (grant DBI-9722862 for RPM).

References

- Alexeev, D. G., Lipanov, A. A. & Skuratovskii, I. Y. (1992). *Patterson methods in fibre diffraction*. *Int. J. Biol. Macromol.* **14**, 139–144.
- Arnott, S. (1980). *Twenty years hard labor as a fibre diffractionist*. In *Fibre Diffraction Methods*, ACS Symposium Series, Vol. 141, edited by A. D. French & K. H. Gardner, pp. 1–30. Washington: American Chemical Society.
- Arnott, S., Chandrasekaran, R., Millane, R. P. & Park, H. (1986). *DNA–RNA hybrid secondary structures*. *J. Mol. Biol.* **188**, 631–640.
- Arnott, S. & Mitra, A. K. (1984). *X-ray diffraction analyses of glycosaminoglycans*. In *Molecular Biophysics of the Extracellular Matrix*, edited by S. Arnott, D. A. Rees & E. R. Morris, pp. 41–67. Clifton: Humana Press.
- Arnott, S., Wilkins, M. H. F., Fuller, W. & Langridge, R. (1967). *Molecular and crystal structures of double-helical RNA III. An 11-fold molecular model and comparison of the agreement between the observed and calculated three-dimensional diffraction data for 10- and 11-fold models*. *J. Mol. Biol.* **27**, 535–548.
- Arnott, S. & Wonacott, A. J. (1966). *The refinement of the crystal and molecular structures of polymers using X-ray data and stereochemical constraints*. *Polymer*, **7**, 157–166.
- Atkins, E. D. T. (1989). *Crystal structure by X-ray diffraction*. In *Comprehensive Polymer Science*, Vol. 1. *Polymer Characterization*, edited by G. A. Allen, pp. 613–650. Oxford: Pergamon Press.
- Barham, P. J. (1993). *Crystallization and morphology of semicrystalline polymers*. In *Materials Science and Technology. A Comprehensive Treatment*, Vol. 12. *Structure and Properties of Polymers*, edited by E. L. Thomas, pp. 153–212. Weinheim: VCH.
- Baskaran, S. & Millane, R. P. (1999a). *Bayesian image reconstruction from partial image and aliased spectral intensity data*. *IEEE Trans. Image Process.* **8**, 1420–1434.
- Baskaran, S. & Millane, R. P. (1999b). *Model bias in Bayesian image reconstruction from X-ray fiber diffraction data*. *J. Opt. Soc. Am. A*, **16**, 236–245.

4.5. POLYMER CRYSTALLOGRAPHY

- Biswas, A. & Blackwell, J. (1988a). *Three-dimensional structure of main-chain liquid-crystalline copolymers. 1. Cylindrically averaged intensity transforms of single chains.* *Macromolecules*, **21**, 3146–3151.
- Biswas, A. & Blackwell, J. (1988b). *Three-dimensional structure of main-chain liquid-crystalline copolymers. 2. Interchain interference effects.* *Macromolecules*, **21**, 3152–3158.
- Biswas, A. & Blackwell, J. (1988c). *Three-dimensional structure of main-chain liquid-crystalline copolymers. 3. Chain packing in the solid state.* *Macromolecules*, **21**, 3158–3164.
- Blackwell, J., Gutierrez, G. A. & Chivers, R. A. (1984). *Diffraction by aperiodic polymer chains: the structure of liquid crystalline copolyesters.* *Macromolecules*, **17**, 1219–1224.
- Blundell, D. J., Keller, A. & Kovacs, A. J. (1966). *A new self-nucleation phenomenon and its application to the growing of polymer crystals from solution.* *J. Polym. Sci. Polym. Lett. Ed.* **4**, 481–486.
- Brisse, F. (1989). *Electron diffraction of synthetic polymers: the model compound approach to polymer structure.* *J. Electron Microsc. Tech.* **11**, 272–279.
- Brisse, F., Remillard, B. & Chanzy, H. (1984). *Poly(1,4-trans-cyclohexanedimethylsuccinate). A structural determination using X-ray and electron diffraction.* *Macromolecules*, **17**, 1980–1987.
- Brünger, A. T. (1992). *X-PLOR*. Version 3.1. New Haven: Yale University Press.
- Brünger, A. T. (1997). *Free R value: cross-validation in crystallography.* *Methods Enzymol.* **277**, 366–396.
