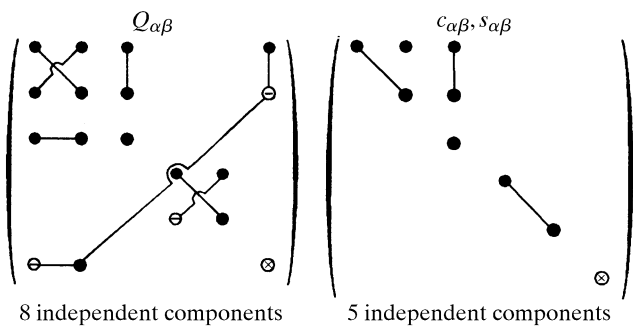
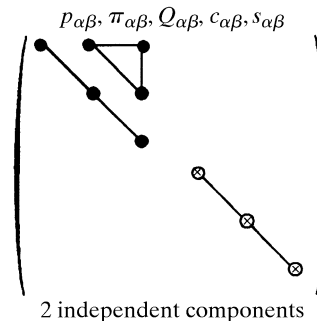


1.1. INTRODUCTION TO THE PROPERTIES OF TENSORS

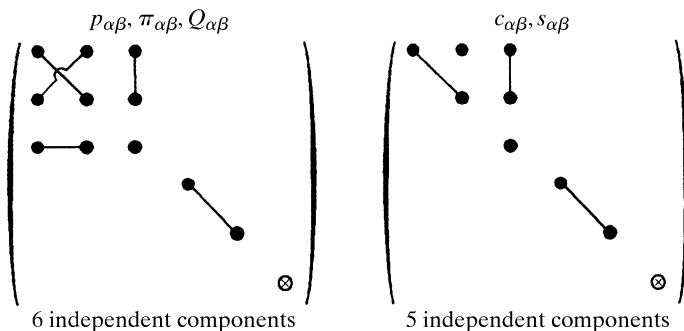


1.1.4.10.6.8. Spherical system

For all tensors



(ii) Groups 622, 6mm, 6̄2m and 6/mmm:



1.1.4.10.7. Reduction of the number of independent components of axial tensors of rank 2

It was shown in Section 1.1.4.5.3.2 that axial tensors of rank 2 are actually tensors of rank 3 antisymmetric with respect to two indices. The matrix of independent components of a tensor such that

$$g_{ijk} = -g_{jik}$$

is given by

$$\left(\begin{array}{ccc|ccc|cc} & 122 & 133 & 123 & 131 & & 132 & & 121 \\ -121 & & 223 & & 231 & -122 & 232 & -123 & \\ -131 & -232 & & -233 & & -132 & & -133 & -231 \end{array} \right).$$

The second-rank axial tensor g_{kl} associated with this tensor is defined by

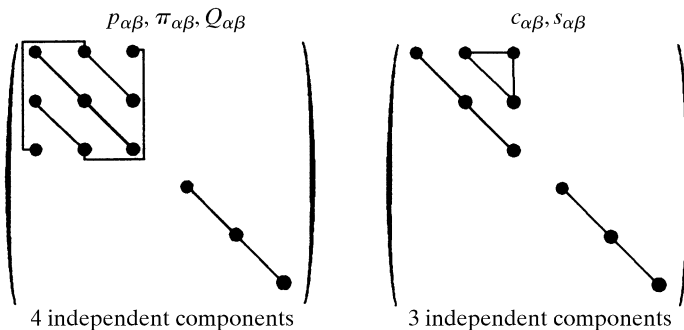
$$g_{kl} = \frac{1}{2} \epsilon_{ijk} g_{ijl}$$

For instance, the piezomagnetic coefficients that give the magnetic moment M_i due to an applied stress T_α are the components of a second-rank axial tensor, $\Lambda_{i\alpha}$ (see Section 1.5.7.1):

$$M_i = \Lambda_{i\alpha} T_\alpha$$

1.1.4.10.6.7. Cubic system

(i) Groups 23 and 3m:



