

1. TENSORIAL ASPECTS OF PHYSICAL PROPERTIES

Table 1.7.5.2. Organic and organo-mineral crystals

Abbreviations for crystals: 5-NU: 5-nitouracil; MAP: methyl-(2,4-dinitrophenyl)-aminopropanoate; MNA: 2-methyl-4-nitroaniline; POM: 3-methyl-4-nitropyridine-*N*-oxide; NPP: *N*-(4-nitrophenyl)-*L*-propranolol; 2A5NPDP: 2-amino-5-nitropyridine dihydrogen phosphate. OPA, OPO and SROPO are abbreviations for optical parametric amplification, oscillation and single resonant optical parametric oscillator, respectively. 1 e.s.u. = 4.19×10^{-4} m V⁻¹.

Crystal	Space group	Transparency	Refractive index phase matching (PM)	Damage threshold
Urea	$P\bar{4}2_1m$	220 nm to 2 μ m	90° type-II PM at 597 nm PM to 238 nm	1.4 GW cm ⁻² at 354.7 nm
5-NU	$P2_12_12_1$	410 nm to 2 μ m	$n_b > n_c > n_a$ Types I and II for SHG and SFG ($\omega + 2\omega \rightarrow 3\omega$)	
MAP	$P2_1$	500 nm to 2 μ m	$n_x < n_y < n_z$ Non-critical PM: at 1.083 μ m (along z); at 1.06 μ m (between room temperature and liquid N ₂)	>3 GW cm ⁻² at 1.06 μ m, 10 ns, 10 Hz >150 MW cm ⁻² at 532 nm, 7 ns, 10 Hz
MNA	Cc	500 nm to 2 μ m	$n_x = 2.093$ and $n_y = 2.494$ at 1.06 μ m	
POM	$P2_12_12_1$	500 nm to 2 μ m	$n_b > n_a > n_c$ Type-I PM tunable from 2 μ m to 0.8 μ m	~1 TW cm ⁻² at 610 nm (10 Hz, 100 fs) 2 GW cm ⁻² at 1.06 μ m (20 ps) 150 MW cm ⁻² at 0.532 μ m (20 ps) 50 MW cm ⁻² at 0.532 μ m (10 ns)
NPP	$P2_1$	500 nm to 2 μ m	$n_y > n_x > n_z$ $n_x - n_z = 0.78$ at 532 nm Non-critical PM at 1.15 μ m $d\theta_{PM}/dT = -0.303$ mrad K ⁻¹	10 GW cm ⁻² at 620 nm (100 fs, 10 Hz)
2A5NPDP	$Pna2_1$	0.420 to 1.7 μ m	$n_x < n_y < n_z$ $n_z - n_x = 0.158$ at 546 nm $n_z - n_y = 0.152$ at 546 nm Type-II non-critical PM at 1.06 μ m at 210 K Type-I ($d_{eff} = 2.25$ pm V ⁻¹) PM at 1.34 μ m Type-II ($d_{eff} = 4.5$ pm V ⁻¹) PM at 1.34 μ m $d\theta_{PM}/dT = -0.137$ mrad K ⁻¹ for type II at 1.34 μ m $d\lambda/dT = 0.176$ nm K ⁻¹ for PM (295 < T < 343 K)	
DAST	Cc	700 nm to 2 μ m	$n_1(720 \text{ nm}) = 2.519$ $n_2(720 \text{ nm}) = 1.720$ $n_3(720 \text{ nm}) = 1.635$	
2A5NPCl	$P2_1$	410 nm to 1.65 μ m	See Horiuchi <i>et al.</i> (2002)	