- Cael, J. J., Winter, W. T. & Arnott, S. (1978). *Calcium chondroitin 4-sulfate: molecular conformation and organization of polysaccharide chains in a proteoglycan.* *J. Mol. Biol.* **125**, 21–42.
- Campbell Smith, P. J. & Arnott, S. (1978). *LALS: a linked-atom least-squares reciprocal-space refinement system incorporating stereochemical constraints to supplement sparse diffraction data.* *Acta Cryst.* **A34**, 3–11.
- Chandrasekaran, R. & Arnott, S. (1989). *The structures of DNA and RNA helices in oriented fibres.* In *Landolt–Bornstein Numerical Data and Functional Relationships in Science and Technology*, Vol. VII/1b, edited by W. Saenger, pp. 31–170. Berlin, Heidelberg: Springer-Verlag.
- Chandrasekaran, R., Radha, A. & Lee, E. J. (1994). *Structural roles of calcium ions and side chains in welan: an X-ray study.* *Carbohydr. Res.* **252**, 183–207.
- Chanzy, H., Perez, S., Miller, D. P., Paradossi, G. & Winter, W. T. (1987). *An electron diffraction study of mannan I. Crystal and molecular structure.* *Macromolecules*, **20**, 2407–2413.
- Chivers, R. A. & Blackwell, J. (1985). *Three-dimensional structure of copolymers of p-hydroxybenzoic acid and 2-hydroxy-6-naphthoic acid: a model for diffraction from a nematic structure.* *Polymer*, **26**, 997–1002.
- Clark, E. S. & Muus, I. T. (1962). *The relationship between Bragg reflections and disorder in crystalline polymers.* *Z. Kristallogr.* **117**, 108–118.
- Cochran, W., Crick, F. H. C. & Vand, V. (1952). *The structure of synthetic polypeptides. I. The transform of atoms on a helix.* *Acta Cryst.* **5**, 581–586.
- Cowley, J. M. (1961). *Diffraction intensities from bent crystals.* *Acta Cryst.* **14**, 920–927.
- Cowley, J. M. (1981). *Diffraction Physics*, 2nd revised ed. Amsterdam: North-Holland.
- Cowley, J. M. (1988). *Imaging [and] imaging theory.* In *High-Resolution Transmission Electron Microscopy and Associated Techniques*, edited by P. Busek, J. M. Cowley & L. Eyring, pp. 3–57. New York: Oxford University Press.
- Crowther, R. A., DeRosier, D. J. & Klug, A. (1970). *The reconstruction of a three-dimensional structure from projections and its application to electron microscopy.* *Proc. R. Soc. London Ser. A*, **317**, 319–344.
- Daubeny, R. de P., Bunn, C. W. & Brown, C. J. (1954). *The crystal structure of polyethylene terephthalate.* *Proc. R. Soc. London Ser. A*, **226**, 531–542.
- Day, D. & Lando, J. B. (1980). *Structure determination of a poly(diacetylene) monolayer.* *Macromolecules*, **13**, 1483–1487.
- De Titta, G. T., Edmonds, J. W., Langs, D. A. & Hauptman, H. (1975). *Use of negative quartet cosine invariants as a phasing figure of merit: NQEST.* *Acta Cryst.* **A31**, 472–479.
- Dorset, D. L. (1989). *Electron diffraction from crystalline polymers.* In *Comprehensive Polymer Science*, Vol. 1. *Polymer Characterization*, edited by G. A. Allen, pp. 651–668. Oxford: Pergamon Press.
- Dorset, D. L. (1991a). *Is electron crystallography possible? The direct determination of organic crystal structures.* *Ultramicroscopy*, **38**, 23–40.
- Dorset, D. L. (1991b). *Electron diffraction structure analysis of polyethylene. A direct phase determination.* *Macromolecules*, **24**, 1175–1178.
- Dorset, D. L. (1991c). *Electron crystallography of linear polymers: direct structure analysis of poly(ϵ -caprolactone).* *Proc. Natl Acad. Sci. USA*, **88**, 5499–5502.
- Dorset, D. L. (1992). *Electron crystallography of linear polymers: direct phase determination for zonal data sets.* *Macromolecules*, **25**, 4425–4430.
- Dorset, D. L. (1995a). *Comments on the validity of the direct phasing and Fourier methods in electron crystallography.* *Acta Cryst.* **A51**, 869–879.
- Dorset, D. L. (1995b). *Structural Electron Crystallography*. New York: Plenum.
