

9. BASIC STRUCTURAL FEATURES

Table 9.1.1.2. Examples for sphere packings with high contact numbers and high densities and with low contact numbers and low densities

Type	<i>k</i>	Symmetry	Parameters	Distance <i>d</i>	Net	Stacking	Density
1	12	$P6_3/mmc$ 2(c) $\frac{1}{3}, \frac{2}{3}, \frac{1}{4}$	$c/a = \frac{2}{3}\sqrt{6}$	<i>a</i>	(001) 3 ⁶	3, 3 2	0.7405
2	12	$Fm\bar{3}m$ 4(a) 0, 0, 0	-	$\frac{1}{2}\sqrt{2}a$	{111} 3 ⁶ {001} 4 ⁴	3, 3 3 4, 4 2	
3	11	$Cmca$ 8(f) 0, <i>y</i> , <i>z</i>	$y = \frac{1}{6}, z = \frac{3}{2}\sqrt{2} - 2$ $b/a = \sqrt{3}, c/a = \frac{2}{3}\sqrt{6} + \sqrt{3}$	<i>a</i>	(001) 3 ⁶	3, 2 4	0.7187
4	11	$P3_121$ 6(c) <i>x</i> , <i>y</i> , <i>z</i>	$x = \frac{1}{2}, y = \frac{5}{6}, z = \sqrt{2} - \frac{4}{3}$ $c/a = \sqrt{6} + \frac{3}{2}\sqrt{3}$	<i>a</i>	(001) 3 ⁶	3, 2 6	
5	11	$Fdd2$ 16(b) <i>x</i> , <i>y</i> , <i>z</i>	$x = \frac{1}{6}, y = \frac{3}{4}\sqrt{2} - 1, z = 0$ $b/a = \frac{4}{3}\sqrt{2} + 2, c/a = \frac{1}{3}\sqrt{3}$	<i>c</i>	(010) 3 ⁶	3, 2 8	
6	11	$P6_522$ 12(c) <i>x</i> , <i>y</i> , <i>z</i>	$x = \frac{1}{6}, y = \frac{1}{3}, z = \frac{1}{2}\sqrt{2} - \frac{2}{3}$ $c/a = 2\sqrt{6} + 3\sqrt{3}$	<i>a</i>	(001) 3 ⁶	3, 2 12	
7	11	$C2/m$ 4(i) <i>x</i> , 0, <i>z</i>	$x = \frac{1}{2}\sqrt{2} - \frac{1}{2}, z = 3\sqrt{2} - 4$ $b/a = \frac{1}{3}\sqrt{3}, c/a = \frac{1}{6}\sqrt{6} + \frac{1}{3}\sqrt{3}$ $\cos \beta = \frac{1}{6}\sqrt{6} - \frac{1}{3}\sqrt{3}$	<i>b</i>	(001) 3 ⁶	3, 2 12	
8	11	$P4_2/mnm$ 4(f) <i>x</i> , <i>x</i> , 0	$x = \frac{1}{2}\sqrt{2} - \frac{1}{2}, c/a = 2 - \sqrt{2}$	<i>c</i>	-	-	0.7187
9	10	$I4/mmm$ 2(a) 0, 0, 0	$c/a = \frac{1}{3}\sqrt{6}$	<i>c</i>	{110} 3 ⁶	2, 2 2	0.6981
10	10	$P6_222$ 3(c) $\frac{1}{2}, 0, 0$	$c/a = \frac{3}{2}\sqrt{3}$	<i>a</i>	(001) 3 ⁶	2, 2 3	
11	10	$Fddd$ 8(a) 0, 0, 0	$b/a = \sqrt{3}, c/a = 2\sqrt{3}$	<i>a</i>	(001) 3 ⁶	2, 2 4	
12	10	$Fddd$ 16(g) $\frac{1}{8}, \frac{1}{8}, z$	$z = \frac{5}{16}, b/a = \sqrt{3}, c/a = 4\sqrt{3}$	<i>a</i>	(001) 3 ⁶	2, 2 8	
