

Laue class $D_{4h} - 4/mmm$

6. SCANNING TABLES

Tetragonal

 No. 140 $I4/mcm$

$$\mathcal{G} = I_{mcm}^{\frac{4}{2} \frac{2}{2} \frac{2}{2}}$$

 D_{4h}^{18}

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group a' b' d	Scanning group \mathcal{H}	Linear orbit sd	Sectional layer group $\mathcal{L}(\mathbf{sd})$	
(001)	a b c	$I4/mcm$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$p4/mbm$ $p4/nbm$ $p4bm$	L63 L62 L56
(100) (010)	b c a -a c b	$Icma$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pbmb$ $pbma [(a' + b')/4]$ $pbm2 (b'/4)$	L38 L45 L24
(110) (1 $\bar{1}$ 0)	(-a+b) c (a+b) (a+b) c (a-b)	$Fmmm$ $[(a' + d)/4]$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$cmme [(a' + b')/4]$ $cmmm (a'/4)$ $cmm2 (a'/4)$	L48 L47 L26

 No. 141 $I4_1/amd$

$$\mathcal{G} = I_{amd}^{\frac{4}{1} \frac{2}{2} \frac{2}{2}} \text{ origin 1}$$

 D_{4h}^{19}

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group a' b' d	Scanning group \mathcal{H}	Linear orbit sd	Sectional layer group $\mathcal{L}(\mathbf{sd})$	
(001)	a b c	$I4_1/amd$ (origin 1)	$[0\mathbf{d}, \frac{1}{2}\mathbf{d};$ $\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\frac{1}{8}\mathbf{d}, \frac{5}{8}\mathbf{d};$ $\frac{3}{8}\mathbf{d}, \frac{7}{8}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{4})\mathbf{d},$ $(\pm s + \frac{1}{2})\mathbf{d}, (\pm s + \frac{3}{4})\mathbf{d}]$	$p\bar{4}m2$ $p\bar{4}m2 (a/2 \text{ or } b/2)$ $pmmb (b/4)$ $pmma (a/4)$ $pmm2$	L59 L59 L41 L41 L23
(100) (010)	b c a -a c b	$Imcm$ $(a'/4 + b'/8)$ $Imcm$ $(a'/4 + 3b'/8)$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$ $[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pmam (a'/4 + b'/8)$ $pman (b'/8)$ $pma2 (a'/4 + b'/8)$ $pmam (a'/4 + 3b'/8)$ $pman (b'/8)$ $pma2 (a'/4 + 3b'/8)$	L40 L42 L24 L40 L42 L24
(110) (1 $\bar{1}$ 0)	(-a+b) c (a+b) (a+b) c (a-b)	$Fddd$ (or. 1) or $Fddd$ (or. 2) $[(a' + b' + d)/8]$ $Fddd$ (or. 1) $[(a' + b' + d)/4]$ or $Fddd$ (or. 2) $[3(a' + b' + d)/8]$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d};$ $\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\frac{1}{8}\mathbf{d}, \frac{5}{8}\mathbf{d};$ $\frac{3}{8}\mathbf{d}, \frac{7}{8}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{4})\mathbf{d};$ $(\pm s + \frac{1}{2})\mathbf{d}, (\pm s + \frac{3}{4})\mathbf{d}]$ $[0\mathbf{d}, \frac{1}{2}\mathbf{d};$ $\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\frac{1}{8}\mathbf{d}, \frac{5}{8}\mathbf{d};$ $\frac{3}{8}\mathbf{d}, \frac{7}{8}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{4})\mathbf{d};$ $(\pm s + \frac{1}{2})\mathbf{d}, (\pm s + \frac{3}{4})\mathbf{d}]$	$c222$ $c222 [(a' + b')/4]$ $\hat{p}112/b [(a' + b')/8]$ $\hat{p}112/a [(3a' + b')/8]$ or $(a' + 3b')/8$ $\hat{p}112$ $c222$ $c222 [(a' + b')/4]$ $\hat{p}112/a [(3a' + b')/8]$ or $(a' + 3b')/8$ $\hat{p}112/b [(a' + b')/8]$ $\hat{p}112$	L22 L22 L16 L16 L16 L03 L22 L22 L16 L16 L03

