

1.7. NONLINEAR OPTICAL PROPERTIES

The intracavity SHG conversion efficiency is usually defined as the ratio of the SH output power to the maximum output power that would be obtained from the laser without the nonlinear crystal by optimal linear output coupling.

Maximizing (1.7.3.67) with respect to K according to (1.7.3.62), (1.7.3.65) and (1.7.3.66) gives (Perkins & Fahlen, 1987)

$$K_{\text{opt}} = (\gamma_L + \gamma_{NL})S \quad (1.7.3.68)$$

and

$$P_{\text{out}}^{\text{max}}(2\omega) = (1/2S)[(2g_o L')^{1/2} - (\gamma_L + \gamma_{NL})^{1/2}]^2. \quad (1.7.3.69)$$

(1.7.3.69) shows that for the case where $\gamma_{NL} \ll \gamma_L$ ($\gamma \simeq \gamma_L$), the maximum SH power is identically equal to the maximum fundamental power, (1.7.3.64), available from the same laser for the same value of loss, which, according to the previous definition of the intracavity efficiency, corresponds to an SHG conversion efficiency of 100%. $P_{\text{out}}^{\text{max}}(2\omega)$ strongly decreases as the losses ($\gamma_L + \gamma_{NL}$) increase. Thus an efficient intracavity device requires the reduction of all losses at ω and 2ω to an absolute minimum.

(1.7.3.68) indicates that K_{opt} is independent of the operating power level of the laser, in contrast to the optimum transmitting mirror where T_{opt} , given by (1.7.3.63), depends on the laser gain. K_{opt} depends only on the total losses and saturation parameter. For given losses, the knowledge of K_{opt} allows us to define the optimal parameters of the nonlinear crystal, in particular the figure of merit, $d_{\text{eff}}^2/n_3^2 n_1^2 n_2^2$ and the ratio $(L/w_o)^2$, in which the walk-off effect and the damage threshold must also be taken into account.

Some examples: a power of 1.1 W at 0.532 μm was generated in a TEM₀₀ c.w. SHG intracavity device using a 3.4 mm Ba₂NaNb₅O₁₅ crystal within a 1.064 μm Nd:YAG laser cavity (Geusic *et al.*, 1968). A power of 9.0 W has been generated at 0.532 μm using a more complicated geometry based on an Nd:YAG intracavity-lens folded-arm cavity configuration using KTP (Perkins & Fahlen, 1987). High-average-power SHG has also been demonstrated with output powers greater than 100 W at 0.532 μm in a KTP crystal inside the cavity of a diode side-pumped Nd:YAG laser (LeGarrec *et al.*, 1996).

For type-II phase matching, a rotated quarter waveplate is useful in order to reinstate the initial polarization of the fundamental waves after a round trip through the nonlinear crystal, the retardation plate and the mirror (Perkins & Driscoll, 1987).

If the nonlinear crystal surface on the laser medium side has a 100% reflecting coating at 2ω and if the other surface is 100% transmitting at 2ω , it is possible to extract the full SH power in one direction (Smith, 1970). Furthermore, such geometry allows us to avoid losses of the backward SH beam in the laser medium and in other optical components behind.

External-cavity SHG also leads to good results. The resonated wave may be the fundamental or the harmonic one. The corresponding theoretical background is detailed in Ashkin *et al.* (1966). For example, a bow-tie configuration allowed the generation of 6.5 W of TEM₀₀ c.w. 0.532 μm radiation in a 6 mm LiB₃O₅ (LBO) crystal; the Nd:YAG laser was an 18 W c.w. laser with an injection-locked single frequency (Yang *et al.*, 1991).

1.7.3.3.3. Third harmonic generation (THG)

Fig. 1.7.3.16 shows the three possible ways of achieving THG: a cascading interaction involving two $\chi^{(2)}$ processes, *i.e.* $\omega + \omega = 2\omega$ and $\omega + 2\omega = 3\omega$, in two crystals or in the same crystal, and direct THG, which involves $\chi^{(3)}$, *i.e.* $\omega + \omega + \omega = 3\omega$.