13	10	$Cmcm$ 4(c) 0, <i>y</i> , $\frac{1}{4}$	$y = \frac{3}{10}, b/a = \frac{1}{3}\sqrt{15}, c/a = \frac{2}{5}\sqrt{10}$	$\frac{1}{3}\sqrt{6}a$	(001) 4 ⁴	3, 3 2	0.6981
14	10	$Pnma$ 4(c) <i>x</i> , $\frac{1}{4}, z$	$x = \frac{7}{20}, z = \frac{7}{8}, b/a = \frac{4}{5}, c/a = \frac{2}{15}\sqrt{15}$	<i>c</i>	(010) 4 ⁴	3, 3 2	
15	10	$P6_3/mmc$ 4(f) $\frac{1}{3}, \frac{2}{3}, z$	$z = \frac{3}{4} - \frac{1}{4}\sqrt{6}, c/a = \frac{2}{3}\sqrt{6} + 2$	<i>a</i>	(001) 3 ⁶	3, 1 4	0.6657
16	10	$R\bar{3}m$ 6(c) 0, 0, <i>z</i>	$z = \frac{1}{2} - \frac{1}{6}\sqrt{6}, c/a = \sqrt{6} + 3$	<i>a</i>	(001) 3 ⁶	3, 1 6	
17	10	$Cmcm$ 4(c) 0, <i>y</i> , $\frac{1}{4}$	$y = \frac{3}{4} - \frac{1}{4}\sqrt{6},$ $c/a = 1, b/a = \sqrt{3} + \sqrt{2}$	<i>a</i>	(010) 4 ⁴	4, 2 4	0.6657
18	10	$I4_1/amd$ 8(e) 0, 0, <i>z</i>	$z = \frac{1}{2} - \frac{1}{8}\sqrt{6}, c/a = 2\sqrt{3} + 2\sqrt{2}$	<i>a</i>	(001) 4 ⁴	4, 2 8	
19	10	$I4/m$ 8(h) <i>x</i> , <i>y</i> , 0	$x = \frac{6}{17} - \frac{1}{17}\sqrt{2}, y = \frac{7}{17} - \frac{4}{17}\sqrt{2}$ $c/a = (\frac{14}{17} - \frac{8}{17}\sqrt{2})^{1/2}$	<i>c</i>	-	-	0.6619
20	10	$R\bar{3}$ 18(f) <i>x</i> , <i>y</i> , <i>z</i>	$x = \frac{3}{7}, y = \frac{1}{7}, z = 0, c/a = \frac{1}{7}\sqrt{42}$	$\frac{1}{7}\sqrt{7}a$	(001) 3 ⁴ 6	3, 2 3	0.6347
21	4	$Fd\bar{3}m$ 32(e) <i>x</i> , <i>x</i> , <i>x</i>	$x = \frac{3}{8} - \frac{1}{8}\sqrt{6}$	$(\frac{3}{4}\sqrt{2} - \frac{1}{2}\sqrt{3})a$	-	-	0.1235
22	4	$Im\bar{3}m$ 48(j) 0, <i>y</i> , <i>z</i>	$y = \frac{4}{7} - \frac{3}{28}\sqrt{2}, z = \frac{5}{14} - \frac{1}{28}\sqrt{2}$	$(\frac{3}{14}\sqrt{2} - \frac{1}{7})a$	-	-	0.1033
23	4	$I4_132$ 48(i) <i>x</i> , <i>y</i> , <i>z</i>	$x = y = \frac{1}{8}\sqrt{2}, z = 0$	$(\frac{1}{2} - \frac{1}{4}\sqrt{2})a$	-	-	0.0789
24	3	$I4_132$ 24(h) $\frac{1}{8}, y, \frac{1}{4} - y$	$y = \frac{1}{4}\sqrt{3} - \frac{3}{8}$	$(\frac{1}{2}\sqrt{6} - \frac{3}{4}\sqrt{2})a$	-	-	0.0555