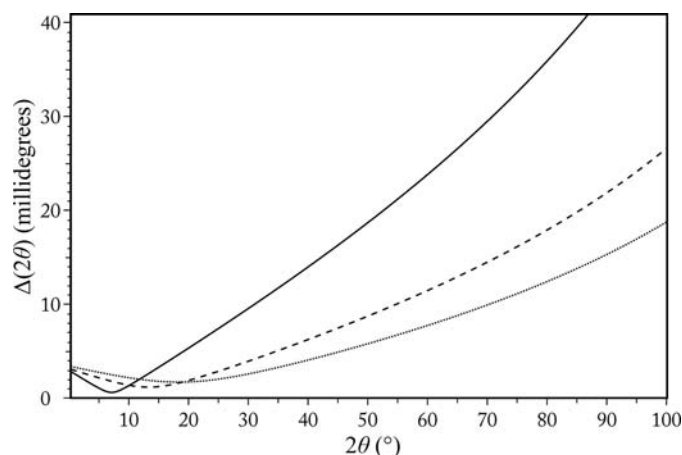


2. INSTRUMENTATION AND SAMPLE PREPARATION


Figure 2.2.11

$\Delta(2\theta)$ calculated from equation (2.2.2) for a beamline with a double-crystal Si(111) monochromator, an Si(111) analyser ($\Delta_m = \Delta_a$ and $\theta_m = \theta_a$) and an FWHM vertical divergence of $25 \mu\text{rad}$ at $\lambda = 0.4 \text{ \AA}$ (solid line: $\Delta_m \simeq 8.3 \mu\text{rad}$, $\theta_m = 3.6571^\circ$), $\lambda = 0.8 \text{ \AA}$ (dashed line: $\Delta_m \simeq 16.6 \mu\text{rad}$, $\theta_m = 7.3292^\circ$) and $\lambda = 1.2 \text{ \AA}$ (dotted line: $\Delta_m \simeq 25.2 \mu\text{rad}$, $\theta_m = 11.0319^\circ$).

$$b = \tan \theta_a / \tan \theta_m - 2 \tan \theta / \tan \theta_m.$$

Here α represents the vertical divergence from the source, δ is the difference between the Bragg angles of a central ray reflected from the monochromator at the angle θ_m and of another ray at angle θ'_m such that $\delta = \theta'_m - \theta_m$, and θ_a is the Bragg angle of the analyser crystal. The terms α'_m , Δ'_m and Δ'_a are related to the FWHM of the Gaussians representing the vertical divergence distribution or the Darwin widths of the monochromator and analyser crystals, α_m , Δ_m and Δ_a , respectively, with

$$\alpha'_m = \alpha_m / 2(\ln 2)^{1/2}, \quad \Delta'_m = \Delta_m / 2(\ln 2)^{1/2}, \quad \Delta'_a = \Delta_a / 2(\ln 2)^{1/2}.$$

From the above equation, the intrinsic FWHM of the Gaussian-approximated peaks of the powder-diffraction pattern can be obtained as

$$\Delta^2(2\theta) = \alpha_m^2 \left(\frac{\tan \theta_a}{\tan \theta_m} - 2 \frac{\tan \theta}{\tan \theta_m} + 1 \right)^2 + \frac{1}{2} \Delta_m^2 \left(\frac{\tan \theta_a}{\tan \theta_m} - 2 \frac{\tan \theta}{\tan \theta_m} \right) + \Delta_a^2. \quad (2.2.2)$$

Note that the true peak shape is not Gaussian, and a pseudo-Voigt (e.g. as described by Thompson *et al.*, 1987), Voigt (e.g. Langford, 1978; David & Matthewman, 1985; Balzar & Ledbetter, 1993) or other function modelled from first principles (e.g. Cheary & Coelho, 1992; Ida *et al.*, 2001, 2003) is usually better. Examples of FWHM curves calculated from equation (2.2.2) are plotted in Fig. 2.2.11 at three wavelengths. Differentiating the Bragg equation gives $\Delta d/d = -\cot \theta \Delta(\theta)$, where θ is in radians.