No. 141 $I4_1/amd$

$$\mathcal{G} = I_{a m d}^4 \frac{2}{2} \text{ origin 2}$$

 D_{4h}^{19}

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group a' b' d	Scanning group \mathcal{H}	Linear orbit sd	Sectional layer group $\mathcal{L}(s\mathbf{d})$	
(001)	a b c	$I4_1/amd$ (origin 2)	$[0\mathbf{d}, \frac{1}{2}\mathbf{d};$ $\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\frac{1}{8}\mathbf{d}, \frac{5}{8}\mathbf{d};$ $\frac{3}{8}\mathbf{d}, \frac{7}{8}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{4})\mathbf{d},$ $(\pm s + \frac{1}{2})\mathbf{d}, (\pm s + \frac{3}{4})\mathbf{d}]$	$pmm\bar{b}$ $pmma [(a + b)/4]$ $p\bar{4}m2 (3b/4)$ $p\bar{4}m2 (b/4)$ $pmm2 (b/4)$	L41 L41 L59 L59 L23
(100)	b c a	$Imcm$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pmam$ $pman [(a' + b')/4]$ $pma2$	L40 L42 L24
(010)	-a c b	$Imcm$ $[(a' + b' + d)/4]$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pman$ $pman [(a' + b')/4]$ $pma2 [(a' + b')/4]$	L42 L40 L24
(110)	(-a+b) c (a+b)	$Fddd$ (or. 1) $[(a' + 3b' + d)/8]$ or $Fddd$ (or. 2) $[(a' + d)/4]$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d};$ $\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\frac{1}{8}\mathbf{d}, \frac{5}{8}\mathbf{d};$ $\frac{3}{8}\mathbf{d}, \frac{7}{8}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{4})\mathbf{d};$ $(\pm s + \frac{1}{2})\mathbf{d}, (\pm s + \frac{3}{4})\mathbf{d}]$	$\widehat{p}112/a$ $\widehat{p}112/b (a'/4 \text{ or } b'/4)$ $c222 [(a' + 3b')/8]$ $c222 [(3a' + b')/8]$ $\widehat{p}112 [(a' + 3b')/8$ or $(3a' + b')/8]$	L16 L16 L22 L22 L03
($\bar{1}\bar{1}0$)	(a+b) c (a-b)	$Fddd$ (or. 1) $[(3a' + b' + d)/8]$ or $Fddd$ (or. 2) $[(b' + d)/4]$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d};$ $\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\frac{1}{8}\mathbf{d}, \frac{5}{8}\mathbf{d};$ $\frac{3}{8}\mathbf{d}, \frac{7}{8}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{4})\mathbf{d};$ $(\pm s + \frac{1}{2})\mathbf{d}, (\pm s + \frac{3}{4})\mathbf{d}]$	$\widehat{p}112/a$ $\widehat{p}112/b (a'/4 \text{ or } b'/4)$ $c222 [(3a' + b')/8]$ $c222 [(a' + 3b')/8]$ $\widehat{p}112 [(a' + 3b')/4$ or $(3a' + b')/8]$	L16 L16 L22 L22 L03

Arithmetic class $4/mmmP$ (cont.)

Serial No.	135	136	137		138	
Group type	D_{4h}^{13}	D_{4h}^{14}	D_{4h}^{15}		D_{4h}^{16}	
Group	$P4_2/mbc$	$P4_2/mmm$	$P4_2/nmc$		$P4_2/ncm$	
			Origin 1	Origin 2	Origin 1	Origin 2
$(mn0)$	$P112/m$	$P112/m$	$P112/n$	$P112/n$	$P112/n$	$P112/n$
$(\bar{m}0)$					$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$	
$(\bar{m}\bar{n}0)$						
$(nm0)$						
$(0mn)$	$P112_1/a$	$P112_1/n$	$P112_1/m$	$P112_1/m$	$P112_1/b$	$P112_1/b$
$(0\bar{m}\bar{n})$			$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$		$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$	
$(m0n)$	$P112_1/b$				$P112_1/a$	$P112_1/a$
$(m0\bar{n})$					$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$	
(hhl)	$B112/b$	$B112/m$	$B112/b$	$B112/b$	$B112/m$	$B112/m$
$(\bar{h}\bar{h}l)$	$(\mathbf{a}/2 \text{ or } \mathbf{b}/2)$		$(\mathbf{a} - \mathbf{b} + \mathbf{c})/4$		$(\mathbf{a} - \mathbf{b} + \mathbf{c})/4$	
$(h\bar{h}l)$			$B112/b$	$B112/b$	$B112/m$	$B112/m$
$(\bar{h}hl)$			$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$	$(\mathbf{a}/2 \text{ or } \mathbf{b}/2)$	$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$	$(\mathbf{a}/2 \text{ or } \mathbf{b}/2)$