- Dorset, D. L. (1995c). *Filling the cone – overcoming the goniometric tilt limit in electron crystallography by direct methods.* *Am. Cryst. Assoc. Abstr. Series 2*, 23, p. 89.
- Dorset, D. L., Kopp, S., Fryer, J. R. & Tivol, W. T. (1995). *The Sayre equation in electron crystallography.* *Ultramicroscopy*, **57**, 59–89.
- Dorset, D. L. & McCourt, M. P. (1993). *Electron crystallographic analysis of a polysaccharide structure – direct phase determination and model refinement for mannan I.* *J. Struct. Biol.* **111**, 118–124.
- Dorset, D. L., McCourt, M. P., Kopp, S., Wittmann, J.-C. & Lotz, B. (1994). *Direct determination of polymer crystal structures by electron crystallography – isotactic poly(1-butene), form (III).* *Acta Cryst.* **B50**, 201–208.
- Doyle, P. A. & Turner, P. S. (1968). *Relativistic Hartree–Fock X-ray and electron scattering factors.* *Acta Cryst.* **A24**, 390–397.
- Drenth, J. (1994). *Principles of Protein X-ray Crystallography*. New York: Springer-Verlag.
- Finkenstadt, V. L. & Millane, R. P. (1998). *Fiber diffraction patterns for general unit cells: the cylindrically projected reciprocal lattice.* *Acta Cryst.* **A54**, 240–248.
- Forsyth, V. T., Mahendrasingam, A., Pigram, W. J., Greenall, R. J., Bellamy, K., Fuller, W. & Mason, S. A. (1989). *Neutron fibre diffraction study of DNA hydration.* *Int. J. Biol. Macromol.* **11**, 236–240.
- Franklin, R. E. (1955). *Structure of tobacco mosaic virus.* *Nature (London)*, **175**, 379–381.
- Franklin, R. E. & Gosling, R. G. (1953). *The structure of sodium thymonucleate fibres. II. The cylindrically symmetrical Patterson function.* *Acta Cryst.* **6**, 678–685.
- Franklin, R. E. & Holmes, K. C. (1958). *Tobacco mosaic virus: application of the method of isomorphous replacement to the determination of the helical parameters and radial density distribution.* *Acta Cryst.* **11**, 213–220.
- Franklin, R. E. & Klug, A. (1955). *The splitting of layer lines in X-ray fibre diagrams of helical structures: application to tobacco mosaic virus.* *Acta Cryst.* **8**, 777–780.
- Fraser, R. D. B. & MacRae, T. P. (1973). *Conformations in Fibrous Proteins*. New York: Academic Press.
- Fraser, R. D. B., MacRae, T. P., Miller, A. & Rowlands, R. J. (1976). *Digital processing of fibre diffraction patterns.* *J. Appl. Cryst.* **9**, 81–94.
- Fraser, R. D. B., Suzuki, E. & MacRae, T. P. (1984). *Computer analysis of X-ray diffraction patterns.* In *Structure of Crystalline Polymers*, edited by I. H. Hall, pp. 1–37. New York: Elsevier.
- French, A. D. & Gardner, K. H. (1980). *Editors. Fibre Diffraction Methods.* ACS Symposium Series, Vol. 141. Washington: American Chemical Society.
- Geil, P. H. (1963). *Polymer Single Crystals*. New York: John Wiley & Sons.
- Gilmore, C. J., Shankland, K. & Bricogne, G. (1993). *Application of the maximum entropy method to powder diffraction and electron crystallography.* *Proc. R. Soc. London Ser. A*, **442**, 97–111.
- Gonzalez, A., Nave, C. & Marvin, D. A. (1995). *Pf1 filamentous bacteriophage: refinement of a molecular model by simulated annealing using 3.3 Å resolution X-ray fiber diffraction data.* *Acta Cryst.* **D51**, 792–804.
- Graaf, H. de (1989). *On the calculation of small-angle diffraction patterns from distorted lattices.* *Acta Cryst.* **A45**, 861–870.
- Grubb, D. T. (1993). *Elastic properties of crystalline polymers.* In *Materials Science and Technology. A Comprehensive Treatment*, Vol. 12. *Structure and Properties of Polymers*, edited by E. L. Thomas, pp. 301–356. Weinheim: VCH.
- Hall, I. H. (1984). *Editor. Structure of Crystalline Polymers*. New York: Elsevier.

