

## 3.6. WHOLE POWDER PATTERN MODELLING

For cuprite, the literature (Tromans & Meech, 2001) suggests that the main slip system is  $\{001\}\{100\}$ . The contrast factor can be calculated analytically from the single-crystal elastic constants of cuprite ( $c_{11} = 121$ ,  $c_{12} = 105$  and  $c_{44} = 12.1$  GPa; Every & McCurdy, 1992b) following Martinez-Garcia *et al.* (2007):

$$\bar{C}_{\text{Cu}_2\text{O},e} = 0.355963 - 0.609491 \frac{h^2k^2 + k^2l^2 + h^2l^2}{(h^2 + k^2 + l^2)^2}, \quad (3.6.58)$$

$$\bar{C}_{\text{Cu}_2\text{O},s} = \frac{2h^2k^2 + k^2l^2 + h^2l^2}{3(h^2 + k^2 + l^2)^2}. \quad (3.6.59)$$

For tenorite, a different approach was followed. The phase is minor and the single-crystal elastic constants are not readily available: we can therefore use the contrast factor in an effective way by refining the coefficients of the corresponding invariant [see equation (3.6.42)]. This preserves the profile shape determined by Wilkens' theory and just dilutes the meaning of the dislocation density. The average contrast factor is

$$\begin{aligned} \bar{C}_{\text{CuO},(hkl)} &= \left\{ 4[E_1h^4 + E_2k^4 + E_3l^4 + 2(E_4h^2k^2 + E_5k^2l^2 + E_6h^2l^2) \right. \\ &\quad \left. + 4(E_7h^3k + E_8h^3l + E_9k^3h)]Y^4Z^4\sin^4\beta \right\} \\ &\quad \times \left( \{k^2Z^2 + 2Y^2(l^2 + h^2Z^2) - Z[4hlY^2\cos(\beta) + k^2Z\cos(2\beta)]\}^2 \right)^{-1}, \end{aligned} \quad (3.6.60)$$

where  $a$ ,  $b$ ,  $c$  and  $\beta$  are the unit-cell parameters of tenorite,  $Y = b/a$  and  $Z = c/a$ .

The dislocation density in  $\text{Cu}_2\text{O}$  is quite high [ $\rho = 2.8(5) \times 10^{16} \text{ m}^{-2}$ ]: dislocations are more of the edge character [ $f_E = 0.85(3)$ ] and the outer cutoff radius  $R_e = 9(3)$  nm leads to a Wilkens' parameter of approximately 1.5, suggesting a strong dislocation interaction. The high dislocation density in this material is justified by the very low shear modulus ( $G = 10.3$  GPa; Every & McCurdy, 1992b), whereas the high dislocation interaction is the result of the severe deformation induced by the milling.

#### APPENDIX A3.6.1 Functions for profile shapes

The unit-area Gaussian  $G(x, \omega)$  and Lorentzian  $L(x, \omega)$  functions are defined as

$$G(x, \omega) = \frac{2\sqrt{\ln 2/\pi}}{\omega} \exp\left(-\frac{4x^2 \ln 2}{\omega^2}\right), \quad (3.6.61)$$

$$L(x, \omega) = \frac{2}{\pi\omega} \left( \frac{1}{1 + 4x^2/\omega^2} \right), \quad (3.6.62)$$

where  $x$  is the running variable and  $\omega$  is the full-width at half-maximum. Based on these definitions, the Voigt and pseudo-Voigt are

$$V(x, \omega_L, \omega_G) = L(x, \omega_L) \otimes G(x, \omega_G) \quad (3.6.63)$$

and

$$pV(x, \omega_L, \omega_G) = \eta L(x, \omega_L) + (1 - \eta)G(x, \omega_G), \quad (3.6.64)$$

respectively, where  $\eta$  is the mixing parameter (ranging between 0 and 1) and  $\omega_L$  and  $\omega_G$  are the width of the Lorentzian and Gaussian components, respectively.

