

Orthorhombic

6. SCANNING TABLES

 Laue class  $D_{2h} - mmm$ 

 No. 59  $Pm\bar{m}n$ 

$$\mathcal{G} = P \begin{matrix} 2_1 & 2_1 & 2 \\ m & m & n \end{matrix} \text{ origin } 2$$

 $D_{2h}^{13}$ 

| Orientation orbit<br>( <i>hkl</i> ) | Conventional basis<br>of the scanning group<br><b>a'</b> <b>b'</b> <b>d</b> | Scanning<br>group<br>$\mathcal{H}$ | Linear<br>orbit<br><b>sd</b>  | Sectional<br>layer group<br>$\mathcal{L}(\mathbf{sd})$                     |                   |
|-------------------------------------|---|------------------------------------|---|--|-------------------|
| (001)                               | <b>a</b> <b>b</b> <b>c</b>  | $Pm\bar{m}n$                       | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$<br>$[\mathbf{sd}, -\mathbf{sd}]$   | $p\bar{m}mn$<br>$p\bar{m}m2 [(\mathbf{a} + \mathbf{b})/4]$                 | L46<br>L23        |
| (100)                               | <b>b</b> <b>c</b> <b>a</b>  | $Pm\bar{m}n$                       | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$<br>$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$<br>$[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $p2_1/m11$<br>$p\bar{m}2m (\mathbf{a}'/4)$<br>$p\bar{m}11 (\mathbf{a}'/4)$ | L15<br>L27<br>L11 |
| (010)                               | <b>c</b> <b>a</b> <b>b</b>  | $Pm\bar{m}n$                       | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$<br>$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$<br>$[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $p12_1/m1$<br>$p2\bar{m}m (\mathbf{b}'/4)$<br>$p1\bar{m}1 (\mathbf{b}'/4)$ | L15<br>L27<br>L11 |

 No. 60  $Pbcn$ 

$$\mathcal{G} = P \begin{matrix} 2_1 & 2 & 2_1 \\ b & c & n \end{matrix}$$

 $D_{2h}^{14}$ 

| Orientation orbit<br>( <i>hkl</i> ) | Conventional basis<br>of the scanning group<br><b>a'</b> <b>b'</b> <b>d</b> | Scanning<br>group<br>$\mathcal{H}$ | Linear<br>orbit<br><b>sd</b>  | Sectional<br>layer group<br>$\mathcal{L}(\mathbf{sd})$           |                   |
|-------------------------------------|---|------------------------------------|---|--|-------------------|
| (001)                               | <b>a</b> <b>b</b> <b>c</b>  | $Pbcn$                             | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$<br>$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$<br>$[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $p2_1/b11$<br>$pb2n$<br>$pb11 (\mathbf{a}/4)$                    | L17<br>L34<br>L12 |
| (100)                               | <b>b</b> <b>c</b> <b>a</b>  | $Pbna$                             | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$<br>$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$<br>$[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $p2/b11$<br>$pb2_1a (\mathbf{a}'/4)$<br>$pb11$                   | L16<br>L33<br>L12 |
| (010)                               | <b>c</b> <b>a</b> <b>b</b>  | $Pnca$                             | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$<br>$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$<br>$[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $p112/a$<br>$p2_12_12 (\mathbf{a}'/4)$<br>$p112 (\mathbf{a}'/4)$ | L07<br>L21<br>L03 |

 No. 61  $Pbca$ 

$$\mathcal{G} = P \begin{matrix} 2_1 & 2_1 & 2_1 \\ b & c & a \end{matrix}$$

 $D_{2h}^{15}$ 

| Orientation orbit<br>( <i>hkl</i> ) | Conventional basis<br>of the scanning group<br><b>a'</b> <b>b'</b> <b>d</b> | Scanning<br>group<br>$\mathcal{H}$ | Linear<br>orbit<br><b>sd</b>                        | Sectional<br>layer group<br>$\mathcal{L}(\mathbf{sd})$ |     |
|-------------------------------------|---|------------------------------------|---|--|-----|
| (001)                               | <b>a</b> <b>b</b> <b>c</b>  | $Pbca$                             | $0\mathbf{d}, \frac{1}{2}\mathbf{d}$                | $p2_1/b11$   | L17 |
| (100)                               | <b>b</b> <b>c</b> <b>a</b>  |                                    | $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$    | $pb2_1a$   | L33 |
| (010)                               | <b>c</b> <b>a</b> <b>b</b>  |                                    | $[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $pb11 (\mathbf{a}'/4)$                                 | L12 |