Gozzo *et al.* (2006) have extended the formulation of Sabine to include the effects of collimating and focusing mirrors in the overall scheme. Axial (horizontal) divergence of the beam between the sample and the detector causes shifts and broadening of the peaks, as well as the well known low-angle peak asymmetry due to the curvature of the Debye–Scherrer cones. Sabine (1987*b*), based on the work of Hewat (1975) and Hastings *et al.* (1984), suggests the magnitude of the broadening, $B(2\theta)$, due to horizontal divergence Φ can be estimated *via*

$$B(2\theta) = \left(\frac{1}{4}\Phi\right)^2 (\cot 2\theta + \tan \theta_a),$$

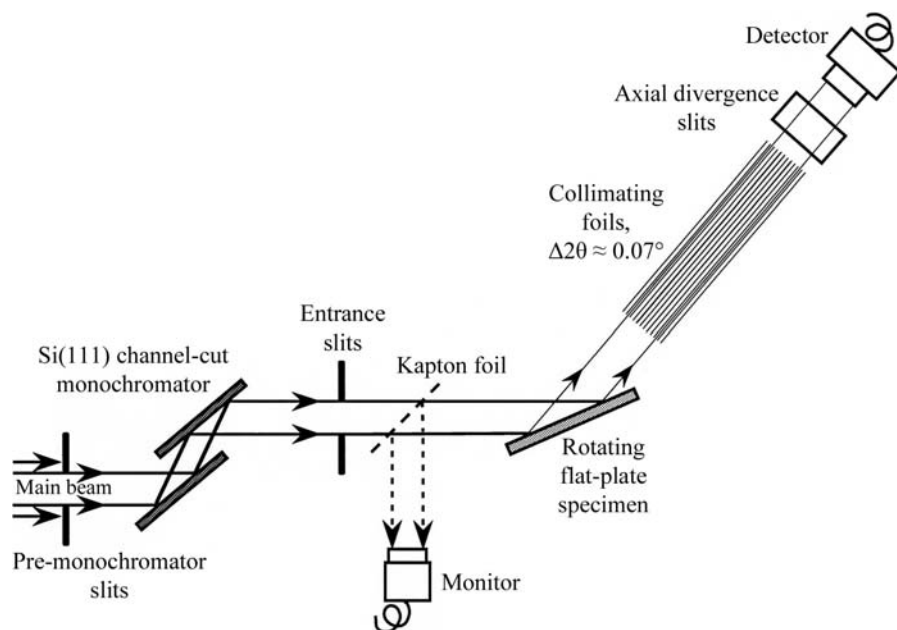
where B and Φ are in radians. This value is added to $\Delta(2\theta)$.

2.2.4.1.2. Hart–Parrish design

A variant of the parallel-beam scheme replaces the analyser crystal with a set of long, fine Soller collimators (Parrish *et al.*, 1986; Parrish & Hart, 1987; Parrish, 1988; Cernik *et al.*, 1990; Collins *et al.*, 1992) (Fig. 2.2.12). The collimators define a true angle of diffraction, but with lower 2θ resolution than an analyser crystal because their acceptance angle is necessarily much larger and so the transmitted intensity is greater. They are not particularly suitable for fine capillary specimens, as the separation between foils may be similar to the capillary diameter, resulting in problems of shadowing of the diffracted beam. However, they are achromatic, and so do not need to be reoriented at each change of wavelength, which may have advantages when performing anomalous-scattering studies around an element's absorption edge. Unlike an analyser crystal, however, they do not suppress fluorescence. Peak shapes and resolution can be influenced by reflection of X-rays from the surface of the foils, or any imperfections in their manufacture, e.g. if the blades are not straight and flat. The theoretical resolution curve of such an instrument can be obtained from equation (2.2.2) by setting $\tan \theta_a$ to zero and replacing the angular acceptance of the analyser crystal Δ_a with the angular acceptance of the collimator Δ_c .

2.2.4.2. Debye–Scherrer instruments

The simplest diffractometer has a receiving slit at a convenient distance from the sample in front of a point detector such as a scintillation counter. The height of the slit should match the capillary diameter, or incident beam height for flat plates. A slightly larger antiscatter slit near the sample should also be employed to reduce


Figure 2.2.12

Schematic representation of a parallel-beam diffractometer of the Hart–Parrish design. The collimators installed on Stations 8.3 and 2.3 at the SRS Daresbury (Cernik *et al.*, 1990; Collins *et al.*, 1992) had steel blades $50 \mu\text{m}$ thick, 355 mm long, separated by 0.2 mm spacers, defining a theoretical opening angle (FWHM Δ_c) of 0.032° and a transmission of 80%.