4. DIFFUSE SCATTERING AND RELATED TOPICS

- Hall, I. H., Neisser, J. Z. & Elder, M. (1987). *A computer-based method of measuring the integrated intensities of the reflections on the X-ray diffraction photograph of an oriented crystalline polymer*. *J. Appl. Cryst.* **20**, 246–255.
- Hamilton, W. C. (1965). *Significance tests on the crystallographic R factor*. *Acta Cryst.* **18**, 502–510.
- Hauptman, H. A. (1993). *A minimal principle in X-ray crystallography: starting in a small way*. *Proc. R. Soc. London Ser. A*, **442**, 3–12.
- Hendricks, S. & Teller, E. (1942). *X-ray interference in partially ordered layer lattices*. *J. Chem. Phys.* **10**, 147–167.
- Hirsch, P. B., Howie, A., Nicholson, P. B., Pashley, D. W. & Whelan, M. J. (1965). *Electron Microscopy of Thin Crystals*. London: Butterworths.
- Hofmann, D., Schneider, A. I. & Blackwell, J. (1994). *Molecular modelling of the structure of a wholly aromatic thermotropic copolyester*. *Polymer*, **35**, 5603–5610.
- Holmes, K. C. & Barrington Leigh, J. (1974). *The effect of disorientation on the intensity distribution of non-crystalline fibres. I. Theory*. *Acta Cryst.* **A30**, 635–638.
- Holmes, K. C., Popp, D., Gebhard, W. & Kabsch, W. (1990). *Atomic model of the actin filament*. *Nature (London)*, **347**, 44–49.
- Holmes, K. C., Stubbs, G. J., Mandelkow, E. & Gallwitz, U. (1975). *Structure of tobacco mosaic virus at 6.7 Å resolution*. *Nature (London)*, **254**, 192–196.
- Hosemann, R. & Bagchi, S. N. (1962). *Direct Analysis of Diffraction by Matter*. Amsterdam: North-Holland.
- Hu, H. & Dorset, D. L. (1989). *Three-dimensional electron diffraction structure analysis of polyethylene*. *Acta Cryst.* **B45**, 283–290.
- Hu, H. & Dorset, D. L. (1990). *Crystal structure of poly(ϵ -caprolactone)*. *Macromolecules*, **23**, 4604–4607.
- Hudson, L., Harford, J. J., Denny, R. C. & Squire, J. M. (1997). *Myosin head configuration in relaxed fish muscle: resting state myosin heads must swing axially by up to 150 Å or turn upside down to reach rigor*. *J. Mol. Biol.* **273**, 440–455.
- Iannelli, P. (1994). *FWR: a computer program for refining the molecular structure in the crystalline phase of polymers based on the analysis of the whole X-ray fibre diffraction patterns*. *J. Appl. Cryst.* **27**, 1055–1060.
- Isoda, S., Tsuji, M., Ohara, M., Kawaguchi, A. & Katayama, K. (1983a). *Structural analysis of β -form poly(p-xylene) starting from a high-resolution image*. *Polymer*, **24**, 1155–1161.
- Isoda, S., Tsuji, M., Ohara, M., Kawaguchi, A. & Katayama, K. (1983b). *Direct observation of dislocations in polymer single crystals*. *Makromol. Chem. Rapid Commun.* **4**, 141–144.
- Ivanova, M. I. & Makowski, L. (1998). *Iterative low-pass filtering for estimation of the background in fiber diffraction patterns*. *Acta Cryst.* **A54**, 626–631.
- Klug, A., Crick, F. H. C. & Wyckoff, H. W. (1958). *Diffraction from helical structures*. *Acta Cryst.* **11**, 199–213.
- Kopp, S., Wittmann, J. C. & Lotz, B. (1994). *Epitaxial crystallization and crystalline polymorphism of poly(1-butene): form (III) and (II)*. *Polymer*, **35**, 908–915.
- Lipson, H. & Cochran, W. (1966). *The Determination of Crystal Structures*, p. 381. Ithaca: Cornell University Press.
- Liu, J. & Geil, P. H. (1993). *Morphological observations of nascent poly(p-oxabenzate)*. *Polymer*, **34**, 1366–1374.
- Liu, J., Yuan, B.-L., Geil, P. H. & Dorset, D. L. (1997). *Chain conformation and molecular packing in poly(p-oxabenzate) single crystals at ambient temperature*. *Polymer*, **38**, 6031–6047.