1.7.3.3.3.1. SHG ($\omega + \omega = 2\omega$) and SFG ($\omega + 2\omega = 3\omega$) in different crystals

We consider the case of the situation in which the SHG is phase-matched with or without pump depletion and in which the sum-frequency generation (SFG) process ($\omega + 2\omega = 3\omega$), phase-

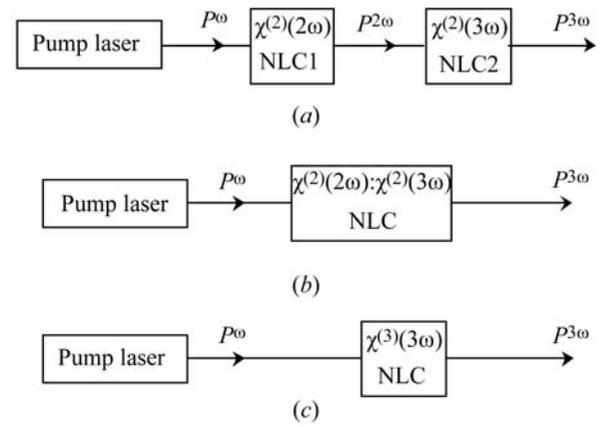


Fig. 1.7.3.16. Configurations for third harmonic generation. (a) Cascading process SHG ($\omega + \omega = 2\omega$): SFG ($\omega + 2\omega = 3\omega$) in two crystals NLC1 and NLC2 and (b) in a single nonlinear crystal NLC; (c) direct process THG ($\omega + \omega + \omega = 3\omega$) in a single nonlinear crystal NLC.

matched or not, is without pump depletion at ω and 2ω . All the waves are assumed to have a flat distribution given by (1.7.3.36) and the walk-off angles are nil, in order to simplify the calculations.

This configuration is the most frequently occurring case because it is unusual to get simultaneous phase matching of the two processes in a single crystal. The integration of equations (1.7.3.22) over Z for the SFG in the undepleted pump approximation with $E_1^\omega(Z_{\text{SFG}} = 0) = E_1^\omega(L_{\text{SHG}})$, $E_2^{2\omega}(Z_{\text{SFG}} = 0) = E_2^{2\omega}(L_{\text{SHG}})$ and $E_3^{3\omega}(Z_{\text{SFG}} = 0) = 0$, followed by the integration over the cross section leads to

$$P^{3\omega}(L_{\text{SFG}}) = B_{\text{SFG}}[aP^\omega(L_{\text{SHG}})]P^{2\omega}(L_{\text{SHG}}) \frac{L_{\text{SFG}}^2}{w_o^2} \sin^2 c^2 \frac{\Delta k_{\text{SFG}} L_{\text{SFG}}}{2} \quad (\text{W})$$

with

$$B_{\text{SFG}} = \frac{72\pi 2N - 1}{\epsilon_o c} \frac{d_{\text{eff}}^2}{N} \frac{T_3^{3\omega} T_1^\omega T_2^{2\omega}}{\lambda_\omega^2 n_3^3 n_1^\omega n_2^{2\omega}} \quad (\text{W}^{-1})$$

$$a = 1 \text{ for type-I SHG, } a = \frac{1}{2} \text{ for type-II SHG.} \quad (1.7.3.70)$$

$P^\omega(L_{\text{SHG}})$ and $P^{2\omega}(L_{\text{SHG}})$ are the fundamental and harmonic powers, respectively, at the exit of the first crystal. L_{SHG} and L_{SFG} are the lengths of the first and the second crystal, respectively. $\Delta k_{\text{SFG}} = k^{3\omega} - (k^\omega + k^{2\omega})$ is the SFG phase mismatch. λ_ω is the fundamental wavelength. The units and other parameters are as defined in (1.7.3.42).

For type-II SHG, the fundamental waves are polarized in two orthogonal vibration planes, so only half of the fundamental power can be used for type-I, -II or -III SFG ($a = 1/2$), in contrast to type-I SHG ($a = 1$). In the latter case, and for type-I SFG, it is necessary to set the fundamental and second harmonic polarizations parallel.

The cascading conversion efficiency is calculated according to (1.7.3.61) and (1.7.3.70); the case of type-I SHG gives, for example,

$$\eta_{\text{THG}}(L_{\text{SHG}}, L_{\text{SFG}}) = \frac{P^{3\omega}(L_{\text{SFG}})}{P_{\text{tot}}^\omega(0)} = B_{\text{SFG}}(T^\omega)^4 P_{\text{tot}}^\omega(0) \tanh^2(\Gamma L_{\text{SHG}}) \times \text{sech}^2(\Gamma L_{\text{SHG}}) \frac{L_{\text{SFG}}^2}{w_o^2} \sin^2 c^2 \left(\frac{\Delta k_{\text{SFG}} L_{\text{SFG}}}{2} \right), \quad (1.7.3.71)$$

where Γ is as in (1.7.3.59).