#### References

- Adler, T. & Houska, C. R. (1979). *Simplifications in the X-ray line-shape analysis*. *J. Appl. Phys.* **50**, 3282–3287.
- Alexander, L. (1954). *The synthesis of X-ray spectrometer line profiles with application to crystallite size measurements*. *J. Appl. Phys.* **25**, 155–161.
- Armstrong, N., Leoni, M. & Scardi, P. (2006). *Considerations concerning Wilkens' theory of dislocation line-broadening*. *Z. Kristallogr. Suppl.* **23**, 81–86.
- Balogh, L., Ribárik, G. & Ungár, T. (2006). *Stacking faults and twin boundaries in fcc crystals determined by X-ray diffraction profile analysis*. *J. Appl. Phys.* **100**, 023512.
- Balzar, D. & Popović, S. (1996). *Reliability of the simplified integral-breadth methods in diffraction line-broadening analysis*. *J. Appl. Cryst.* **29**, 16–23.
- Bergmann, J. & Kleeberg, R. (2001). *Fundamental parameters versus learnt profiles using the Rietveld program BGMN*. *Mater. Sci. Forum*, **378–381**, 30–37.
- Berkum, J. G. M. van (1994). *Strain Fields in Crystalline Materials*. PhD thesis, Technische Universiteit Delft, Delft, The Netherlands.
- Bertaut, E. F. (1949a). *Etude aux rayons X de la répartition des dimensions des cristallites dans une poudre cristalline*. *C. R. Acad. Sci.* **228**, 492–494.
- Bertaut, E. F. (1949b). *Signification de la dimension cristalline mesurée d'après la largeur de raie Debye-Scherrer*. *C. R. Acad. Sci.* **228**, 187–189.
- Bertaut, E. F. (1950). *Raies de Debye-Scherrer et répartition des dimensions des domaines de Bragg dans les poudres polycristallines*. *Acta Cryst.* **3**, 14–18.
- Beyerlein, K. R., Leoni, M. & Scardi, P. (2012). *Temperature diffuse scattering of nanocrystals*. *Acta Cryst.* **A68**, 382–392.
- Billinge, S. J. L. (2008). *Local structure from total scattering and atomic pair distribution function (PDF) analysis*. In *Powder Diffraction: Theory and Practice*, edited by R. E. Dinnebier & S. J. L. Billinge. London: Royal Society of Chemistry.
- Brese, N. E., O'Keeffe, M., Ramakrishna, B. L. & Von Dreele, R. B. (1990). *Low-temperature structures of CuO and AgO and their relationships to those of MgO and PdO*. *J. Solid State Chem.* **89**, 184–190.
- Bruker (2009). *DIFFRAC.SUITE TOPAS, Total Pattern Analysis Solution*. Version 5. Bruker AXS, Karlsruhe, Germany.
- Caglioti, G., Paoletti, A. & Ricci, F. P. (1958). *Choice of collimator for a crystal spectrometer for neutron diffraction*. *Nucl. Instrum.* **3**, 223–228.
- Cervellino, A., Giannini, C. & Guagliardi, A. (2003). *Determination of nanoparticle structure type, size and strain distribution from X-ray data for monatomic f.c.c.-derived non-crystallographic nanoclusters*. *J. Appl. Cryst.* **36**, 1148–1158.
- Cheary, R. W. & Coelho, A. (1992). *A fundamental parameters approach to X-ray line-profile fitting*. *J. Appl. Cryst.* **25**, 109–121.
- Cheary, R. W. & Coelho, A. (1994). *Synthesizing and fitting linear position-sensitive detector step-scanned line profiles*. *J. Appl. Cryst.* **27**, 673–681.
- Cheary, R. W. & Coelho, A. A. (1998a). *Axial divergence in a conventional X-ray powder diffractometer. I. Theoretical foundations*. *J. Appl. Cryst.* **31**, 851–861.
- Cheary, R. W. & Coelho, A. A. (1998b). *Axial divergence in a conventional X-ray powder diffractometer. II. Realization and evaluation in a fundamental-parameter profile fitting procedure*. *J. Appl. Cryst.* **31**, 862–868.
- Cline, J. P., Black, D., Windover, D. & Henins, A. (2010). *SRM 660b – Line Position and Line Shape Standard for Powder Diffraction*. [https://www.nist.gov/srmors/view\\_detail.cfm?srm=660b](https://www.nist.gov/srmors/view_detail.cfm?srm=660b).
- Coelho, A. A. (2005). *A bound constrained conjugate gradient solution method as applied to crystallographic refinement problems*. *J. Appl. Cryst.* **38**, 455–461.
- Coelho, A. A. (2009). *TOPAS Academic*. Version 5. <http://www.topas-academic.net/>.
- Cozzoli, P. D., Snoeck, E., Garcia, M. A., Giannini, C., Guagliardi, A., Cervellino, A., Gozzo, F., Hernando, A., Achterhold, K., Ciobanu, N., Parak, F. G., Cingolani, R. & Manna, L. (2006). *Colloidal synthesis and characterization of tetrapod-shaped magnetic nanocrystals*. *Nano Lett.* **6**, 1966–1972.
- Debye, P. (1915). *Zerstreuung von Röntgenstrahlen*. *Ann. Phys.* **351**, 809–823.

