

3. METHODOLOGY

3.9.4.4. Matrix flushing

Once the correct value of RIR is determined for each phase, the matrix-flushing method can be applied using equation (3.9.15). For fluorite in sample 1D, the calculation proceeds as follows:

$$W_{\text{fluorite}} = \frac{I_{\text{fluorite}}/\text{RIR}_{\text{fluorite}}}{\sum_{k=1}^n I_k/\text{RIR}_{k_s}} = \frac{6559.6/3.617}{474.5/1.0 + 6559.6/3.617 + 5468.5/4.856} = 0.5312, \quad (3.9.33)$$

compared with a value of 0.5358 added to the sample by weight. Fig. 3.9.4 shows the bias for fluorite in all samples analysed by the matrix-flushing method. Once again, there is good agreement between the weighed and analysed amounts. However, it is worth reiterating that this method normalizes the sum of all analysed weight fractions to unity. If amorphous or non-analysed phases are present in the sample, then the weight fractions will be overestimated relative to their absolute abundances.

3.9.4.5. Rietveld-based methods

The strengths and weaknesses of some of the methods described in Section 3.9.3 are highlighted through a study of the mechanism and kinetics of nucleation and crystal growth in the context of the Bayer process for the extraction of aluminium from bauxite ores (Webster *et al.*, 2010). Specifically, the experiments utilize synthetic Bayer liquors, consisting of Al-loaded caustic solutions to which a variety of seed material is added. Several polymorphs of $\text{Al}(\text{OH})_3$ (gibbsite, bayerite and nordstrandite) crystallize from solution onto the seed material. The rate of crystallization and the ratio of the phases formed depend on the sample conditions used, including the Al and caustic concentrations in solution, as well as sample temperature.

The mechanism and rate of crystallization were followed by collecting XRD data at the powder-diffraction beamline of the Australian Synchrotron⁴ over a period of about 3 h. The diffractometer incorporates a Mythen detector (Schmitt *et al.*,

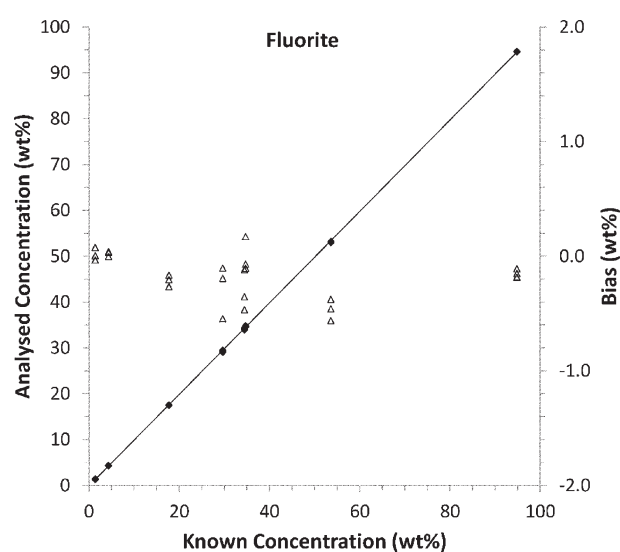


Figure 3.9.4

Plot of the analysed concentration (black diamonds – left axis) and the bias (open triangles – right axis) expressed as wt% for fluorite using the matrix-flushing method with RIRs of 1.0, 3.617 and 4.856 for corundum, fluorite and zincite, respectively. The RIRs were determined using sample 1H where the corundum, fluorite and zincite concentrations are 35.12, 34.69 and 30.19 wt%, respectively.

2003) which allows for the simultaneous collection of $80^\circ 2\theta$ of the diffraction pattern. A wavelength of 0.826 \AA was used to ensure adequate penetration of the beam in the sample. The sample environment (Madsen *et al.*, 2005; Norby *et al.*, 1998) consisted of a 1-mm quartz glass capillary containing a slurry of the seed and Bayer liquor heated to temperatures between 333 and 348 K using a hot-air blower.

The data were analysed using TOPAS (Bruker AXS, 2013), where a learned-profile approach to peak modelling was used with an empirical instrument width and shape contribution determined using the NIST SRM660 LaB_6 profile standard. For the samples in the study, refined parameters included 2θ zero offset, a Chebychev polynomial pattern background and, for each phase, the Rietveld scale factor, crystallite size and strain, and unit-cell dimensions.