Crystal	Nonlinear coefficients SHG (d_{ij}) and EO (r_{ij})	OPO/OPA	References†
Urea	$d_{14} = 1.4$ pm V ⁻¹ $r_{41} = 56 \times 10^{-9}$ e.s.u. $r_{63} = 25 \times 10^{-9}$ e.s.u.	SRO $\lambda_p = 354.7$ nm $t_p = 7$ ns Yield: 20.5% Threshold: 45 mW Output: 6 mW at 1.22 μ m Tunability: 0.499 to 1.23 μ m	(a), (b), (c), (d)
5-NU	$d_{14} = d_{25} = d_{36} = 8.7$ pm V ⁻¹ at 1.06 μ m		(e)
MAP	$d_{21} = 40 \pm 5 \times 10^{-9}$ e.s.u. $d_{22} = 44 \pm 5 \times 10^{-9}$ e.s.u. $d_{23} = 8.8 \pm 2 \times 10^{-9}$ e.s.u. $d_{25} = -1.3 \pm 2 \times 10^{-9}$ e.s.u.		(f)
MNA	$d_{11} = 250$ pm V ⁻¹ at 1.06 μ m $d_{11} = 190$ pm V ⁻¹ at 1.2 μ m $d_{11} = 165$ pm V ⁻¹ at 1.3 μ m $d_{11} = 145$ pm V ⁻¹ at 1.47 μ m $d_{11} = 125$ pm V ⁻¹ at 1.54 μ m $(d_{11}^2/n^3)_{MNA} = 2000(d_{11}^2/n^3)_{LiNbO_3}$ $r_{11} = 67 \pm 25$ pm V ⁻¹ at 632.8 nm $\frac{1}{2}(n_1^3 r_{11} - n_3^3 r_{31}) = 270 \pm 50$ pm V ⁻¹		(g), (h), (i)
POM	$d_{14} = d_{25} = d_{36} = 23 \pm 3$ pm V ⁻¹ at 1.06 μ m $r_{41} = 3.6 \pm 0.6$ pm V ⁻¹ at 632.8 nm $r_{52} = 5.1 \pm 0.4$ pm V ⁻¹ at 632.8 nm $r_{63} = 2.6 \pm 0.3$ pm V ⁻¹ at 632.8 nm	OPA: $G = 10^3$ $\lambda_p = 532$ nm, 10 Hz, 25 ps $I_p = 130$ MW cm ⁻² Infrared input: 5 kW cm ⁻² at degeneracy	(j), (k), (l), (m), (n)
NPP	$d_{21} = 56.5 \pm 5$ pm V ⁻¹ at 1.34 μ m $d_{22} = 18.7 \pm 2$ pm V ⁻¹ at 1.34 μ m $d_{22} = 128$ pm V ⁻¹ at 1.06 μ m $r_{12} = 25.5$ pm V ⁻¹ at 632.8 nm $r_{22} = 24$ pm V ⁻¹ at 632.8 nm $n^3 r_{eff} = 60$ pm V ⁻¹ at 1.34 μ m	OPA: $G \approx 10^4$ at degeneracy (1.24 μ m); pump: 620 nm, 100 fs, 10 Hz OPO, λ_{pump} tuning: 593 < λ_p < 670 nm, 1000 < $\lambda_{i,s}$ < 1500 nm OPO, birefringence tuning: $\lambda_p = 670$ nm, 900 < $\lambda_{i,s}$ < 1700 nm DRO threshold at 670 nm: 0.45 MW cm ⁻² , pump: 2.3 MW cm ⁻² (60 ns, 10 Hz). Yield: 4.5%, IR _{output} 90 μ J	(m), (o), (p), (q), (r), (s)
2A5NPDP	At 1.34 μ m: $d_{33} = 12 \pm 1$ pm V ⁻¹ , $d_{15} = 6 \pm 1$ pm V ⁻¹ At 1.06 μ m: $d_{24} = 1 \pm 0.4$ pm V ⁻¹ , $d_{15} = 7 \pm 1$ pm V ⁻¹	OPA: $\Gamma = 29 \pm 3$ cm ⁻¹ ($I_p = 30$ GW cm ⁻²); $d_{eff} = 2.6 \pm 0.5$ pm V ⁻¹ ; $\lambda_s = 1.005$ μ m, $\lambda_p = 612$ nm OPA: $\Gamma = 19 \pm 3$ cm ⁻¹ , $G = 10^6$, $\lambda_s = 1$ μ m, $\lambda_i = 1.5$ μ m, $\lambda_p = 612$ nm OPO: λ_{pump} tuning: 565 < λ_p < 590 nm; $\lambda_s \approx 1.003$ μ m; 1286 < λ_i < 1500 nm SRO: threshold: 6 MW cm ⁻² ; $I_p = 37.2$ MW cm ⁻² (7 ns, 10 Hz); yield 3%, IR _{output} 150 μ J	(r), (s), (t), (u)

1.7. NONLINEAR OPTICAL PROPERTIES

Table 1.7.5.2 (cont.)