### 3. METHODOLOGY

- Deutsch, M., Forster, E., Holzer, G., Hartwig, J., Hämmäläinen, K., Kao, C.-C., Huotari, S. & Diamant, R. (2004). *X-ray spectrometry of copper: new results on an old subject*. *J. Res. Natl Inst. Stand. Technol.* **109**, 75–98.
- Dragomir, I. C. & Ungár, T. (2002). *Contrast factors of dislocations in the hexagonal crystal system*. *J. Appl. Cryst.* **35**, 556–564.
- Drits, V. A. & Tchoubar, C. (1990). *X-ray Diffraction by Disordered Lamellar Structures: Theory and Applications to Microdivided Silicates and Carbons*. Berlin: Springer-Verlag.
- Edwards, O. S. & Lipson, H. (1942). *Imperfections in the structure of cobalt. I. Experimental work and proposed structure*. *Proc. R. Soc. Lond. Ser. A*, **180**, 268–277.
- Egami, T. & Billinge, S. J. L. (2003). *Underneath the Bragg Peaks. Structural Analysis of Complex Materials*. Oxford: Elsevier.
- Estevez-Rams, E., Leoni, M., Scardi, P., Aragon-Fernandez, B. & Fuess, H. (2003). *On the powder diffraction pattern of crystals with stacking faults*. *Philos. Mag.* **83**, 4045–4057.
- Estevez-Rams, E., Welzel, U., Pentón Madrigal, A. & Mittemeijer, E. J. (2008). *Stacking and twin faults in close-packed crystal structures: exact description of random faulting statistics for the full range of faulting probabilities*. *Acta Cryst.* **A64**, 537–548.
- Every, A. G. & McCurdy, A. K. (1992a). *Landolt–Börnstein: Crystal and Solid State Physics New Series, Group III, Vol. 29*, edited by D. F. Nelson, p. 12. Berlin: Springer.
- Every, A. G. & McCurdy, A. K. (1992b). *Landolt–Börnstein: Crystal and Solid State Physics New Series, Group III, Vol. 29*, edited by D. F. Nelson, p. 68. Berlin: Springer.
- Garrod, R. I., Brett, J. F. & MacDonald, J. A. (1954). *X-ray line broadening and pure diffraction contours*. *Aust. J. Phys.* **7**, 77–95.
- Gevers, R. (1954a). *X-ray diffraction by close-packed crystals with ‘growth stacking faults’ assuming an ‘N-layer influence’*. *Acta Cryst.* **7**, 492–494.
- Gevers, R. (1954b). *X-ray diffraction by close-packed crystals with ‘growth-’ and ‘deformation or transformation stacking faults’ assuming an ‘N-layer influence’*. *Acta Cryst.* **7**, 740–744.
- Grebillé, D. & Bézar, J.-F. (1985). *Calculation of diffraction line profiles in the case of a major size effect: application to boehmite AlOOH*. *J. Appl. Cryst.* **18**, 301–307.
- Groma, I., Ungár, T. & Wilkens, M. (1988). *Asymmetric X-ray line broadening of plastically deformed crystals. I. Theory*. *J. Appl. Cryst.* **21**, 47–54.
- Hölzer, G., Fritsch, M., Deutsch, M., Härtwig, J. & Förster, E. (1997).  $K\alpha_{1,2}$  and  $K\beta_{1,3}$  X-ray emission lines of the 3d transition metals. *Phys. Rev. A*, **56**, 4554–4568.
- Houska, C. R. & Smith, T. M. (1981). *Least-squares analysis of X-ray diffraction line shapes with analytic functions*. *J. Appl. Phys.* **52**, 748.
- Jones, F. W. (1938). *The measurement of particle size by the X-ray method*. *Proc. R. Soc. Lond. Ser. A*, **166**, 16–43.