Auxiliary tables for Laue class  $D_{2h} - mmm$ Centring types  $P$  and  $I$ 

| Orientation orbit<br>( $hkl$ ) | Conventional basis of the scanning group |                             |                              | Auxiliary basis of the scanning group |                    |                    |
|--------------------------------|--|-----------------------------|------------------------------|---------------------------------------|--------------------|--------------------|
|                                | $\mathbf{a}'$                            | $\mathbf{b}'$               | $\mathbf{d}$                 | $\hat{\mathbf{a}}$                    | $\hat{\mathbf{b}}$ | $\hat{\mathbf{c}}$ |
| $(mn0)$                        | $\mathbf{c}$                             | $n\mathbf{a} - m\mathbf{b}$ | $p\mathbf{a} + q\mathbf{b}$  | $\mathbf{a}$                          | $\mathbf{b}$       | $\mathbf{c}$       |
| $(\bar{m}n0)$                  | $\mathbf{c}$                             | $n\mathbf{a} + m\mathbf{b}$ | $-p\mathbf{a} + q\mathbf{b}$ |                                       |                    |                    |
| $(0mn)$                        | $\mathbf{a}$                             | $n\mathbf{b} - m\mathbf{c}$ | $p\mathbf{b} + q\mathbf{c}$  | $\mathbf{b}$                          | $\mathbf{c}$       | $\mathbf{a}$       |
| $(0\bar{m}n)$                  | $\mathbf{a}$                             | $n\mathbf{b} + m\mathbf{c}$ | $-p\mathbf{b} + q\mathbf{c}$ |                                       |                    |                    |
| $(n0m)$                        | $\mathbf{b}$                             | $n\mathbf{c} - m\mathbf{a}$ | $p\mathbf{c} + q\mathbf{a}$  | $\mathbf{c}$                          | $\mathbf{a}$       | $\mathbf{b}$       |
| $(n0\bar{m})$                  | $\mathbf{b}$                             | $n\mathbf{c} + m\mathbf{a}$ | $-p\mathbf{c} + q\mathbf{a}$ |                                       |                    |                    |

Arithmetic class  $222P$ 

| Serial No.    | 16      | 17               | 18               | 19               |
|---------------|---------|------------------|------------------|------------------|
| Group type    | $D_2^1$ | $D_2^2$          | $D_2^3$          | $D_2^4$          |
| Group         | $P222$  | $P222_1$         | $P2_12_12$       | $P2_12_12_1$     |
| $(mn0)$       | $P112$  | $P112_1$         | $P112$           | $P112_1$         |
| $(\bar{m}n0)$ |         |                  |                  | $(\mathbf{a}/4)$ |
| $(0mn)$       |         | $P112$           | $P112_1$         | $P112_1$         |
| $(0\bar{m}n)$ |         |                  | $(\mathbf{b}/4)$ | $(\mathbf{b}/4)$ |
| $(n0m)$       |         | $P112$           | $P112_1$         | $P112_1$         |
| $(n0\bar{m})$ |         | $(\mathbf{c}/4)$ | $(\mathbf{a}/4)$ | $(\mathbf{c}/4)$ |