- Lobert, S., Heil, P. D., Namba, K. & Stubbs, G. (1987). *Preliminary X-ray fibre diffraction studies of cucumber green mottle mosaic virus, watermelon strain*. *J. Mol. Biol.* **196**, 935–938.
- Lobert, S. & Stubbs, G. (1990). *Fibre diffraction analysis of cucumber green mottle mosaic virus using limited numbers of heavy-atom derivatives*. *Acta Cryst.* **A46**, 993–997.
- Lorenz, M. & Holmes, K. C. (1993). *Computer processing and analysis of X-ray fibre diffraction data*. *J. Appl. Cryst.* **26**, 82–91.
- Lorenz, M., Popp, D. & Holmes, K. C. (1993). *Refinement of the F-actin model against X-ray fibre diffraction data by the use of a directed mutation algorithm*. *J. Mol. Biol.* **234**, 826–836.
- Lotz, B. & Wittmann, J. C. (1993). *Structure of polymer single crystals*. In *Materials Science and Technology. A Comprehensive Treatment*, Vol. 12. *Structure and Properties of Polymers*, edited by E. L. Thomas, pp. 79–154. Weinheim: VCH.
- MacGillivray, C. H. & Bruins, E. M. (1948). *On the Patterson transforms of fibre diagrams*. *Acta Cryst.* **1**, 156–158.
- Makowski, L. (1978). *Processing of X-ray diffraction data from partially oriented specimens*. *J. Appl. Cryst.* **11**, 273–283.
- Makowski, L. (1982). *The use of continuous diffraction data as a phase constraint. II. Application to fibre diffraction data*. *J. Appl. Cryst.* **15**, 546–557.
- Makowski, L., Caspar, D. L. D. & Marvin, D. A. (1980). *Filamentous bacteriophage Pfl structure determined at 7 Å resolution by refinement of models for the α -helical subunit*. *J. Mol. Biol.* **140**, 149–181.
- Mandelkern, L. (1989). *Crystallization and melting*. In *Comprehensive Polymer Science*, Vol. 2. *Polymer Properties*, edited by C. Booth & C. Price, pp. 363–414. Oxford: Pergamon Press.
- Mandelkow, E. & Holmes, K. C. (1974). *The positions of the N-terminus and residue 68 in tobacco mosaic virus*. *J. Mol. Biol.* **87**, 265–273.
- Mandelkow, E., Stubbs, G. & Warren, S. (1981). *Structures of the helical aggregates of tobacco mosaic virus protein*. *J. Mol. Biol.* **152**, 375–386.
- Marvin, D. A., Bryan, R. K. & Nave, C. (1987). *Pfl inovirus. Electron density distribution calculated by a maximum entropy algorithm from native fiber diffraction data to 3 Å resolution and single isomorphous replacement data to 5 Å resolution*. *J. Mol. Biol.* **193**, 315–343.
- Mauritz, K. A., Baer, E. & Hopfinger, A. J. (1978). *The epitaxial crystallization of macromolecules*. *J. Polym. Sci. Macromol. Rev.* **13**, 1–61.
- Mazeau, K., Winter, W. T. & Chanzy, H. (1994). *Molecular and crystal structure of a high-temperature polymorph of chitosan from electron diffraction data*. *Macromolecules*, **27**, 7606–7612.
- Millane, R. P. (1988). *X-ray fibre diffraction*. In *Crystallographic Computing 4. Techniques and New Technologies*, edited by N. W. Isaacs & M. R. Taylor, pp. 169–186. Oxford University Press.
- Millane, R. P. (1989a). *R factors in X-ray fibre diffraction. I. Largest likely R factors for N overlapping terms*. *Acta Cryst.* **A45**, 258–260.
- Millane, R. P. (1989b). *R factors in X-ray fibre diffraction. II. Largest likely R factors*. *Acta Cryst.* **A45**, 573–576.
- Millane, R. P. (1989c). *Relating reflection boundaries in X-ray fibre diffraction patterns to specimen morphology and their use for intensity measurement*. *J. Macromol. Sci. Phys.* **B28**, 149–166.
- Millane, R. P. (1990a). *Intensity distributions in fibre diffraction*. *Acta Cryst.* **A46**, 552–559.
- Millane, R. P. (1990b). *Phase retrieval in crystallography and optics. J. Opt. Soc. Am. A*, **7**, 394–411.
- Millane, R. P. (1990c). *Polysaccharide structures: X-ray fibre diffraction studies*. In *Computer Modeling of Carbohydrate Molecules*. ACS Symposium Series No. 430, edited by A. D. French & J. W. Brady, pp. 315–331. Washington: American Chemical Society.