A number of different approaches were used to extract the phase abundances at each stage of the reaction. Initially, QPA was derived using equation (3.9.26); the value that many Rietveld analysis programs output as their first estimate of phase abundance. Fig. 3.9.5 shows the QPA output from an *in situ* experiment in which goethite (FeOOH) was added as the seed.

At the start of the experiment, prior to the crystallization of any of the $\text{Al}(\text{OH})_3$ polymorphs, Fig. 3.9.5 shows that the reported concentration of the goethite seed is 100 wt% since it is the only phase represented in the analysis at that time. On formation of gibbsite, bayerite and nordstrandite, the goethite concentration appears to decrease progressively to about 65 wt% while the total $\text{Al}(\text{OH})_3$ concentration reaches about 35 wt% at the end of the experiment. However, these figures are in disagreement with (i) the fact that goethite is unlikely to dissolve or otherwise be consumed in this system (Murray *et al.*, 2009), (ii) the known addition of goethite to the sample (14.13 wt%) and (iii) the total amount of $\text{Al}(\text{OH})_3$ available from solution (15.92 wt%). The problem with the QPA in this case arises from the fact that only the crystalline components are considered in the analysis and that equation (3.9.26) normalizes the sum of their analysed weight fractions to unity. However, aluminium, which is in solution at the start of the run, forms crystalline phases continuously throughout the reaction after an initial induction period. In order to overcome the anomalies in the QPA results, it is necessary to consider the sample as a whole; that is, the concentration of both the solid and liquid components in the X-ray beam for the duration of the experiment.

In this sample, the concentration of the goethite seed was 14.13 wt% in the slurry injected into the sample capillary. If the assumption is made that, in this environment, goethite is unreactive and its concentration will not change during the reaction, it can be used as an internal standard to put the $\text{Al}(\text{OH})_3$ concentrations on an absolute basis. The QPA results derived using the internal standard or ‘spiked’ approach in equation (3.9.25) are shown in Fig. 3.9.6.

The goethite concentration is fixed at the known addition (14.13 wt%) at the start of the experiment. However, the concentrations of the $\text{Al}(\text{OH})_3$ polymorphs are now put on an absolute scale, thus allowing derivation of more meaningful reaction mechanisms.

If, however, there is residual doubt about the reactivity of the goethite, it may be necessary to use the external standard approach embodied in equation (3.9.21). In this case, the value for the instrument constant, K , can be derived using the Rietveld scale factor, ZMV and the known addition of goethite in a

⁴ Australian Synchrotron beamtime award number AS091/PD1035.

rearranged equation (3.9.21). For this determination, the goethite scale factor from the first few data sets, prior to the start of the reaction, was averaged to minimize any errors that may be introduced by counting statistics. The value of the sample mass absorption coefficient μ_m^* was set to an arbitrary value of unity for both the determination of K and all subsequent analyses, since the overall chemical content of the capillary, and hence the attenuation of the X-ray beam, does not change during the reaction.

This experimental work was conducted at the Australian Synchrotron where the storage-ring current was boosted every 12 h. Between these times the current, and hence the incident-beam intensity, decays, resulting in what amounts to a change in the ‘instrument configuration’. This requires a modification of the K value and subsequent calculation of concentration to compensate for the changing incident intensity using equation (3.9.22).

Fig. 3.9.7 now shows the results of QPA derived from equation (3.9.22). In this case the concentrations of the $\text{Al}(\text{OH})_3$ polymorphs are similar to those in Fig. 3.9.6. However, since the phase abundances are derived using an external standard approach, any changes in the apparent goethite concentration can now be monitored. Fig. 3.9.7 shows that the goethite concentration did not change significantly in the early stages of the experiment ($t < 10$ min) before $\text{Al}(\text{OH})_3$ crystallization was observed but there is a small, systematic decrease in the apparent goethite concentration as the experiment progresses. At the end of the experiment, the goethite concentration appears to be lower by about 1% relative to the concentration at the start.

This apparent decrease could be due to a number of causes including (i) poor correction for beam-intensity changes or (ii) solid material moving about in the capillary with some movement out of the X-ray beam. Alternatively, the decrease could be attributed to the ‘shielding’ of the goethite from the X-ray beam by the $\text{Al}(\text{OH})_3$ phases as they form and coat the goethite particles. This decrease could then be used to obtain an average thickness of the $\text{Al}(\text{OH})_3$ phases on the seed particles. This layer was calculated to be about $5.5 \mu\text{m}$ (assuming a linear absorption coefficient of 9.5 cm^{-1} for gibbsite at 0.826 \AA) resulting in an overall particle size of about $11 \mu\text{m}$ at the end of the run (the goethite particles are about $0.2 \times 2 \mu\text{m}$ and hence do not contribute significantly to the overall particle size). These values are in good agreement with independent studies (Webster *et al.*, 2010) where the gibbsite was examined using scanning electron microscopy (SEM) techniques (Fig. 3.9.8) following crystallization under similar conditions to those used here.