Arithmetic class  $mm2P$ 

| Serial No.    | 25         | 26         | 27         | 28               | 29               | 30         | 31         | 32               | 33               | 34               |                  |
|---------------|------------|------------|------------|------------------|------------------|------------|------------|------------------|------------------|------------------|------------------|
| Group type    | $C_{2v}^1$ | $C_{2v}^2$ | $C_{2v}^3$ | $C_{2v}^4$       | $C_{2v}^5$       | $C_{2v}^6$ | $C_{2v}^7$ | $C_{2v}^8$       | $C_{2v}^9$       | $C_{2v}^{10}$    |                  |
| Group         | $Pmm2$     | $Pmc2_1$   | $Pcc2$     | $Pma2$           | $Pca2_1$         | $Pnc2$     | $Pmn2_1$   | $Pba2$           | $Pna2_1$         | $Pnn2$           |                  |
| $(mn0)$       | $P112$     | $P112_1$   | $P112$     | $P112$           | $P112_1$         | $P112$     | $P112_1$   | $P112$           | $P112_1$         | $P112$           |                  |
| $(\bar{m}n0)$ |            |            |            |                  |                  |            |            | $(\mathbf{a}/4)$ |                  |                  |                  |
| $(0mn)$       |            | $P11m$     | $P11m$     | $P11b$           | $P11m$           | $P11b$     | $P11n$     | $P11m$           | $P11a$           | $P11n$           | $P11n$           |
| $(0\bar{m}n)$ |            |            |            | $(\mathbf{a}/4)$ | $(\mathbf{a}/4)$ |            |            |                  | $(\mathbf{a}/4)$ | $(\mathbf{a}/4)$ | $(\mathbf{a}/4)$ |
| $(n0m)$       |            | $P11a$     | $P11a$     | $P11b$           | $P11b$           | $P11a$     | $P11n$     | $P11b$           | $P11b$           | $P11n$           |                  |
| $(n0\bar{m})$ |            |            |            |                  | $(\mathbf{b}/4)$ |            |            | $(\mathbf{b}/4)$ | $(\mathbf{b}/4)$ | $(\mathbf{b}/4)$ |                  |

Arithmetic classes  $222I$ ,  $mm2I$  and  $mmmI$ 

| Serial No.    | 23               | 24               | 44            | 45            | 46            | 71            | 72               | 73   | 74            |  |          |
|---------------|------------------|------------------|---------------|---------------|---------------|---------------|------------------|--|---------------|--|----------|
| Group type    | $D_2^8$          | $D_{2v}^9$       | $C_{2v}^{20}$ | $C_{2v}^{21}$ | $C_{2v}^{22}$ | $D_{2h}^{25}$ | $D_{2h}^{26}$    | $D_{2h}^{27}$                              | $D_{2h}^{28}$ |  |          |
| Group         | $I222$           | $I2_12_12_1$     | $Imm2$        | $Iba2$        | $Ima2$        | $Immm$        | $Ibam$           | $Ibca$                                     | $Imma$        |  |          |
| $(mn0)$       | $I112$           | $I112$           | $I112$        | $I112$        | $I112$        | $I112/m$      | $I112/m$         | $I112/b$                                   | $I112/b$      |  |          |
| $(\bar{m}n0)$ |                  | $(\mathbf{b}/4)$ |               |               |               |               |                  |  |               |  |          |
| $(0mn)$       |                  | $I112$           | $I11m$        | $I11b$        | $I11m$        |               |                  |  | $I112/b$      |  | $I112/m$ |
| $(0\bar{m}n)$ |                  | $(\mathbf{c}/4)$ |               |               |               |               | $(\mathbf{a}/4)$ |  |               |  |          |
| $(n0m)$       | $I112$           |                  | $I11a$        | $I11b$        |               | $I112/a$      |                  | $I112/m$                                   |               |  |          |
| $(n0\bar{m})$ | $(\mathbf{a}/4)$ |                  |               |               |               |               |                  | $(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$ |               |  |          |

Arithmetic class  $mmmP$

| Serial No.<br>Group type<br>Group | 47<br>$D_{2h}^1$<br>$Pmmm$ | 48<br>$D_{2h}^2$<br>$Pnnn$                         |          | 49<br>$D_{2h}^3$<br>$Pccm$ | 50<br>$D_{2h}^4$<br>$Pban$              |          |
|-----------------------------------|----------------------------|--|----------|----------------------------|---|----------|
|                                   |                            | Origin 1   | Origin 2 |                            | Origin 1                                | Origin 2 |
| $(mn0)$<br>$(\bar{m}n0)$          | $P112/m$                   | $P112/n$<br>[[ <b>a</b> + <b>b</b> + <b>c</b> ]/4] | $P112/n$ | $P112/m$                   | $P112/n$<br>[[ <b>a</b> + <b>b</b> ]/4] | $P112/n$ |
| $(0mn)$<br>$(0\bar{m}n)$          |                            |  |          | $P112/b$                   | $P112/a$<br>[[ <b>a</b> + <b>b</b> ]/4] | $P112/a$ |
| $(n0m)$<br>$(n0\bar{m})$          |                            |  |          | $P112/a$                   | $P112/b$<br>[[ <b>a</b> + <b>b</b> ]/4] | $P112/b$ |