Crystal	Nonlinear coefficients SHG (d_{ij}) and EO (r_{ij})	OPO/OPA	References†
DAST	$d_{11}(1318 \text{ nm}) = 1010 \text{ pm V}^{-1}$ $d_{11}(1542 \text{ nm}) = 290 \text{ pm V}^{-1}$ $d_{26}(1542 \text{ nm}) = 39 \text{ pm V}^{-1}$ $r_{11}(720 \text{ nm}) = 92 \text{ pm V}^{-1}$ $r_{11}(1313 \text{ nm}) = 53 \text{ pm V}^{-1}$ $r_{11}(1535 \text{ nm}) = 47 \text{ pm V}^{-1}$	Terahertz generation (difference frequency mixing)	(v), (w)
2A5NPCI	$d_{11} = 9 \pm 4 \text{ pm V}^{-1}$ $d_{12} = 8 \pm 3 \text{ pm V}^{-1}$ $d_{13} = 11 \pm 4 \text{ pm V}^{-1}$ $d_{\text{eff}} = 5.1 \text{ pm V}^{-1}$ or 9.7 pm V^{-1}		(x)

† References: (a) Halbout *et al.*, 1979; (b) Morrell *et al.*, 1979; (c) Donaldson & Tang, 1984; (d) Rosker *et al.*, 1985; (e) Puccetti *et al.*, 1993; (f) Oudar & Hierle, 1977; (g) Levine *et al.*, 1979; (h) Lipscomb *et al.*, 1981; (i) Morita *et al.*, 1988; (j) Zyss *et al.*, 1981; (k) Sigelle & Hierle, 1981; (l) Zyss *et al.*, 1985; (m) Ledoux *et al.*, 1987; (n) Josse *et al.*, 1988; (o) Ledoux *et al.*, 1990; (p) Josse *et al.*, 1992; (q) Khodja *et al.*, 1995(b); (r) Khodja, 1995; (s) Zyss *et al.*, 1984; (t) Kotler *et al.*, 1992; (u) Fève *et al.*, 1999; (v) Bosshard, 2000; (w) Kawase *et al.*, 2000; (x) Horiuchi *et al.*, 2002.

conversion occur simultaneously inside the same crystal. An overview of these attractive materials is given in Brenier (2000).

1.7.6. Glossary

μ_0	vacuum magnetic permeability
ϵ_0	permittivity of free space
c	velocity of light in a vacuum
\mathbf{P}	electronic polarization
\mathbf{P}^n	n th order electronic polarization
\mathbf{P}^{NL}	nonlinear polarization
$\chi^{(n)}$	n th order dielectric susceptibility tensor
ϵ	dielectric tensor
n	refractive index
n_x, n_y, n_z	principal refractive indices
(x, y, z)	principal axes of the index surface (optical frame)
n_o, n_e	refractive indices of the ordinary and extraordinary eigen modes
T	transmission coefficient
V	half of the angle between optic axes
ω	laser circular frequency
λ	laser wavelength
φ	laser phase
v_g	laser group velocity
\mathbf{k}	wavevector
\mathbf{u}	unit wavevector
(θ, φ)	spherical coordinates of the wavevector in the optical frame
Π	neutral vibration plane
\mathbf{E}	electric field vector
(\mathbf{e}, E)	unit vector and amplitude of the electric field
\mathbf{D}	dielectric displacement vector
\mathbf{d}	unit dielectric displacement vector
\mathbf{H}	magnetic field vector
\mathbf{S}	Poynting vector
\mathbf{s}	unit Poynting vector
W	work done per unit time
(X, Y, Z)	orthonormal wave frame where Z is along the wavevector
ρ	double refraction angle (walk-off angle)
∇	nabla operator
\otimes	tensorial product
\cdot	tensorial contraction
\times	vectorial product
Q^*	complex conjugate of Q
w_0	laser beam waist radius
Z_R	Rayleigh length of the laser beam
τ	laser pulse half duration
f	repetition rate of the pulsed laser
$P, P(t)$	laser instantaneous power

I	instantaneous laser intensity
\tilde{E}	total energy per laser pulse
\tilde{P}	average laser power
P_c	laser peak power
L	crystal length
$\chi_{\text{eff}}, d_{\text{eff}}$	effective coefficient
$\mathbf{F}^{(n)}$	n th order field tensor
Δk	phase mismatch
η_{SHG}	conversion efficiency of second harmonic generation
G, h	spatial walk-off attenuation functions

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