

1. TENSORIAL ASPECTS OF PHYSICAL PROPERTIES

Table 1.5.10.1. Conversion of Gaussian to SI units

Symbol	Quantity	Gaussian unit and its SI equivalent
<b>B</b>	Magnetic induction	1 gauss (G) = 10 <sup>-4</sup> tesla (T)
<b>H</b>	Magnetic field	1 oersted (Oe) = 10 <sup>3</sup> /(4π) A m <sup>-1</sup>
<b>M</b>	Magnetization (= magnetic moment per unit volume)	1 emu cm <sup>-3</sup> = 10 <sup>3</sup> A m <sup>-1</sup>
$\alpha$	Linear magnetoelectric tensor (rationalized units)	1 (dimensionless units) = 4π × 10 <sup>-8</sup> /3 s m <sup>-1</sup>
$\Lambda$	Piezomagnetic tensor	1 Oe <sup>-1</sup> = 4π × 10 <sup>-3</sup> m A <sup>-1</sup> = 4π × 10 <sup>-3</sup> T Pa <sup>-1</sup>
$\chi$	Magnetic volume susceptibility	1 (dimensionless units) = 4π (dimensionless units)
$\chi_g$	Magnetic mass susceptibility	1 cm <sup>3</sup> g <sup>-1</sup> = 4π × 10 <sup>-6</sup> m <sup>3</sup> g <sup>-1</sup>
$\chi_{mol}$	Magnetic molar susceptibility	1 cm <sup>3</sup> mol <sup>-1</sup> = 4π × 10 <sup>-6</sup> m <sup>3</sup> mol <sup>-1</sup>

We used here the modified equation (1.5.9.7):

$$\frac{1}{2}c_{ijkl}S_{ij}^*S_{kl}^* = -\frac{1}{2}V_{ij}^0S_{ij}^* \quad (1.5.9.30)$$

Substituting the values for the spontaneous magnetostriction, the final equation for the anisotropy energy measured at atmospheric pressure may be written as

$$\begin{aligned} U_a &= U_a^0 + \frac{1}{2}V_{ij}^0S_{ij}^* \\ &= (K_{ij}^0 + K'_{ij})n_i n_j + (K_{ijkl}^0 + K'_{ijkl})n_i n_j n_k n_l \\ &\quad + (K_{ijklmn}^0 + K'_{ijklmn})n_i n_j n_k n_l n_m n_n + \dots \end{aligned} \quad (1.5.9.31)$$

As an example, for the ferromagnets with a cubic prototype this equation may be written as

$$U_a = (K_1^0 + K_1')S(n_1^2 n_2^2) + (K_2^0 + K_2')n_1^2 n_2^2 n_3^2. \quad (1.5.9.32)$$

The coefficients  $K_1'$  and  $K_2'$  may be expressed in terms of the saturation magnetostriction constants  $h_0, \dots, h_5$  [see (1.5.9.12)] and the elastic stiffnesses  $c_{\alpha\beta}$ :

$$\begin{aligned} K_1' &= c_{11}[h_0(2h_4 - 3h_3) + h_1(h_1 - h_3 + 3h_4) - h_4(h_3 - 2h_4)] \\ &\quad + c_{12}[2h_0(2h_4 - 3h_3) - (h_1 + h_4)(h_1 + 2h_3)] - \frac{1}{2}c_{44}h_2^2, \end{aligned} \quad (1.5.9.33)$$

$$\begin{aligned} K_2' &= -c_{11}[3h_4(h_1 + h_3) + (h_4 - h_3)(4h_4 - 3h_3)] \\ &\quad + c_{12}[3h_4(h_1 + h_3) + h_3(5h_4 - 6h_3)] \\ &\quad - \frac{1}{2}c_{44}(6h_2 + h_5)h_5. \end{aligned} \quad (1.5.9.34)$$

For cubic crystals,  $K_1^0$  and  $K_1'$  are of the same magnitude. As an example, for Ni one has  $K_1^0 = 80\,000 \text{ erg cm}^{-3} = 8000 \text{ J m}^{-3}$  and  $K_1' = -139\,000 \text{ erg cm}^{-3} = -13\,900 \text{ J m}^{-3}$ .

1.5.10. Transformation from Gaussian to SI units

Numerical values of magnetic quantities are given in Gaussian units in this chapter. For each quantity that appears in a table or figure, Table 1.5.10.1 gives the corresponding Gaussian unit and its value expressed in SI units. More details on the transformation between Gaussian and SI units are given e.g. in the Appendix of Jackson (1999).

1.5.11. Glossary

$\alpha_{ij}$	(linear) magnetoelectric tensor
$\beta_{ijk}$	nonlinear magnetoelectric tensor <i>EHH</i>
$\gamma_{ijk}$	nonlinear magnetoelectric tensor <i>HEE</i>
$\Delta$	Weiss constant
$\Delta n$	magnetic birefringence
$\epsilon_{ij}$	dielectric permittivity
$\lambda$	constant describing magnetostriction
$\Lambda_{ijk}$	tensor describing the piezomagnetic effect
$\Lambda_{i\alpha}$	matrix describing the piezomagnetic effect
$\mu_{ij}$	magnetic permeability

$\mu$	magnetic moment
$\mu_B$	Bohr magneton
$\pi_{ijkl}$	piezomagnetoelectric tensor
$\rho(\mathbf{r})$	charge density
$\Phi$	thermodynamic potential
$\chi_{ij}^e$	dielectric susceptibility
$\chi_{ij}, \chi_{ij}^m$	magnetic susceptibility
<b>B</b>	magnetic induction
$c$	speed of light
$c_{ijkl}$	elastic stiffness
$d\tau$	volume element
$e$	charge of the electron
<b>E</b>	electric field
$g$	Landé <i>g</i> -factor
<b>H</b>	magnetic field
$\mathbf{j}(\mathbf{r})$	current density
<b>J</b>	total angular momentum
<b>k</b>	position vector in reciprocal space
$k_B$	Boltzmann factor
$\mathbf{l}_i$	sum of the magnetic moments in a unit cell, in which some of the moments are taken with opposite sign
$\mathbf{L}_i$	antiferromagnetic vector
<b>L</b>	orbital angular momentum (Section 1.5.1.1), antiferromagnetic vector (remainder of this chapter)
$\mathbf{m}(\mathbf{r})$	magnetic moment density
<b>m</b>	sum of the magnetic moments in a unit cell
<b>M</b>	magnetization (= magnetic moment per unit volume = ferromagnetic vector)
$N$	No. of atoms per unit volume
$P$	effective number of Bohr magnetons (Section 1.5.1), pressure (remainder of this chapter)
<b>P</b>	electric polarization
<b>r</b>	position vector in space
<b>S(r)</b>	spin density
<b>S</b>	spin angular momentum (of an atom or ion)
$s_{ijkl}$	elastic compliance
$S_{ij}$	strain tensor
$T_{ij}$	stress tensor
$T$	temperature
$T_c$	transition temperature, in particular Curie temperature
$T_N$	Néel temperature
$U$	energy
$U_a$	anisotropy energy
$U_{el}$	elastic energy
$U_{me}$	magnetoelastic energy
$v$	velocity
$Z$	atomic number (= number of electrons per atom)

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