3.9.5. Alternative methods for determination of calibration constants

3.9.5.1. Standardless determination of the phase constant C

In order to determine the phase calibration constant C , it is common to obtain (i) a pure sample of the phase of interest that accurately reflects the form of the phase in the samples to be analysed, or (ii) a multiphase sample in which the phase concentration is known by other means (for example, chemical analysis or point counting). In some systems, there may be insufficient sample available to risk ‘contaminating’ it with an internal standard, especially if the material needs to be analysed using other techniques. The addition of an internal standard may also introduce microabsorption problems or increase the complexity of patterns that are already highly overlapped. For

other situations, the time frame demanded for the analysis may prohibit the time-consuming procedures of standard addition, data collection and separate determination of the phase calibration constant.

Zevin & Kimmel (1995) have described an approach to the derivation of phase constants which relies on having a suite of samples to be analysed that (i) have the same phases present in all samples and (ii) exhibit a wide range of composition of these phases in various samples in order to stabilize the analysis. If we reconsider the relationship between the weight fraction W_α and the observed intensity [equation (3.9.3)],

$$W_\alpha = \frac{I_\alpha \mu_m^*}{C_\alpha}, \quad (3.9.34)$$

and assume that all phases in the system are known and included in the analysis, we can introduce the additional constraint that the sum of all W_α 's is unity (or at least a known value):

$$\sum_{j=1}^n W_j = 1.0. \quad (3.9.35)$$

In a system of n samples containing m phases, we can explicitly write the relationships expressed in equations (3.9.34) and (3.9.35) as a set of simultaneous equations:

$$\begin{aligned} 1.0 &= \frac{1}{C_1} I_{11} \mu_1^* + \frac{1}{C_2} I_{12} \mu_1^* + \dots + \frac{1}{C_m} I_{1m} \mu_1^*, \\ 1.0 &= \frac{1}{C_1} I_{21} \mu_2^* + \frac{1}{C_2} I_{22} \mu_2^* + \dots + \frac{1}{C_m} I_{2m} \mu_2^*, \\ 1.0 &= \frac{1}{C_1} I_{n1} \mu_n^* + \frac{1}{C_2} I_{n2} \mu_n^* + \dots + \frac{1}{C_m} I_{nm} \mu_n^*, \end{aligned} \quad (3.9.36)$$

where μ_n^* is the mass absorption coefficient for the n th sample.

Knudsen (1981) has described a modification to this approach by including an internal standard in each of the samples to be analysed and using the ratio of intensities of the analyte and internal standard phases in place of the I_{nm} in equation (3.9.36). While this eliminates the need to determine and use the mass absorption coefficient, the tedious procedure of adding and mixing an internal standard is required for each sample and for reasons described above may not be appropriate.

The relationships embodied in equations (3.9.36) can be expressed more simply in matrix notation as

$$\mathbf{L}' = \mathbf{I}'\mathbf{C}', \quad (3.9.37)$$

where \mathbf{L}' is a column vector (dimensions $1 \times n$) containing the known (or assumed) sum of weight fractions for each sample (unity in this case), \mathbf{C}' is a column vector (dimensions $1 \times m$) containing the calibration constants for each phase and \mathbf{I}' is a rectangular matrix (dimensions n rows \times m columns) containing the measured peak intensities (or scale factors) for each phase multiplied by the sample mass absorption coefficient.

A least-squares solution of equation (3.9.37) to derive the value for C for each phase can be calculated using matrix-manipulation methods (Knudsen, 1981):

$$\mathbf{C}' = (\mathbf{I}'^T \mathbf{I}')^{-1} \mathbf{I}'^T \mathbf{L}', \quad (3.9.38)$$

where the superscripts T and -1 represent the transpose and inverse matrix functions, respectively.

Accuracy in the calculation of the individual values of C is improved by having (i) phases of the same or similar composition in all samples and (ii) a wide range of concentrations of each phase across the sample suite. These conditions may be met in,