- Millane, R. P. (1990d). *R factors in X-ray fibre diffraction. III. Asymptotic approximations to largest likely R factors*. *Acta Cryst.* **A46**, 68–72.
- Millane, R. P. (1991). *An alternative approach to helical diffraction*. *Acta Cryst.* **A47**, 449–451.
- Millane, R. P. (1992a). *Largest likely R factors for normal distributions*. *Acta Cryst.* **A48**, 649–650.
- Millane, R. P. (1992b). *R factors in X-ray fibre diffraction. IV. Analytic expressions for largest likely R factors*. *Acta Cryst.* **A48**, 209–215.
- Millane, R. P. (1993). *Image reconstruction from cylindrically averaged diffraction intensities*. In *Digital Image Recovery and Synthesis II*, Proc. SPIE, Vol. 2029, edited by P. S. Idell, pp. 137–143. Bellingham: SPIE.
- Millane, R. P. & Arnott, S. (1985). *Background removal in X-ray fibre diffraction patterns*. *J. Appl. Cryst.* **18**, 419–423.
- Millane, R. P. & Arnott, S. (1986). *Digital processing of X-ray diffraction patterns from oriented fibres*. *J. Macromol. Sci. Phys.* **B24**, 193–227.
- Millane, R. P. & Baskaran, S. (1997). *Optimal difference Fourier synthesis in fibre diffraction*. *Fiber Diffr. Rev.* **6**, 14–18.
- Millane, R. P., Byler, M. A. & Arnott, S. (1985). *Implementing constrained least squares refinement of helical polymers on a vector pipeline machine*. In *Supercomputer Applications*, edited by R. W. Numrich, pp. 137–143. New York: Plenum.
- Millane, R. P., Chandrasekaran, R., Arnott, S. & Dea, I. C. M. (1988). *The molecular structure of kappa-carrageenan and comparison with iota-carrageenan*. *Carbohydr. Res.* **182**, 1–17.
- Millane, R. P. & Stroud, W. J. (1991). *Effects of disorder on fibre diffraction patterns*. *Int. J. Biol. Macromol.* **13**, 202–208.
- Millane, R. P. & Stubbs, G. (1992). *The significance of R factors in fibre diffraction*. *Polym. Prepr.* **33**, 321–322.
- Miller, R., DeTitta, G. T., Jones, R., Langs, D. A., Weeks, C. M. & Hauptman, H. A. (1993). *On the application of the minimal principle to solve unknown structures*. *Science*, **259**, 1430–1433.

4.5. POLYMER CRYSTALLOGRAPHY

- Namba, K., Pattanayek, R. & Stubbs, G. J. (1989). *Visualization of protein–nucleic acid interactions in a virus. Refined structure of intact tobacco mosaic virus at 2.9 Å resolution by X-ray fibre diffraction.* *J. Mol. Biol.* **208**, 307–325.
- Namba, K. & Stubbs, G. (1985). *Solving the phase problem in fibre diffraction. Application to tobacco mosaic virus at 3.6 Å resolution.* *Acta Cryst.* **A41**, 252–262.
- Namba, K. & Stubbs, G. (1987a). *Difference Fourier syntheses in fibre diffraction.* *Acta Cryst.* **A43**, 533–539.
- Namba, K. & Stubbs, G. (1987b). *Isomorphous replacement in fibre diffraction using limited numbers of heavy-atom derivatives.* *Acta Cryst.* **A43**, 64–69.
- Namba, K., Wakabayashi, K. & Mitsui, T. (1980). *X-ray structure analysis of the thin filament of crab striated muscle in the rigor state.* *J. Mol. Biol.* **138**, 1–26.
- Namba, K., Yamashita, I. & Vonderviszt, F. (1989). *Structure of the core and central channel of bacterial flagella.* *Nature (London)*, **342**, 648–654.
- Nambudripad, R., Stark, W. & Makowski, L. (1991). *Neutron diffraction studies of the structure of filamentous bacteriophage Pfl.* *J. Mol. Biol.* **220**, 359–379.
- Park, H., Arnott, S., Chandrasekaran, R., Millane, R. P. & Campagnari, F. (1987). *Structure of the α -form of poly(dA)–poly(dT) and related polynucleotide duplexes.* *J. Mol. Biol.* **197**, 513–523.