- Kaganer, V. M. & Sabelfeld, K. K. (2010). *X-ray diffraction peaks from correlated dislocations: Monte Carlo study of dislocation screening*. *Acta Cryst.* **A66**, 703–716.
- Kamminga, J.-D. & Delhez, R. (2000). *Calculation of diffraction line profiles from specimens with dislocations. A comparison of analytical models with computer simulations*. *J. Appl. Cryst.* **33**, 1122–1127.
- Kern, A. A. & Coelho, A. A. (1998). *A new fundamental parameters approach in profile analysis of powder data*. New Delhi: Allied Publishers.
- Klimanek, P. & Kuzel, R. (1988). *X-ray diffraction line broadening due to dislocations in non-cubic materials. I. General considerations and the case of elastic isotropy applied to hexagonal crystals*. *J. Appl. Cryst.* **21**, 59–66.
- Klug, H. P. & Alexander, L. E. (1974). *X-ray Diffraction Procedures for Polycrystalline and Amorphous Materials*, 2nd ed. New York: Wiley.
- Krill, C. E. & Birringer, R. (1998). *Estimating grain-size distributions in nanocrystalline materials from X-ray diffraction profile analysis*. *Philos. Mag. A*, **77**, 621–640.
- Krivoglaz, M. A. (1969). *Theory of X-ray and Thermal Neutron Scattering by Real Crystals*. New York: Plenum Press.
- Krivoglaz, M. A., Martynenko, O. V. & Ryaboshapka, K. P. (1983). *Influence of correlation in position of dislocations on X-ray diffraction by deformed crystals*. *Phys. Met. Metall.* **55**, 1–12.
- Krivoglaz, M. A. & Ryaboshapka, K. P. (1963). *Theory of X-ray scattering by crystals containing dislocations. Screw and edge dislocations randomly distributed throughout the crystal*. *Phys. Met. Metall.* **15**, 14–26.
- Kuzel, R. & Klimanek, P. (1989). *X-ray diffraction line broadening due to dislocations in non-cubic crystalline materials. III. Experimental results for plastically deformed zirconium*. *J. Appl. Cryst.* **22**, 299–307.
- Langford, J. I. & Louër, D. (1982). *Diffraction line profiles and Scherrer constants for materials with cylindrical crystallites*. *J. Appl. Cryst.* **15**, 20–26.
- Langford, J. I. & Wilson, A. J. C. (1978). *Scherrer after sixty years: a survey and some new results in the determination of crystallite size*. *J. Appl. Cryst.* **11**, 102–113.
- Leineweber, A. (2011). *Understanding anisotropic microstrain broadening in Rietveld refinement*. *Z. Kristallogr.* **226**, 905–923.
- Leineweber, A. & Mittemeijer, E. J. (2004). *Diffraction line broadening due to lattice-parameter variations caused by a spatially varying scalar variable: its orientation dependence caused by locally varying nitrogen content in  $\epsilon$ -FeN<sub>0.433</sub>*. *J. Appl. Cryst.* **37**, 123–135.
- Leineweber, A. & Mittemeijer, E. J. (2010). *Notes on the order-of-reflection dependence of microstrain broadening*. *J. Appl. Cryst.* **43**, 981–989.
- Lele, S. & Anantharaman, T. R. (1966). *Influence of crystallite shape on particle size broadening of Debye–Scherrer reflections*. *Proc. Indian Acad. Sci. A*, **64**, 261–274.
- Leonardi, A., Leoni, M., Siboni, S. & Scardi, P. (2012). *Common volume functions and diffraction line profiles of polyhedral domains*. *J. Appl. Cryst.* **45**, 1162–1172.