Centring type I

Orientation orbit (hkl)	Conventional basis of the scanning group $\mathbf{a}' \quad \mathbf{b}' \quad \mathbf{d}$			Auxiliary basis of the scanning group $\hat{\mathbf{a}} \quad \hat{\mathbf{b}} \quad \hat{\mathbf{c}}$		
$(mn0)$	\mathbf{c}	$n\mathbf{a} - m\mathbf{b}$	$p\mathbf{a} + q\mathbf{b}$	\mathbf{a}	\mathbf{b}	\mathbf{c}
$(\bar{m}0)$	\mathbf{c}	$m\mathbf{a} + n\mathbf{b}$	$-q\mathbf{a} + p\mathbf{b}$			
$(\bar{m}\bar{n}0)$	\mathbf{c}	$n\mathbf{a} + m\mathbf{b}$	$-p\mathbf{a} + q\mathbf{b}$			
$(nm0)$	\mathbf{c}	$m\mathbf{a} - n\mathbf{b}$	$q\mathbf{a} + p\mathbf{b}$			
$(0mn)$	\mathbf{a}	$n\mathbf{b} - m\mathbf{c}$	$p\mathbf{b} + q\mathbf{c}$	\mathbf{b}	\mathbf{c}	\mathbf{a}
$(0\bar{m}\bar{n})$	\mathbf{a}	$n\mathbf{b} + m\mathbf{c}$	$-p\mathbf{b} + q\mathbf{c}$			
$(m0n)$	\mathbf{b}	$m\mathbf{c} - n\mathbf{a}$	$q\mathbf{c} + p\mathbf{a}$	\mathbf{c}	\mathbf{a}	\mathbf{b}
$(m0\bar{n})$	\mathbf{b}	$m\mathbf{c} + n\mathbf{a}$	$-q\mathbf{c} + p\mathbf{a}$			
(hhl)	$\mathbf{a} - \mathbf{b}$	$n\hat{\mathbf{a}} - m\mathbf{c}$	$p\hat{\mathbf{a}} + q\mathbf{c}$	$(\mathbf{a} + \mathbf{b} + \mathbf{c})/2$	\mathbf{c}	$\mathbf{a} - \mathbf{b}$
$(\bar{h}\bar{h}l)$	$\mathbf{a} - \mathbf{b}$	$n\hat{\mathbf{a}} + m\mathbf{c}$	$-p\hat{\mathbf{a}} + q\mathbf{c}$			
$(h\bar{h}l)$	$\mathbf{a} + \mathbf{b}$	$n\hat{\mathbf{a}} - m\mathbf{c}$	$p\hat{\mathbf{a}} + q\mathbf{c}$	$(\mathbf{b} - \mathbf{a} + \mathbf{c})/2$	\mathbf{c}	$\mathbf{a} + \mathbf{b}$
$(\bar{h}hl)$	$\mathbf{a} + \mathbf{b}$	$n\hat{\mathbf{a}} + m\mathbf{c}$	$-p\hat{\mathbf{a}} + q\mathbf{c}$			

$l \text{ odd} \Rightarrow n = 2l, m = 2h + l; l \text{ even} \Rightarrow n = l, m = h + l/2$