- Perez, S. & Chanzy, H. (1989). *Electron crystallography of linear polysaccharides.* *J. Electron Microsc. Tech.* **11**, 280–285.
- Rickert, S. E., Lando, J. B., Hopfinger, A. J. & Baer, E. (1979). *Epitaxial polymerization of (SN)_x I. Structure and morphology of single crystals on alkali halide substrates.* *Macromolecules*, **12**, 1053–1057.
- Rybnikar, F., Liu, J. & Geil, P. H. (1994). *Thin film melt-polymerized single crystals of poly(p-oxybenzoate).* *Makromol. Chem. Phys.* **195**, 81–104.
- Sayre, D. (1952). *The squaring method: a new method for phase determination.* *Acta Cryst.* **5**, 60–65.
- Schneider, A. I., Blackwell, J., Pielartzik, H. & Karbach, A. (1991). *Structure analysis of copoly(ester carbonate).* *Macromolecules*, **24**, 5676–5682.
- Shotton, M. W., Denny, R. C. & Forsyth, V. T. (1998). *CCP13 software development.* *Fiber Diffraction Rev.* **7**, 40–44.
- Sim, G. A. (1960). *A note on the heavy atom method.* *Acta Cryst.* **13**, 511–512.
- Squire, J. M., Al-Khayat, H. A. & Yagi, N. (1993). *Muscle thin-filament structure and regulation. Actin sub-domain movements and the tropomyosin shift modelled from low-angle X-ray diffraction.* *J. Chem. Soc. Faraday Trans.* **89**, 2717–2726.
- Squire, J., Cantino, M., Chew, M., Denny, R., Harford, J., Hudson, L. & Luther, P. (1998). *Myosin rod-packing schemes in vertebrate muscle thick filaments.* *J. Struct. Biol.* **122**, 128–138.
- Squire, J. M. & Vibert, P. J. (1987). *Editors. Fibrous Protein Structure.* London: Academic Press.
- Stanley, E. (1986). *'Peakiness' test functions.* *Acta Cryst.* **A42**, 297–299.
- Stark, W., Glucksman, M. J. & Makowski, L. (1988). *Conformation of the coat protein of filamentous bacteriophage Pfl determined by neutron diffraction from magnetically oriented gels of specifically deuterated virions.* *J. Mol. Biol.* **199**, 171–182.
- Storks, K. H. (1938). *An electron diffraction examination of some linear high polymers.* *J. Am. Chem. Soc.* **60**, 1753–1761.
- Stroud, W. J. & Millane, R. P. (1995a). *Analysis of disorder in biopolymer fibres.* *Acta Cryst.* **A51**, 790–800.
- Stroud, W. J. & Millane, R. P. (1995b). *Diffraction by disordered polycrystalline fibres.* *Acta Cryst.* **A51**, 771–790.
- Stroud, W. J. & Millane, R. P. (1996a). *Cylindrically averaged diffraction by distorted lattices.* *Proc. R. Soc. London*, **452**, 151–173.
- Stroud, W. J. & Millane, R. P. (1996b). *Diffraction by polycrystalline fibres with correlated disorder.* *Acta Cryst.* **A52**, 812–829.
- Stubbs, G. (1987). *The Patterson function in fibre diffraction.* In *Patterson and Pattersons*, edited by J. P. Glusker, B. K. Patterson & M. Rossi, pp. 548–557. Oxford University Press.
- Stubbs, G. (1989). *The probability distributions of X-ray intensities in fibre diffraction: largest likely values for fibre diffraction R factors.* *Acta Cryst.* **A45**, 254–258.
- Stubbs, G. (1999). *Developments in fiber diffraction.* *Curr. Opin. Struct. Biol.* **9**, 615–619.
- Stubbs, G., Warren, S. & Holmes, K. (1977). *Structure of RNA and RNA binding site in tobacco mosaic virus from a 4 Å map calculated from X-ray fibre diagrams.* *Nature (London)*, **267**, 216–221.
- Stubbs, G. J. (1974). *The effect of disorientation on the intensity distribution of non-crystalline fibres. II. Applications.* *Acta Cryst.* **A30**, 639–645.
- Stubbs, G. J. & Diamond, R. (1975). *The phase problem for cylindrically averaged diffraction patterns. Solution by isomorphous replacement and application to tobacco mosaic virus.* *Acta Cryst.* **A31**, 709–718.