- Leoni, M. (2008). *Diffraction analysis of layer disorder*. *Z. Kristallogr.* **223**, 561–568.
- Leoni, M., Confente, T. & Scardi, P. (2006). *PM2K: a flexible program implementing whole powder pattern modelling*. *Z. Kristallogr. Suppl.* **23**, 249–254.
- Leoni, M., Di Maggio, R., Polizzi, S. & Scardi, P. (2004). *X-ray diffraction methodology for the microstructural analysis of nanocrystalline powders: application to cerium oxide*. *J. Am. Ceram. Soc.* **87**, 1133–1140.
- Leoni, M., Gualtieri, A. F. & Roveri, N. (2004). *Simultaneous refinement of structure and microstructure of layered materials*. *J. Appl. Cryst.* **37**, 166–173.
- Leoni, M., Martínez-García, J. & Scardi, P. (2007). *Dislocation effects in powder diffraction*. *J. Appl. Cryst.* **40**, 719–724.
- Leoni, M. & Scardi, P. (2004). *Nanocrystalline domain size distributions from powder diffraction data*. *J. Appl. Cryst.* **37**, 629–634.
- Leoni, M., Scardi, P. & Langford, J. I. (1998). *Characterization of standard reference materials for obtaining instrumental line profiles*. *Powder Diffr.* **13**, 210–215.
- Martínez-García, J., Leoni, M. & Scardi, P. (2007). *Analytical expression for the dislocation contrast factor of the {001}{100} cubic slip-system: Application to Cu<sub>2</sub>O*. *Phys. Rev. B*, **76**, 174117.
- Martínez-García, J., Leoni, M. & Scardi, P. (2008). *Analytical contrast factor of dislocations along orthogonal diad axes*. *Philos. Mag. Lett.* **88**, 443–451.
- Martínez-García, J., Leoni, M. & Scardi, P. (2009). *A general approach for determining the diffraction contrast factor of straight-line dislocations*. *Acta Cryst.* **A65**, 109–119.
- Matěj, Z., Matějová, L., Novotný, F., Drahokoupil, J. & Kuzel, R. (2011). *Determination of crystallite size distribution histogram in nanocrystalline anatase powders by XRD*. *Z. Kristallogr. Proc.* **1**, 87–92.
- Nakajima, A., Yoshihara, A. & Ishigame, M. (1994). *Defect-induced Raman spectra in doped CeO<sub>2</sub>*. *Phys. Rev. B*, **50**, 13297–13307.
- Nye, J. F. (1987). *Physical Properties of Crystals: Their Representation by Tensors and Matrices*, reprint edition. Oxford University Press.
- Paterson, M. S. (1952). *X-ray diffraction by face-centered cubic crystals with deformation faults*. *J. Appl. Phys.* **23**, 805–811.
- Patterson, A. L. (1939). *The Scherrer formula for X-ray particle size determination*. *Phys. Rev.* **56**, 978–982.
- Pawley, G. S. (1981). *Unit-cell refinement from powder diffraction scans*. *J. Appl. Cryst.* **14**, 357–361.
- Popa, N. C. (1998). *The (hkl) dependence of diffraction-line broadening caused by strain and size for all Laue groups in Rietveld refinement*. *J. Appl. Cryst.* **31**, 176–180.
- Rao, S. & Houska, C. R. (1986). *X-ray diffraction profiles described by refined analytical functions*. *Acta Cryst.* **A42**, 14–19.
- Ribárik, G. (2008). *Modeling of Diffraction Patterns Properties*. PhD thesis, Eötvös University, Budapest.