Arithmetic classes $422I$ and $4mmI$

Serial No.	97	98	107	108	109	110
Group type	D_4^9	D_4^{10}	C_{4v}^9	C_{4v}^{10}	C_{4v}^{11}	C_{4v}^{12}
Group	$I422$	$I4_122$	$I4mm$	$I4cm$	$I4_1md$	$I4_1cd$
$(mn0)$	$I112$	$I112$	$I112$	$I112$	$I112$	$I112$
$(\bar{m}0)$						
$(\bar{m}\bar{n}0)$						
$(nm0)$						
$(0mn)$	$I112$	$I112$	$I11m$	$I11b$	$I11m$	$I11b$
$(0\bar{m}\bar{n})$		$(\mathbf{b}/4 + \mathbf{c}/8)$				
$(m0n)$		$I112$		$I11a$		$I11a$
$(m0\bar{n})$		$(\mathbf{a}/4 + 3\mathbf{c}/8)$				
(hhl)	$A112$	$A112$	$A11m$	$A11m$	$A11n$	$A11n$
$(\bar{h}\bar{h}l)$				$(\mathbf{a}/2 \text{ or } \mathbf{b}/2)$	$(\mathbf{a} - \mathbf{b})/8$	$3(\mathbf{a} - \mathbf{b})/8$
$(h\bar{h}l)$					$A11n$	$A11n$
$(\bar{h}hl)$					$3(\mathbf{a} + \mathbf{b})/8$	$(\mathbf{a} + \mathbf{b})/8$

Arithmetic classes $\bar{4}m2I$ and $\bar{4}2mI$

Serial No.	119	120	121	122
Group type	D_{2d}^9	D_{2d}^{10}	D_{2d}^{11}	D_{2d}^{12}
Group	$\bar{I}4m2$	$\bar{I}4c2$	$\bar{I}42m$	$\bar{I}42d$
$(mn0)$	$I112$	$I112$	$I112$	$I112$
$(\bar{n}m0)$				
$(\bar{m}n0)$				
$(nm0)$				
$(0mn)$	$I11m$	$I11b$	$I112$	$I112$
$(0\bar{m}n)$				$(\mathbf{b}/4 + \mathbf{c}/8)$
$(m0n)$		$I11a$		$I112$
$(m0\bar{n})$				$(\mathbf{a}/4 + 3\mathbf{c}/8)$
(hhl)	$A112$	$A112$	$A11m$	$A11n$
$(\bar{h}\bar{h}l)$		$(\mathbf{c}/4)$		$(\mathbf{a} - \mathbf{b})/8$
$(h\bar{h}l)$				$A11n$
$(\bar{h}hl)$				$3(\mathbf{a} + \mathbf{b})/8$

Arithmetic class $4/mmmI$

Serial No.	139	140	141		142	
Group type	D_{4h}^{17}	D_{4h}^{18}	D_{4h}^{19}		D_{4h}^{20}	
Group	$I4/mmm$	$I4/mcm$	$I4_1/amd$		$I4_1acd$	
			Origin 1	Origin 2	Origin 1	Origin 2
$(mn0)$	$A112/a$	$A112/a$	$I112/b$	$I112/b$	$I112/b$	$I112/b$
$(\bar{n}m0)$			$(\mathbf{b} + \mathbf{c})/8$		$(\mathbf{b} + \mathbf{c})/8$	
$(\bar{m}n0)$						
$(nm0)$						
$(0mn)$	$I112/m$	$I112/b$	$I112/m$	$I112/m$	$I112/b$	$I112/b$
$(0\bar{m}n)$			$(\mathbf{b}/4 + \mathbf{c}/8)$		$(\mathbf{b}/4 + \mathbf{c}/8)$	
$(m0n)$		$I112/a$	$I112/m$	$I112/m$	$I112/a$	$I112/a$
$(m0\bar{n})$			$(\mathbf{a}/4 + 3\mathbf{c}/8)$	$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$	$(\mathbf{a}/4 + 3\mathbf{c}/8)$	$(\mathbf{a} + \mathbf{b} + \mathbf{c})/4$
(hhl)	$A112/m$	$A112/m$	$A112/a$	$A112/a$	$A112/a$	$A112/a$
$(\bar{h}\bar{h}l)$			$3(\mathbf{a}/4 + \mathbf{c}/8)$	$(\mathbf{a} - \mathbf{b} + \mathbf{c})/4$	$(\mathbf{a}/4 + 3\mathbf{c}/8)$	
$(h\bar{h}l)$			$A112/a$	$A112/a$	$A112/a$	
$(\bar{h}hl)$			$(\mathbf{a}/4 + \mathbf{c}/8)$	$(\mathbf{a}/2 \text{ or } \mathbf{b}/2)$	$3(\mathbf{a}/4 + \mathbf{c}/8)$	