| Serial No.<br>Group type<br>Group | 51<br>$D_{2h}^5$<br>$Pmma$ | 52<br>$D_{2h}^6$<br>$Pnna$ | 53<br>$D_{2h}^7$<br>$Pmna$ | 54<br>$D_{2h}^8$<br>$Pcca$ | 55<br>$D_{2h}^9$<br>$Pbam$ | 56<br>$D_{2h}^{10}$<br>$Pccn$ |
|-----------------------------------|----------------------------|----------------------------|----------------------------|----------------------------|----------------------------|-------------------------------|
| $(mn0)$<br>$(\bar{m}n0)$          | $P112/a$                   | $P112/a$                   | $P112_1/a$                 | $P112/a$                   | $P112/m$                   | $P112/n$                      |
| $(0mn)$<br>$(0\bar{m}n)$          | $P112_1/m$                 | $P112/n$                   | $P112/m$                   | $P112_1/b$                 | $P112_1/a$                 | $P112_1/b$                    |
| $(n0m)$<br>$(n0\bar{m})$          | $P112/m$                   | $P112_1/n$                 | $P112/n$                   | $P112/a$                   | $P112_1/b$                 | $P112_1/a$                    |

| Serial No.<br>Group type<br>Group | 57<br>$D_{2h}^{11}$<br>$Pbcm$ | 58<br>$D_{2h}^{12}$<br>$Pnmm$ | 59<br>$D_{2h}^{13}$<br>$Pmnn$           |          | 60<br>$D_{2h}^{14}$<br>$Pbcn$ | 61<br>$D_{2h}^{15}$<br>$Pbca$ | 62<br>$D_{2h}^{16}$<br>$Pnma$ |            |   |            |            |            |
|-----------------------------------|-------------------------------|-------------------------------|---|----------|-------------------------------|-------------------------------|-------------------------------|------------|---|------------|------------|------------|
|                                   |                               |                               | Origin 1                                | Origin 2 |                               |                               |                               |            |   |            |            |            |
| $(mn0)$<br>$(\bar{m}n0)$          | $P112_1/m$                    | $P112/m$                      | $P112/n$<br>[[ <b>a</b> + <b>b</b> ]/4] | $P112/n$ | $P112_1/n$                    | $P112_1/a$                    | $P112_1/a$                    |            |   |            |            |            |
| $(0mn)$<br>$(0\bar{m}n)$          |                               |                               |   |          |                               |                               | $P112/a$                      | $P112_1/n$ | $P112_1/m$<br>[[ <b>a</b> + <b>b</b> ]/4] | $P112_1/m$ | $P112_1/a$ | $P112_1/n$ |
| $(n0m)$<br>$(n0\bar{m})$          |                               |                               |   |          |                               |                               | $P112_1/a$                    |            |   | $P112/a$   |            | $P112_1/m$ |

Centring type C

| Orientation orbit<br>( $hkl$ )   | Conventional basis of the scanning group<br><b>a'</b> <b>b'</b> <b>d</b> |   |  | Auxiliary basis of the scanning group<br>$\hat{\mathbf{a}}$ $\hat{\mathbf{b}}$ $\hat{\mathbf{c}}$ |                               |          |
|--|--|---|--|---|-------------------------------|----------|
| $(hk0)$  | <b>c</b>   | $n\hat{\mathbf{a}} - m\hat{\mathbf{b}}$ | $p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$  | $(\mathbf{a} - \mathbf{b})/2$   | $(\mathbf{a} + \mathbf{b})/2$ | <b>c</b> |
| $(\bar{h}k0)$  | <b>c</b>   | $n\hat{\mathbf{a}} + m\hat{\mathbf{b}}$ | $-p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$ |   |                               |          |
| $h$ even, $k$ odd or $h$ odd, $k$ even $\Rightarrow n = h + k, m = h - k$<br>$h, k$ odd $\Rightarrow n = (h + k)/2, m = (h - k)/2$ |  |   |  |   |                               |          |
| $(0mn)$  | <b>a</b>   | $nb - mc$                               | $pb + qc$                                | <b>b</b>  | <b>c</b>                      | <b>a</b> |
| $(0\bar{m}n)$  | <b>a</b>   | $nb + mc$                               | $-pb + qc$                               |   |                               |          |
| $(n0m)$  | <b>b</b>   | $nc - ma$                               | $pc + qa$                                | <b>c</b>  | <b>a</b>                      | <b>b</b> |
| $(n0\bar{m})$  | <b>b</b>   | $nc + ma$                               | $-pc + qa$                               |   |                               |          |