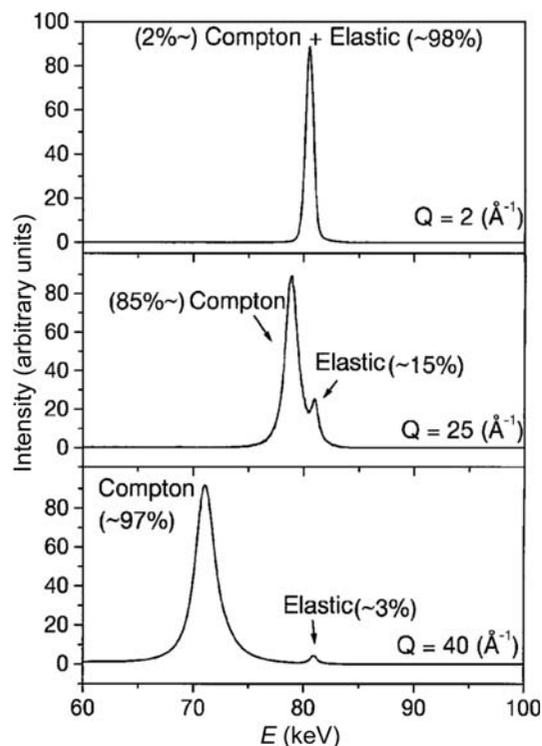1.1. OVERVIEW AND PRINCIPLES

Figure 1.1.24
Spectrum from an energy-resolving detector that shows the elastic and Compton signals as a function of scattering vector **Q**. [Reprinted with permission from Petkov *et al.* (2000). Copyright (2007) by the American Physical Society.]

the non-energy-resolved magnetic diffuse scattering signal. Magnetic PDF is now possible (Frandsen & Billinge, 2015) as described in Chapter 5.7, as well as reciprocal-space studies of magnetic diffuse scattering (Paddison & Goodwin, 2012).

1.1.5.3.4. *Incoherent scattering*

Incoherent scattering does not contain any structural information, and cannot be used to study structure in a diffraction experiment since the intensities of the scattered waves do not depend on the position of the scatterers. This does not mean that all incoherent scattering intensity is useless. The fluorescence intensity is incoherent, but may be used in EXAFS experiments to yield structural information. This is because coherent scattering of the photoexcited electron during an absorption event modulates the absorption cross section and therefore the incoherent fluorescence intensity, so a coherent scattering process leaves a measurable response in an incoherent intensity. Incoherent scattering can also be used to measure excitations, although all momentum-transfer information is lost so it is not possible to measure, for example, dispersions of excitations such as phonons and magnons. Even if the scattering process is incoherent, the energy exchanged between the probe and the sample can be measured by the change in wavelength of the scattered wave, and the amplitude of the scattering at each energy transfer is proportional to the density of states of the excitation being probed. In the case of neutrons, the very large incoherent cross section for scattering by hydrogen ($\sim100\times$ the scattering cross section of most atoms) provides a strong signal for studying low-probability inelastic scattering events. Measuring inelastic scattering from powders can be a rapid way of determining the density of states of phonons, magnons and so on, which is very useful for determining the thermodynamic properties of materials, even though it is less precise than measurement of the full set of dispersion curves.

Another type of incoherent scattering that can be observed in X-ray experiments is Compton scattering (Compton, 1923; Cooper *et al.*, 2004), which is an inelastic incoherent process where the scattering atom recoils during the scattering event. An example of Compton scattering measured in the spectrum from an energy-resolving detector is shown in Fig. 1.1.24.

The Compton scattering is strong in this experiment because the incident X-ray energy is high (80 keV) and the sample is a low-atomic-number alumina-silicate glass. Both the high X-ray energy and the low atomic numbers of the atoms in the sample increase the Compton cross section with respect to the coherent elastic scattering. As the magnitude of the scattering vector, Q, is increased the Compton scattering moves to lower energy and increases in intensity, but the elastic line stays fixed in energy and its intensity decreases because of form-factor and Debye–Waller effects. Momentum as well as energy is conserved in this process and the Compton scattering can be used to measure the momentum distribution of electrons in a material, although this kind of experiment is not widespread these days.

Elastic incoherent scattering provides no information about the sample, and simply degrades the signal-to-noise ratio of the measurement. As such, it is just inconvenient and cannot be easily removed. Monotonic Laue diffuse scattering originates from different chemical species with different scattering powers residing on different sites in the crystal, and when a destructive interference condition is satisfied the resulting intensity does not go to zero but is proportional to $[f_i(h) - f_j(h)]^2$ (Warren, 1990). In pure elements in an X-ray experiment, the atoms on every site are the same and there is no Laue diffuse scattering. This is not true in neutron experiments where different nuclei have different scattering powers and most elements contain a range of isotopes in their natural form (the 'natural abundance'; Squires, 1996). This results in Laue diffuse scattering even in an element, although it is normally not referred to in these terms but is encompassed by a so-called 'incoherent neutron cross section' that is defined and tabulated (see Table 4.4.4.1 in *International Tables for Crystallography*, Volume C) for each element. This is not the only source of incoherent scattering in neutron diffraction, since the scattering power also depends on the relative orientation of the neutron and nuclear spins. In general these spins are all orientationally disordered (and fluctuating) and the result is an additional scattering-event-dependent contribution to the incoherent scattering from the sample, again encompassed by the 'incoherent neutron cross section' of the element. Where necessary, it may be possible to make isotopically enriched samples for neutron experiments so that the proportion of isotopes with large incoherent scattering cross sections is minimized (or the isotopes are removed altogether), and the range of isotopes can also be reduced, which further reduces the incoherent component of the signal. However, the cost and difficulty of doing this means that it is rarely done.

1.1.6. Local and global optimization of crystal structures from powder diffraction data

1.1.6.1. *Rietveld refinement*

More than 40 years have passed since the publication of the pioneering papers by Hugo Rietveld (Rietveld, 1967, 1969), in which he described a method for the refinement of crystal structures from neutron powder diffraction data. Neutron data sets from reactor sources were more amenable than X-ray data sets to this method because the line profiles are quite Gaussian.