1.1.4.10.7.1. Independent components according to the following point groups

(i) Triclinic system

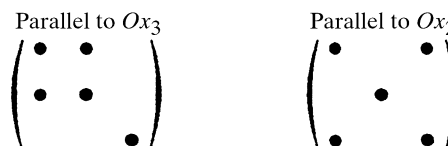
(a) Group 1:



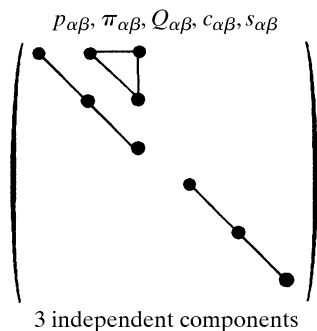
(b) Group $\bar{1}$: all components are equal to zero.

(ii) Monoclinic system

(a) Group 2:

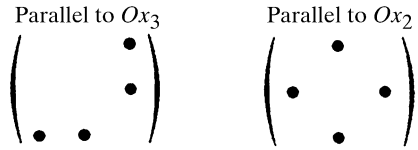


(ii) Groups 432, 4̄3m and m3̄m:

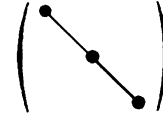


1. TENSORIAL ASPECTS OF PHYSICAL PROPERTIES

(b) Group m :



(v) Cubic and spherical systems
(a) Groups 23, 432 and ∞A_∞ :



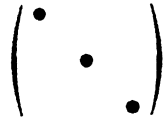
(c) Group $2/m$: all components are equal to zero.

The axial tensor is reduced to a pseudoscalar.

(iii) Orthorhombic system

(b) Groups $m\bar{3}$, $43m$, $m\bar{3}m$ and $\infty(A_\infty/M)C$: all components are equal to zero.

(a) Group 222:



1.1.4.10.7.2. Independent components of symmetric axial tensors according to the following point groups

Some axial tensors are also symmetric. For instance, the optical rotatory power of a gyrotropic crystal in a given direction of direction cosines $\alpha_1, \alpha_2, \alpha_3$ is proportional to a quantity G defined by (see Section 1.6.5.4)

$$G = g_{ij}\alpha_i\alpha_j,$$

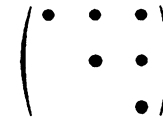
(b) Group $mm2$:



where the gyration tensor g_{ij} is an axial tensor. This expression shows that only the symmetric part of g_{ij} is relevant. This leads to a further reduction of the number of independent components:

(i) Triclinic system

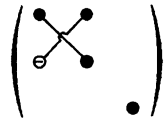
(a) Group 1:



(c) Group mmm : all components are equal to zero.

(iv) Trigonal, tetragonal, hexagonal and cylindrical systems

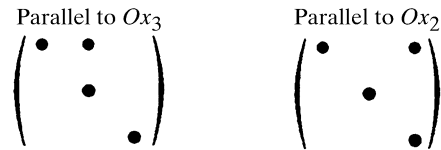
(a) Groups 3, 4, 6 and A_∞ :



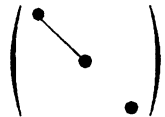
(b) Group $\bar{1}$: all components are equal to zero.

(ii) Monoclinic system

(a) Group 2:



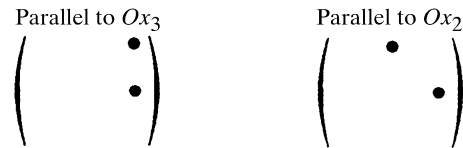
(b) Groups 32, 42, 62 and $A_\infty \infty A_2$:



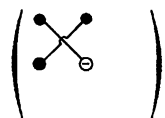
(c) Groups $3m$, $4m$, $6m$ and $A_\infty \infty M$:



(b) Group m :



(d) Group $\bar{4}$:



(c) Group $2/m$: all components are equal to zero.

(iii) Orthorhombic system

(a) Group 222:



(e) Group $\bar{4}2m$:



(b) Group $mm2$:



(f) Groups $\bar{3}$, $4/m$, $\bar{6}2m$, $\bar{3}m$, $4/m\bar{m}$ and $6/m\bar{m}$: all components are equal to zero.

(c) Group mmm : all components are equal to zero.