### 3.6. WHOLE POWDER PATTERN MODELLING

- Ribárik, G., Gubicza, J. & Ungár, T. (2004). *Correlation between strength and microstructure of ball-milled Al–Mg alloys determined by X-ray diffraction. Mater. Sci. Eng. A Struct. Mater.* **387–389**, 343–347.
- Rietveld, H. M. (1969). *A profile refinement method for nuclear and magnetic structures. J. Appl. Cryst.* **2**, 65–71.
- Scardi, P. & Leoni, M. (1999). *Fourier modelling of the anisotropic line broadening of X-ray diffraction profiles due to line and plane lattice defects. J. Appl. Cryst.* **32**, 671–682.
- Scardi, P. & Leoni, M. (2001). *Diffraction line profiles from polydisperse crystalline systems. Acta Cryst.* **A57**, 604–613.
- Scardi, P. & Leoni, M. (2002). *Whole powder pattern modelling. Acta Cryst.* **A58**, 190–200.
- Scardi, P. & Leoni, M. (2004). *Whole powder pattern modelling: theory and application. In Diffraction Analysis of the Microstructure of Materials*, edited by E. J. Mittemeijer & P. Scardi, pp. 51–91. Berlin: Springer-Verlag.
- Scardi, P. & Leoni, M. (2005). *Diffraction whole-pattern modelling study of anti-phase domains in Cu<sub>3</sub>Au. Acta Mater.* **53**, 5229–5239.
- Scardi, P., Leoni, M. & Beyerlein, K. R. (2011). *On the modelling of the powder pattern from a nanocrystalline material. Z. Kristallogr.* **226**, 924–933.
- Scardi, P., Leoni, M. & Delhez, R. (2004). *Line broadening analysis using integral breadth methods: a critical review. J. Appl. Cryst.* **37**, 381–390.
- Scardi, P., Leoni, M., Müller, M. & Di Maggio, R. (2010). *In situ size-strain analysis of nanocrystalline ceria growth. Mater. Sci. Eng. A Struct. Mater.* **528**, 77–82.
- Scardi, P., Leoni, M., Straffelini, G. & Giudici, G. D. (2007). *Microstructure of Cu–Be alloy trioxidative wear debris. Acta Mater.* **55**, 2531–2538.
- Scherrer, P. (1918). *Bestimmung der Größe und der inneren Struktur von Kolloidteilchen mittels Röntgenstrahlen. Nachr. Ges. Wiss. Göttingen*, pp. 98–100.
- Stephens, P. W. (1999). *Phenomenological model of anisotropic peak broadening in powder diffraction. J. Appl. Cryst.* **32**, 281–289.
- Stokes, A. R. & Wilson, A. J. C. (1942). *A method of calculating the integral breadths of Debye–Scherrer lines. Math. Proc. Cambridge Philos. Soc.* **38**, 313–322.
- Stokes, A. R. & Wilson, A. J. C. (1944). *The diffraction of X-rays by distorted crystal aggregates – I. Proc. Phys. Soc.* **56**, 174–181.
- Treacy, M. M. J., Newsam, J. M. & Deem, M. W. (1991). *A general recursion method for calculating diffracted intensities from crystals containing planar faults. Proc. R. Soc. Lond. Ser. A*, **433**, 499–520.
- Tromans, D. & Meech, J. A. (2001). *Enhanced dissolution of minerals: stored energy, amorphism and mechanical activation. Miner. Eng.* **14**, 1359–1377.
- Ungár, T. (2001). *Dislocation densities, arrangements and character from X-ray diffraction experiments. Mater. Sci. Eng. A Struct. Mater.* **309–310**, 14–22.
- Ungár, T. & Borbély, A. (1996). *The effect of dislocation contrast on X-ray line broadening: a new approach to line profile analysis. Appl. Phys. Lett.* **69**, 3173.