- Stubbs, G. J. & Makowski, L. (1982). *Coordinated use of isomorphous replacement and layer-line splitting in the phasing of fibre diffraction data.* *Acta Cryst.* **A38**, 417–425.
- Tadokoro, H. (1979). *Structure of crystalline polymers.* New York: Wiley.
- Tanaka, S. & Naya, S. (1969). *Theory of X-ray scattering by disordered polymer crystals.* *J. Phys. Soc. Jpn*, **26**, 982–993.
- Tatarinova, L. I. & Vainshtein, B. K. (1962). *Issledovanie poli- γ -metil-L-glutamata v α -forme metodom difraktsii elektronov. (Electron diffraction study of poly- γ -methyl-L-glutamate in the α -form.)* *Visokomol. Soed.* **4**, 261–269.
- Tirion, M., ben Avraham, D., Lorenz, M. & Holmes, K. C. (1995). *Normal modes as refinement parameters for the F-actin model.* *Biophys. J.* **68**, 5–12.
- Tsuji, M. (1989). *Electron microscopy.* In *Comprehensive Polymer Science*, Vol. 1. *Polymer Characterization*, edited by G. A. Allen, pp. 785–866. Oxford: Pergamon Press.
- Vainshtein, B. K. (1964). *Structure analysis by electron diffraction.* Oxford: Pergamon Press.
- Vainshtein, B. K. (1966). *Diffraction of X-rays by chain molecules.* Amsterdam: Elsevier.
- Vainshtein, B. K. & Tatarinova, L. I. (1967). *The β -form of poly- γ -methyl-L-glutamate.* *Sov. Phys. Crystallogr.* **11**, 494–498.
- Vibert, P. J. (1987). *Fibre diffraction methods.* In *Fibrous Protein Structure*, edited by J. M. Squire & P. J. Vibert, pp. 23–45. New York: Academic Press.
- Wang, H., Culver, J. N. & Stubbs, G. (1997). *Structure of ribgrass mosaic virus at 2.9 Å resolution: evolution and taxonomy of tobamoviruses.* *J. Mol. Biol.* **269**, 769–779.
- Wang, H. & Stubbs, G. (1993). *Molecular dynamics refinement against fibre diffraction data.* *Acta Cryst.* **A49**, 504–513.
- Wang, H. & Stubbs, G. J. (1994). *Structure determination of cucumber green mottle mosaic virus by X-ray fibre diffraction. Significance for the evolution of tobamoviruses.* *J. Mol. Biol.* **239**, 371–384.
- Welberry, T. R., Miller, G. H. & Carroll, C. E. (1980). *Paracrystals and growth-disorder models.* *Acta Cryst.* **A36**, 921–929.
- Welsh, L. C., Symmons, M. F. & Marvin, D. A. (2000). *The molecular structure and structural transition of the α -helical capsid in filamentous bacteriophage Pfl.* *Acta Cryst.* **D56**, 137–150.
- Welsh, L. C., Symmons, M. F., Sturtevant, J. M., Marvin, D. A. & Perham, R. N. (1998). *Structure of the capsid of Pfl filamentous phage determined from X-ray fiber diffraction data at 3.1 Å resolution.* *J. Mol. Biol.* **283**, 155–177.
- Wilson, A. J. C. (1950). *Largest likely values for the reliability index.* *Acta Cryst.* **3**, 397–399.
- Wittmann, J. C. & Lotz, B. (1985). *Polymer decoration: the orientation of polymer folds as revealed by the crystallization of polymer vapor.* *J. Polym. Sci. Polym. Phys. Ed.* **23**, 205–226.
- Wittmann, J. C. & Lotz, B. (1990). *Epitaxial crystallization of polymers on organic and polymeric substrates.* *Prog. Polym. Sci.* **15**, 909–948.
- Wunderlich, B. (1973). *Macromolecular Physics*, Vol. 1. *Crystal Structure, Morphology, Defects.* New York: Academic Press.
- Yamashita, I., Hasegawa, K., Suzuki, H., Vonderviszt, F., Mimori-Kiyosue, Y. & Namba, K. (1998). *Structure and switching of bacterial flagellar filaments studied by X-ray fiber diffraction.* *Nature Struct. Biol.* **5**, 125–132.
- Zugenmaier, P. & Sarko, A. (1980). *The variable virtual bond.* In *Fibre Diffraction Methods*, ACS Symposium Series Vol. 141, edited by A. D. French & K. H. Gardner, pp. 225–237. Washington: American Chemical Society.