- Ungár, T., Dragomir, I., Révész, Á. & Borbély, A. (1999). *The contrast factors of dislocations in cubic crystals: the dislocation model of strain anisotropy in practice. J. Appl. Cryst.* **32**, 992–1002.
- Ungár, T., Gubicza, J., Ribárik, G. & Borbély, A. (2001). *Crystallite size distribution and dislocation structure determined by diffraction profile analysis: principles and practical application to cubic and hexagonal crystals. J. Appl. Cryst.* **34**, 298–310.
- Ungár, T. & Tichy, G. (1999). *The effect of dislocation contrast on X-ray line profiles in untextured polycrystals. Phys. Stat. Solidi A Appl. Res.* **171**, 425–434.
- Vargas, R., Louër, D. & Langford, J. I. (1983). *Diffraction line profiles and Scherrer constants for materials with hexagonal crystallites. J. Appl. Cryst.* **16**, 512–518.
- Velterop, L., Delhez, R., de Keijser, Th. H., Mittemeijer, E. J. & Reefman, D. (2000). *X-ray diffraction analysis of stacking and twin faults in f.c.c. metals: a revision and allowance for texture and non-uniform fault probabilities. J. Appl. Cryst.* **33**, 296–306.
- Warren, B. E. (1959). *X-ray studies of deformed metals. Progr. Met. Phys.* **8**, 147–202.
- Warren, B. E. (1963). *Single- and double-deformation faults in face-centered cubic crystals. J. Appl. Phys.* **34**, 1973–1975.
- Warren, B. E. (1990). *X-ray Diffraction*. New York: Dover Publications. (Unabridged reprint of the original 1969 book.)
- Warren, B. E. & Averbach, B. L. (1950). *The effect of cold-work distortion on X-ray patterns. J. Appl. Phys.* **21**, 595–599.
- Warren, B. E. & Averbach, B. L. (1952). *The separation of cold-work distortion and particle size broadening in X-ray patterns. J. Appl. Phys.* **23**, 492.
- Welberry, T.R. (2004). *Diffuse X-ray Scattering and Models of Disorder*. Oxford University Press.
- Wilkins, M. (1970a). *The determination of density and distribution of dislocations in deformed single crystals from broadened X-ray diffraction profiles. Phys. Stat. Solidi A Appl. Res.* **2**, 359–370.
- Wilkins, M. (1970b). *Fundamental Aspects of Dislocation Theory*, edited by J. A. Simmons, R. de Wit & R. Bullough, Vol. II, pp. 1195–1221. Washington DC: National Institute of Standards and Technology.
- Wilkins, M. (1987). *X-ray line broadening and mean square strains of straight dislocations in elastically anisotropic crystals of cubic symmetry. Phys. Stat. Solidi A Appl. Res.* **104**, K1–K6.
- Williamson, G. K. & Hall, W. H. (1953). *X-ray line broadening from filed aluminium and wolfram. Acta Metall.* **1**, 22–31.
- Wilson, A. J. C. (1942). *Imperfections in the structure of cobalt. II. Mathematical treatment of proposed structures. Proc. R. Soc. Lond. Ser. A*, **180**, 277–285.
- Wilson, A. J. C. (1943). *The reflexion of X-rays from the ‘anti-phase nuclei’ of AuCu<sub>3</sub>. Proc. R. Soc. Lond. Ser. A*, **181**, 360–368.
- Wilson, A. J. C. (1963). *Mathematical Theory of X-ray Powder Diffractometry*. New York: Gordon & Breach.
- Wilson, A. J. C. (1969). *Variance apparent particle sizes for cylinders, prisms and hemispheres. J. Appl. Cryst.* **2**, 181–183.
- Wilson, A. J. C. & Zsoldos, L. (1966). *The reflexion of X-rays from the ‘anti-phase nuclei’ of AuCu<sub>3</sub>. II. Proc. R. Soc. Lond. Ser. A*, **290**, 508–514.